

How and Why to go Beyond the Discovery of the Higgs Boson

John Alison

University of Chicago

<http://hep.uchicago.edu/~johnda/ComptonLectures.html>

Lecture Outline

April 1st: Newton's dream & 20th Century Revolution

April 8th: Mission Barely Possible: QM + SR

April 15th: *The Standard Model*

April 22nd: Importance of the Higgs

April 29th: Guest Lecture

May 6th: The Cannon and the Camera

May 13th: The Discovery of the Higgs Boson

May 20th: Experimental Challenges

May 27th: Memorial Day: No Lecture

June 3rd: Going beyond the Higgs: What comes next ?

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June 3rd: Going beyond the Standard Model

Sources:

- Nima Arkani-Hamed
- Steven Weinberg
- ...

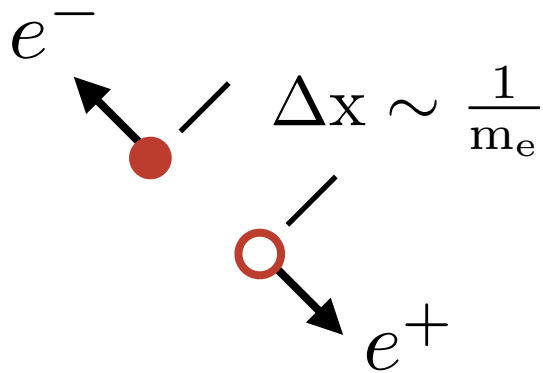
I will keep this list up to date as we go along.

Reminder: Last Lecture

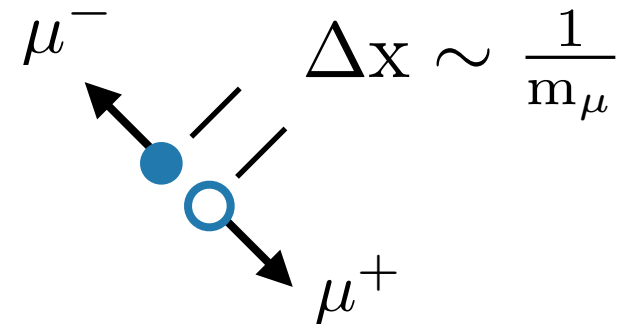
Combining Relativity and Quantum Mechanics

- To preserve causality needed to Anti-particle must exist
- In turn, major implications on the vacuum:

$$\Delta E > 2m_e c^2$$



$$\Delta E > 2m_\mu c^2$$



Reminder: Last Lecture

Combining Relativity and Quantum Mechanics

- Massive restrictions in types of theories possible

- Forced to talk particle spin:

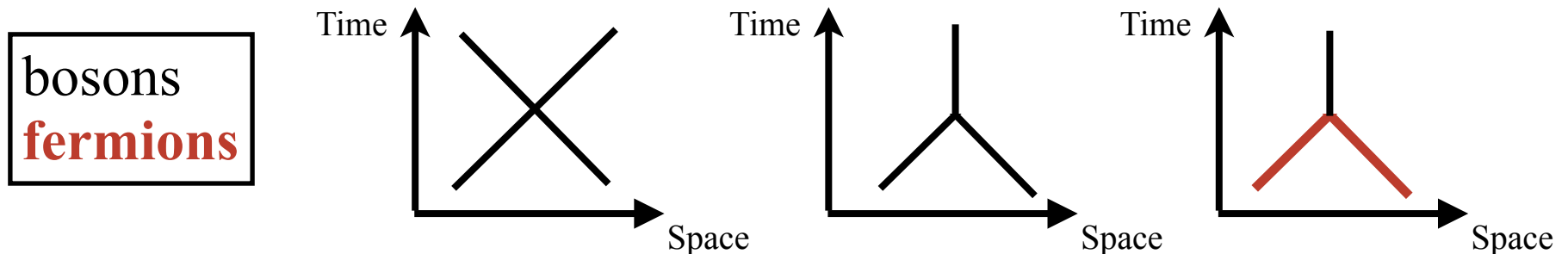
Integer spin = Bosons / Half-integer = Fermions

Can only have: 0 1/2 1 3/2 2

- Major limits to possible interaction:

Charge conservation / Local in space-time

Only finite number of specific interactions allowed :



bosons
fermions

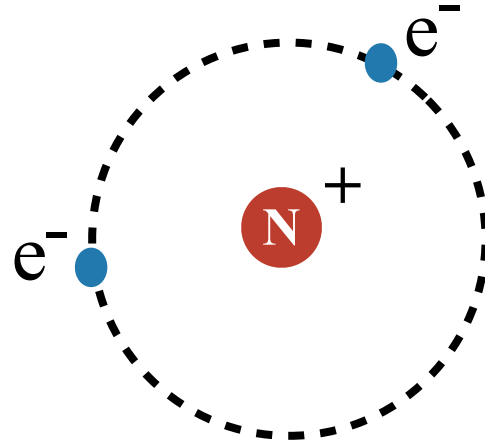
Today's Lecture

The Standard Model:

What the world is made of

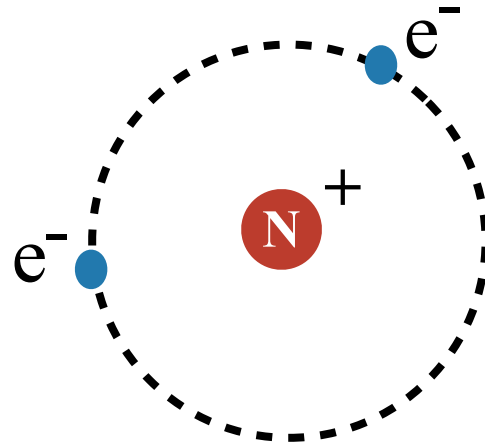
Matter

Stuff in the world made of atoms:



Matter

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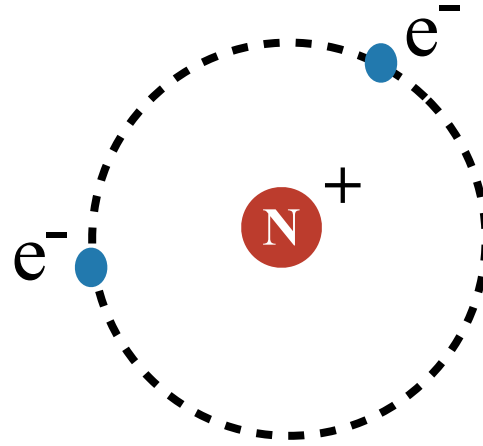
Atoms made of:

Electrons:

Nucleus:

Matter

Stuff in the world made of atoms:



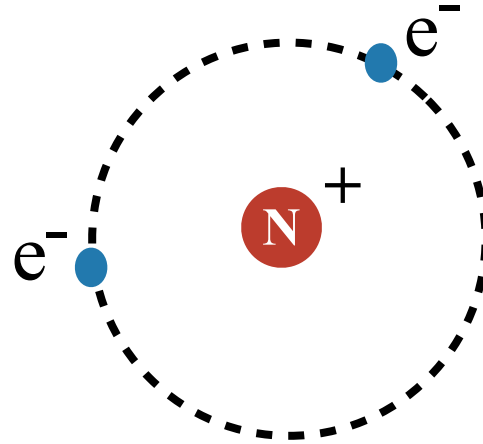
Atoms made of:

Electrons: Negatively charged
Responsible for volume of atom
Thought to be fundamental

Nucleus:

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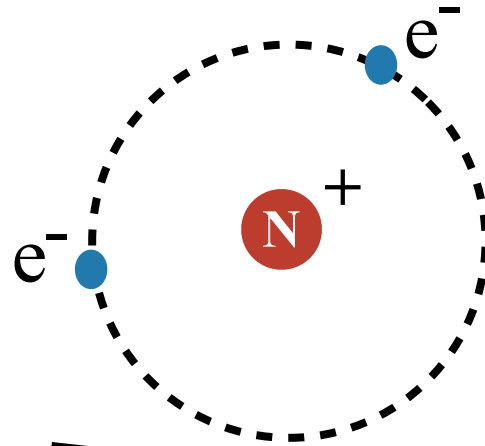
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Made of, protons and neutrons, which are made of quarks
Quarks also thought to be fundamental

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*Matter particles (electrons/quarks) fermions
Large collections behave like classical particles*

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Forces

Gravity:

Known since antiquity / Inverse square law

Always attractive / Irrelevant for atomic/sub-atomic interactions

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Discovered early 1900s / Short distances / No simple relationship

Responsible for holding together the nucleus

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Weak:

Discovered just before turn of 20th century / Looks nothing like others

Radioactive decay. Heats the sun / earth

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*All forces as important.
Look very different from one another*

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The particular version of QFT that was found to describe our universe developed in the 1960-70s.

Most accurate theory in all of science

- Describes all matter/interactions down to 10^{-18}m

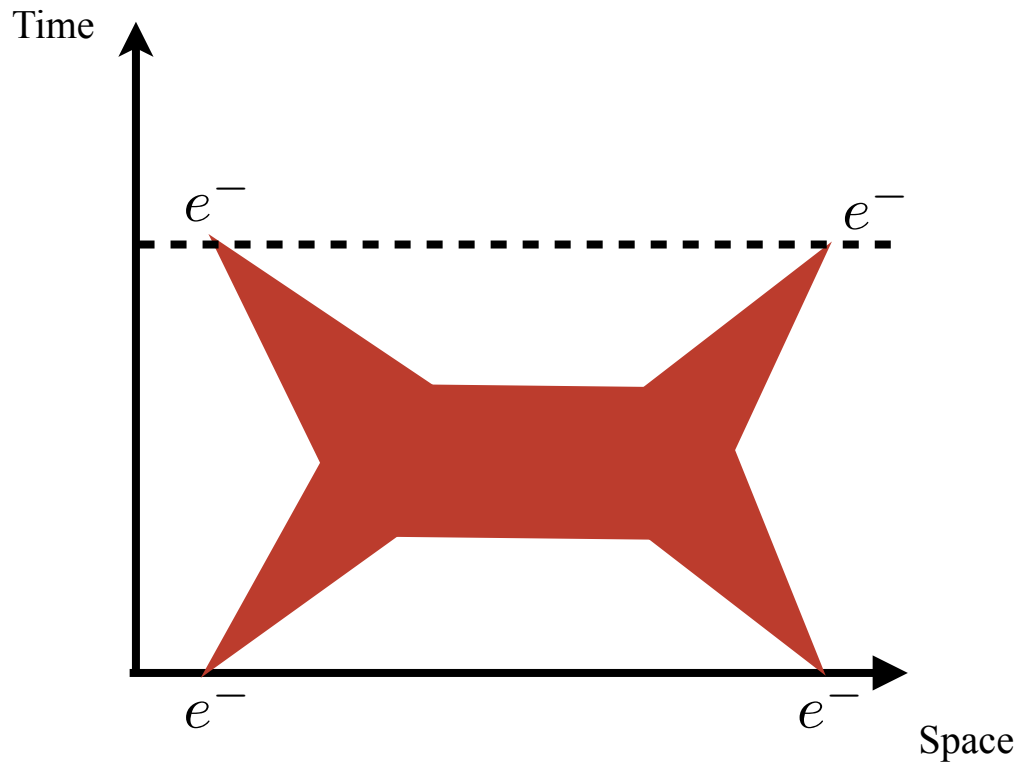
 - (Distances $100 \times$ smaller than proton)

- Accurate/precise description all observed particle interactions

Output of the Theory

Predict probabilities for various things to happen

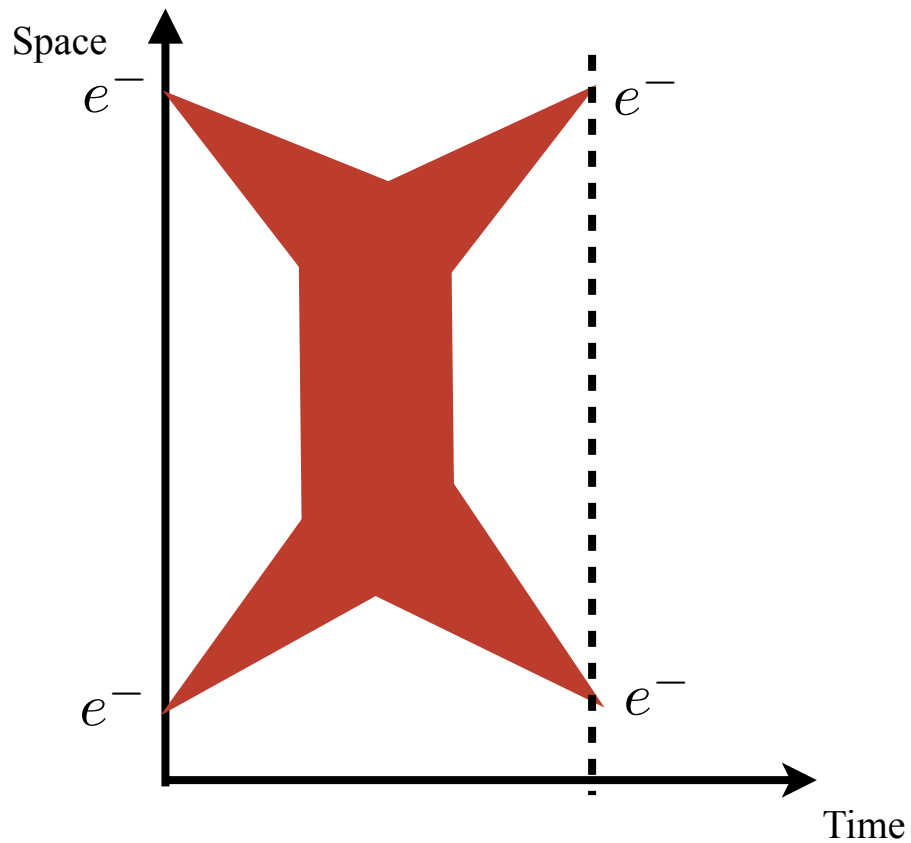
Example:



Output of the Theory

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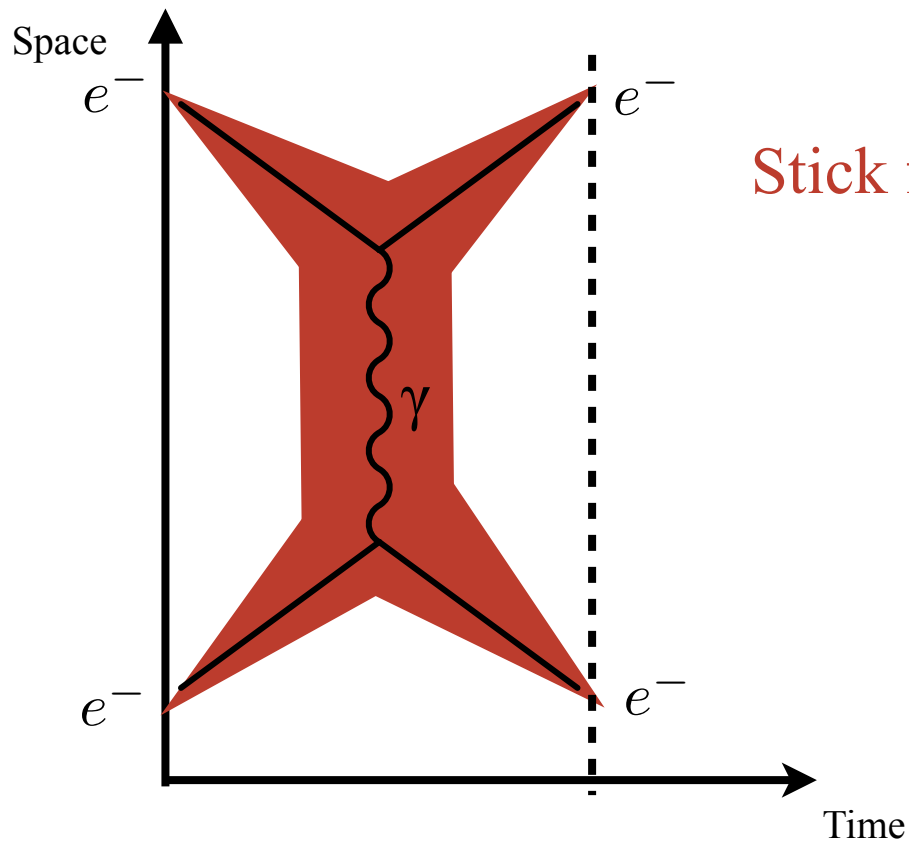
Example:



Output of the Theory

Predict probabilities for various things to happen

Example:

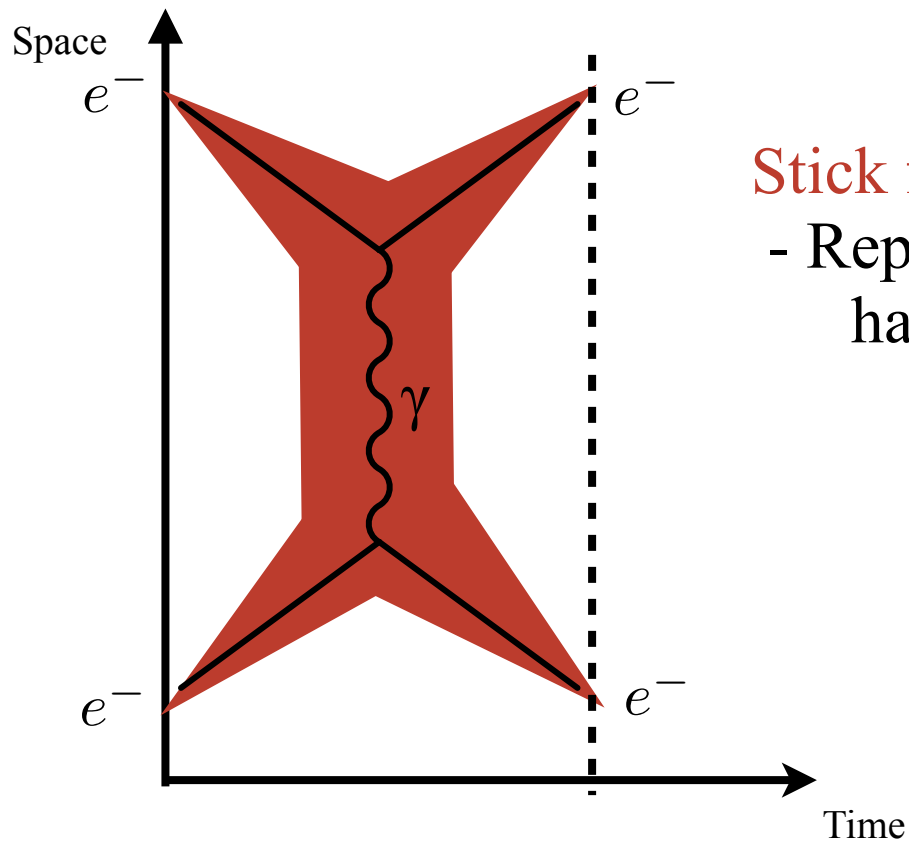


Stick figure: “*Feynman Diagram*”

Output of the Theory

Predict probabilities for various things to happen

Example:



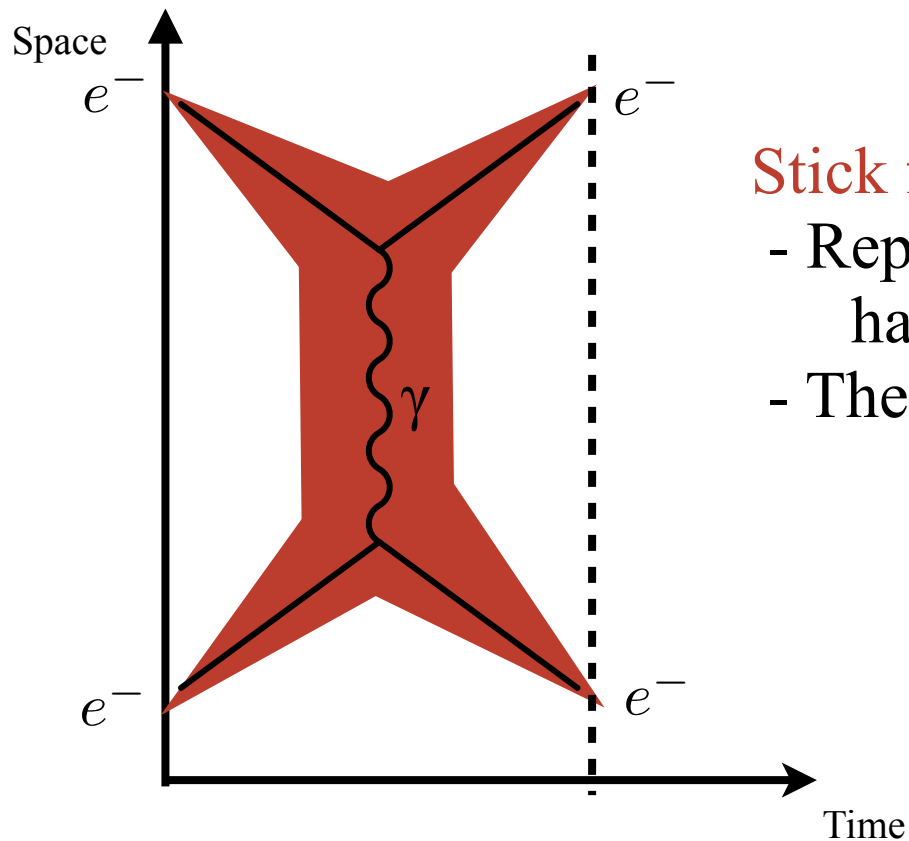
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- Represents one possible way things could have happened

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Example:



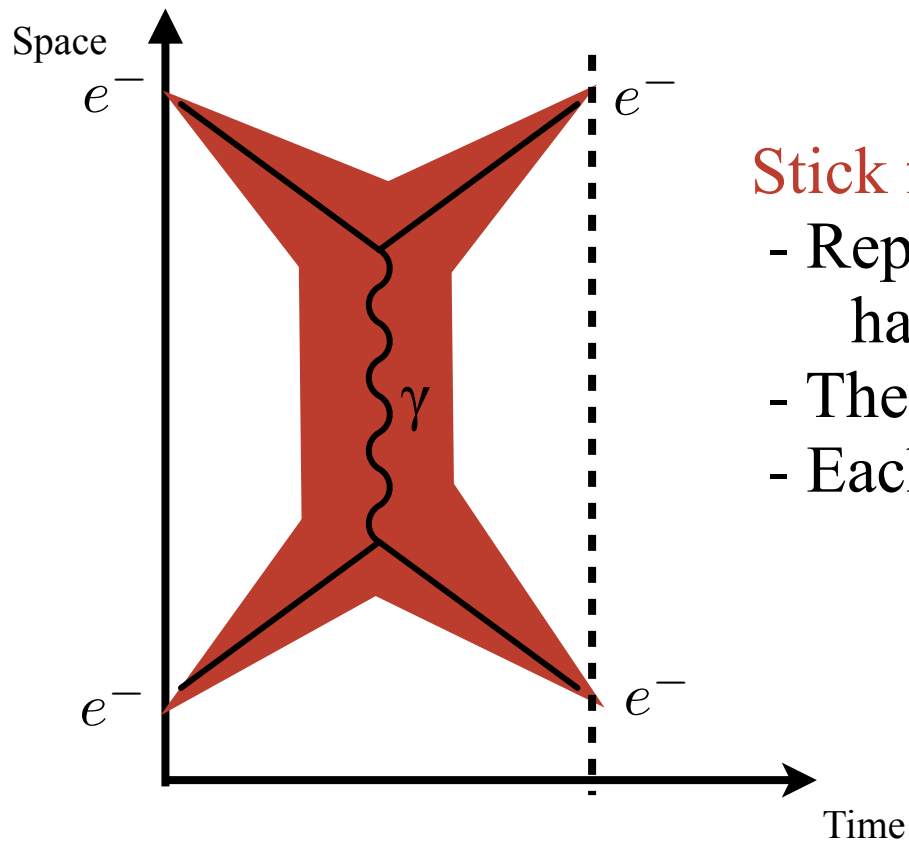
Stick figure: “*Feynman Diagram*”

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- Theory assigns number to each diagram

Output of the Theory

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Example:



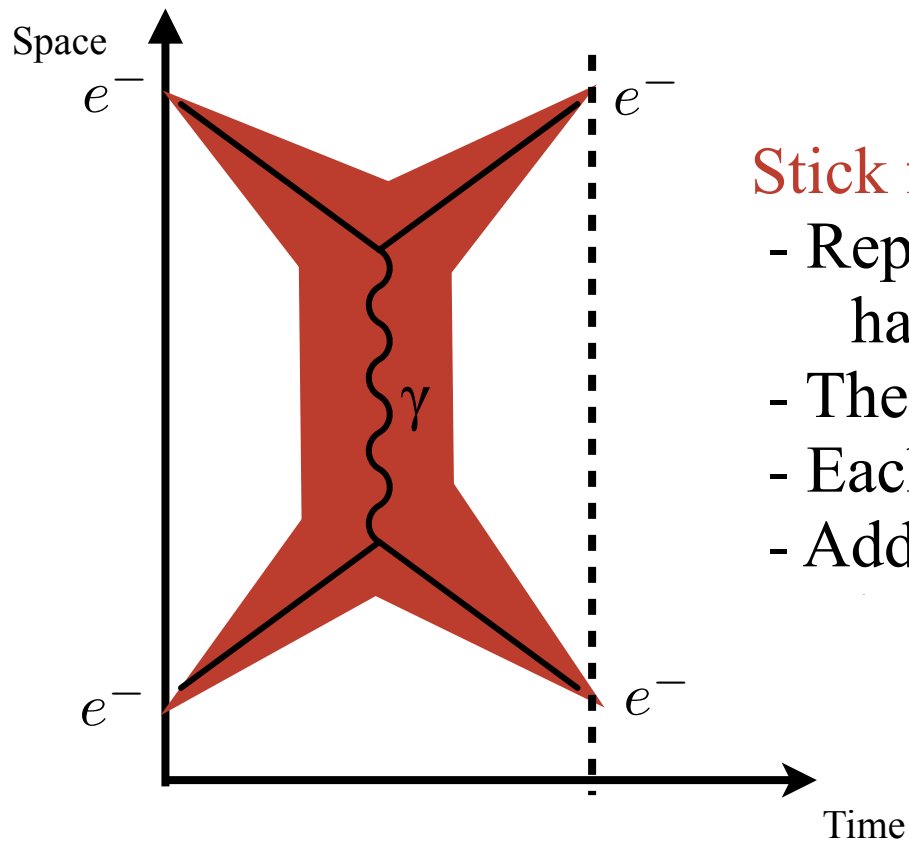
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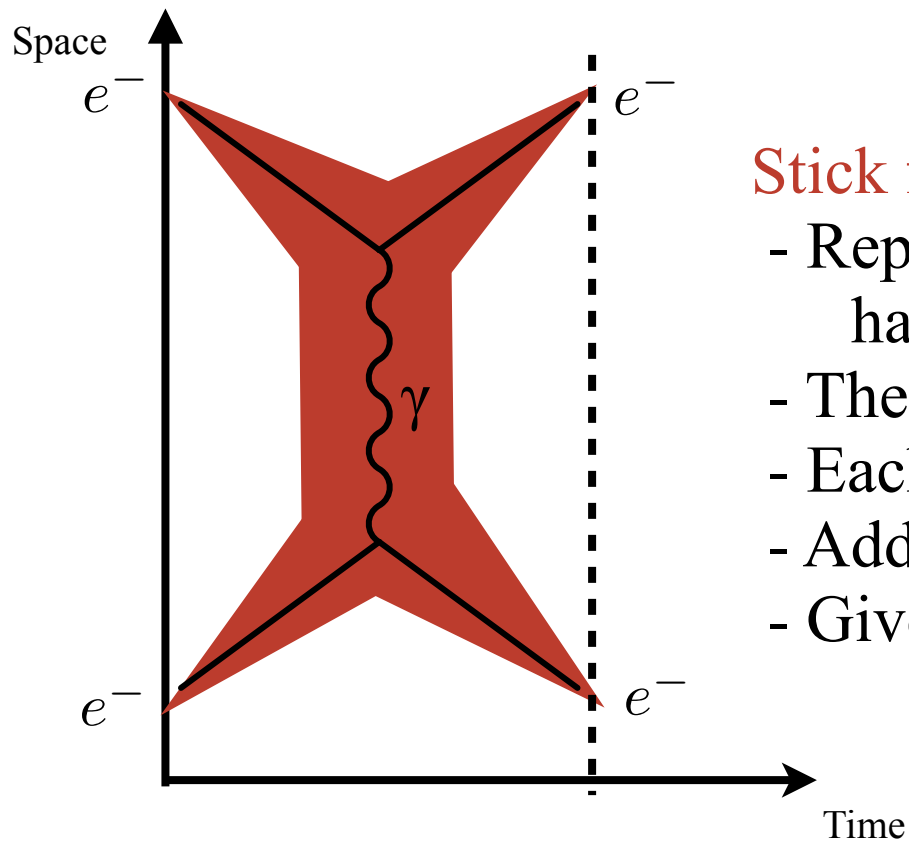
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- Add all paths consistent w/input & output

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Example:



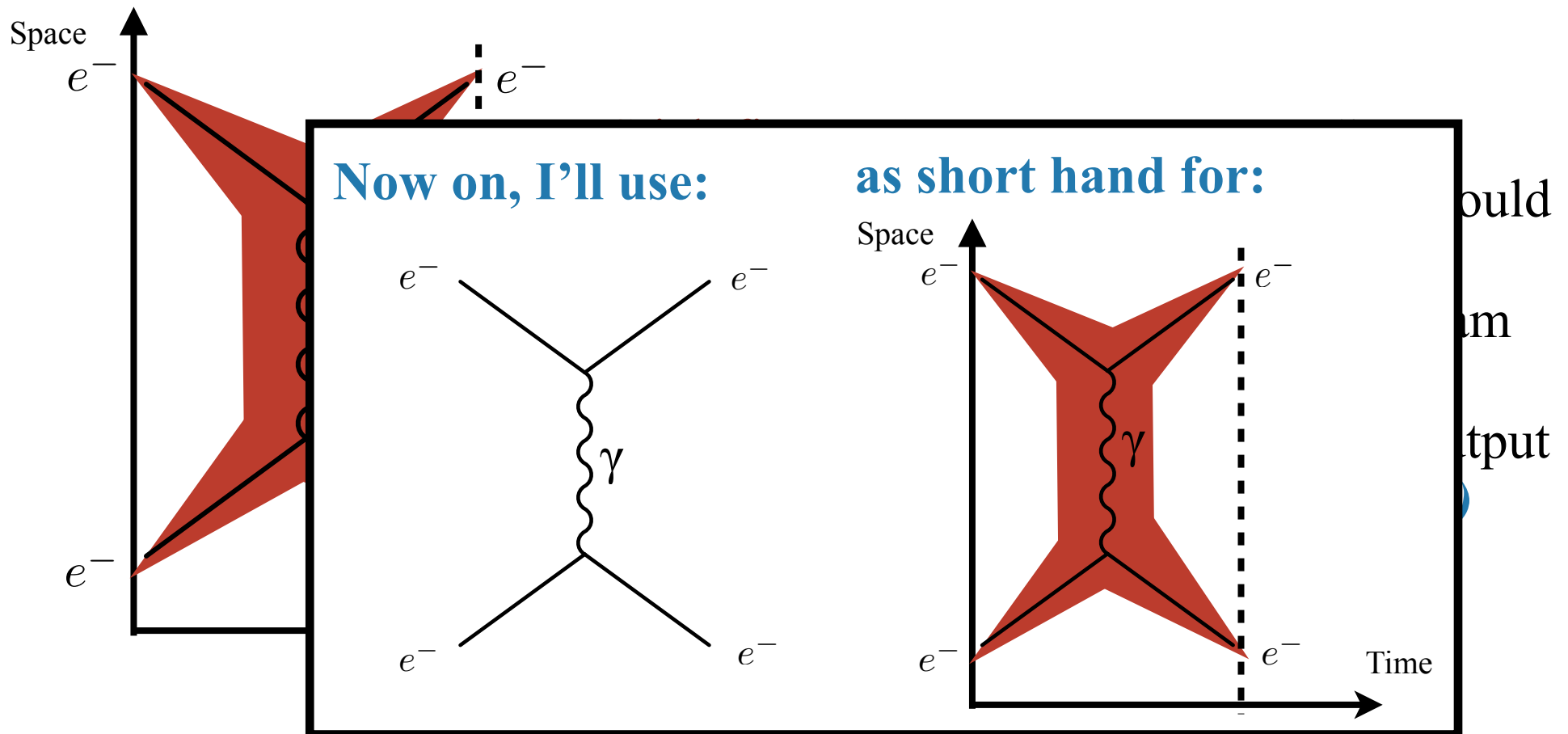
Stick figure: “*Feynman Diagram*”

- Represents one possible way things could have happened
- Theory assigns number to each diagram
- Each diagram only local interactions
- Add all paths consistent w/input & output
- Gives a contribution to ψ (*more later*)

Output of the Theory

Predict probabilities for various things to happen

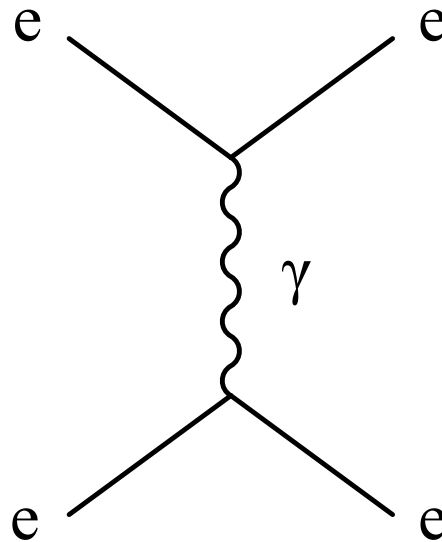
Example:



Forces from Interactions

Forces long-range manifestations of local interactions

No more action at a distance!

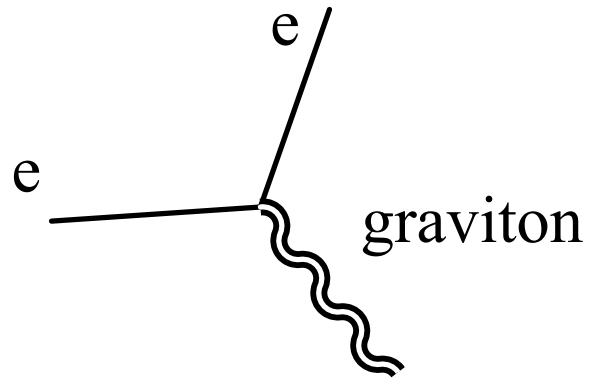


Electromagnetic force between two electrons result exchange of a photon

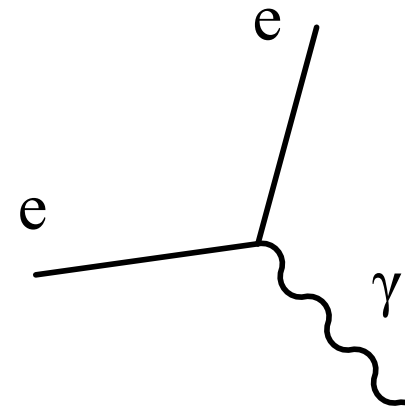
Exchange as local interactions two e- γ interactions

Forces from Interactions

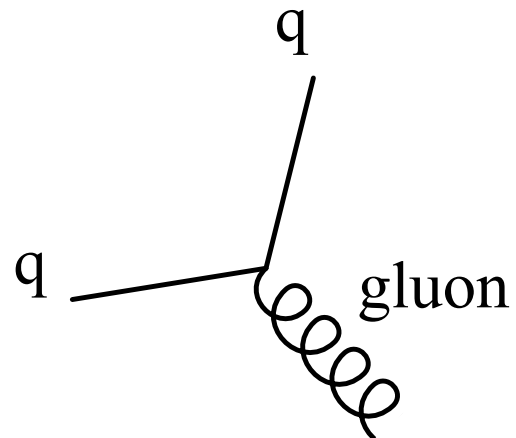
Gravitational Interaction



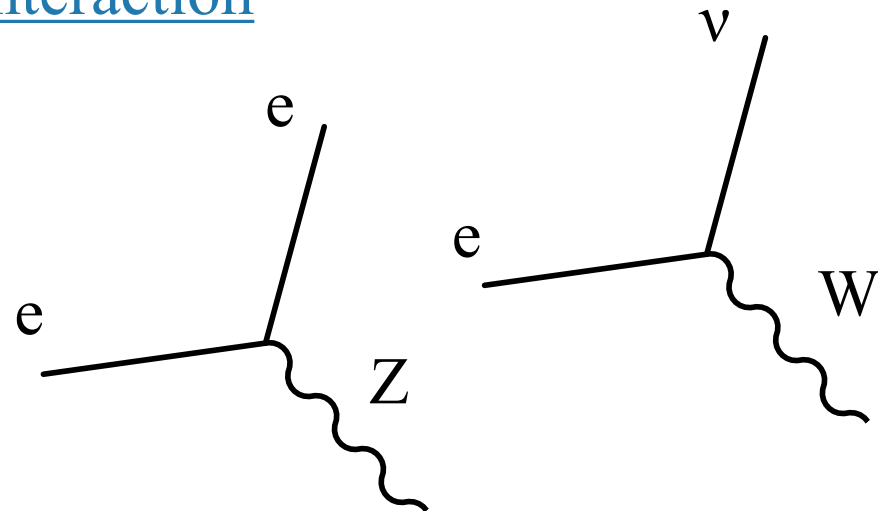
Electromagnetic Interaction



Strong Interaction

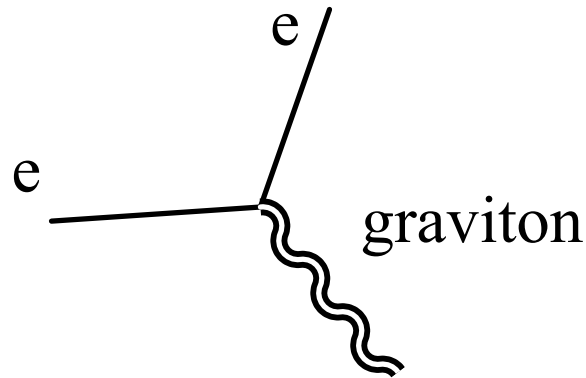


Weak Interaction

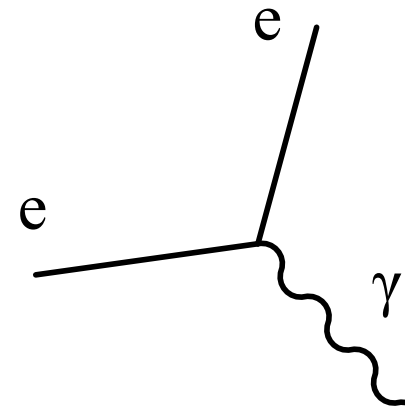


Forces from Interactions

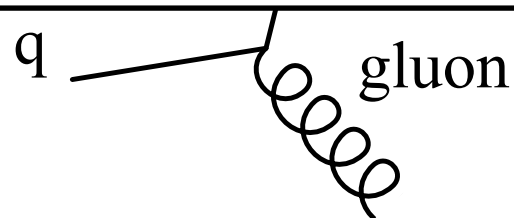
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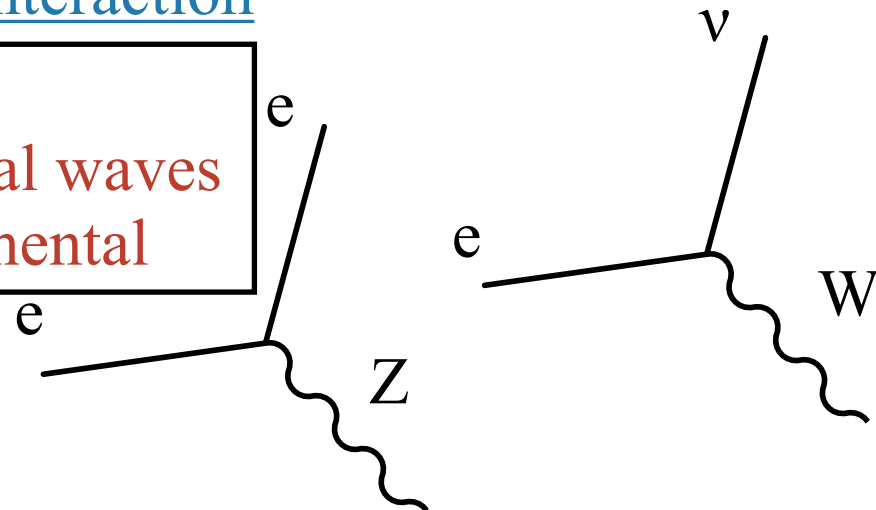
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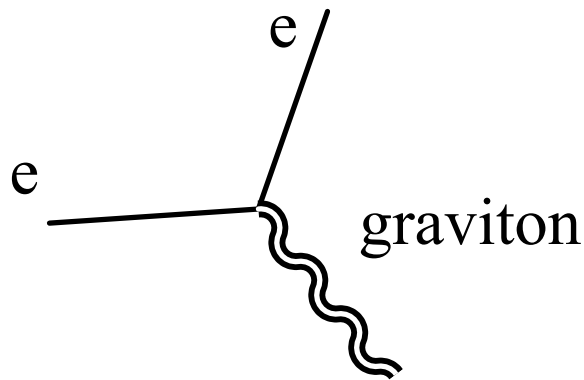
Weak Interaction



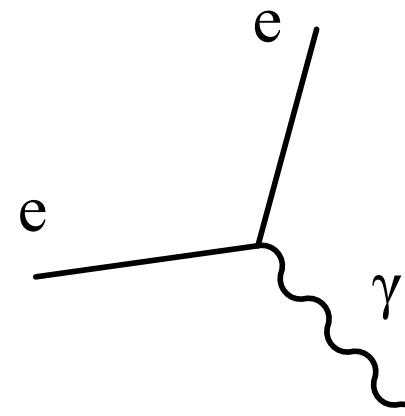
Force particles are bosons
Large collections behave like classical waves
Force particles believed to be fundamental

Forces from Interactions

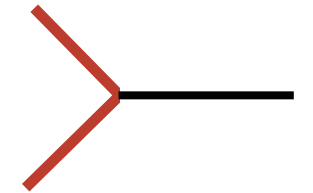
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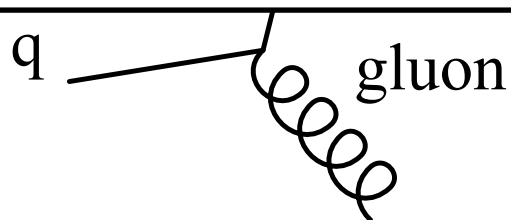
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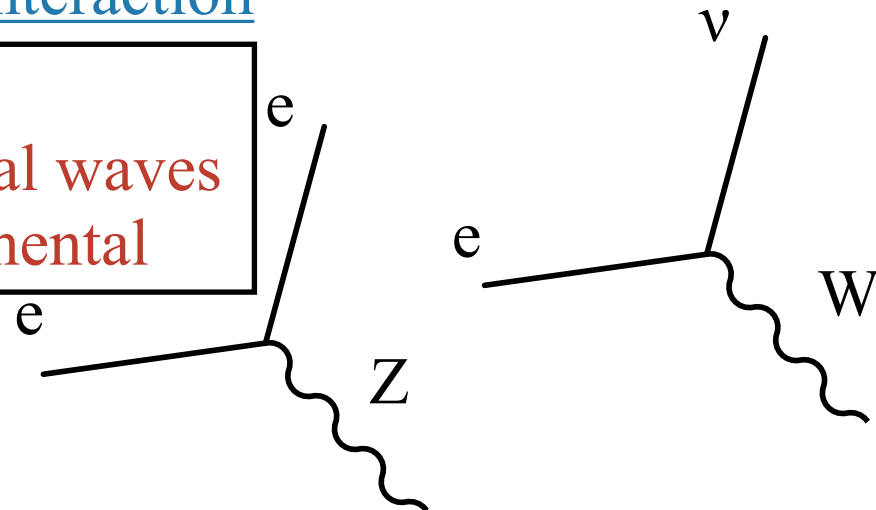
bosons
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Strong Interaction



Weak Interaction

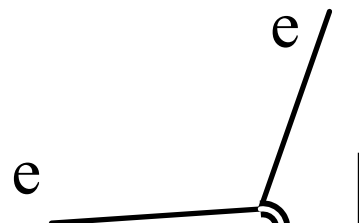


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Forces from Interactions

Gravitational Interaction

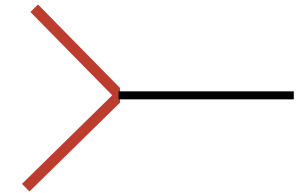
Electromagnetic Interaction



Neutrino (fermion)

- Needed describe weak interactions
- Like electron w/no charge/~no mass
- Believed to be fundamental

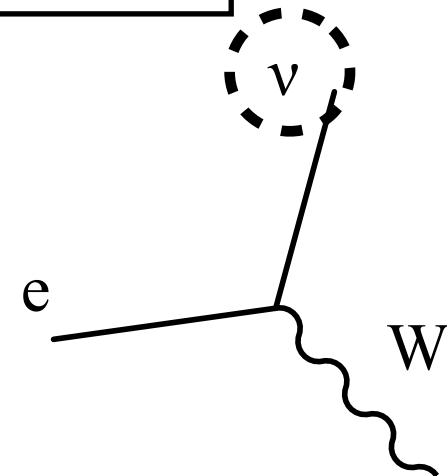
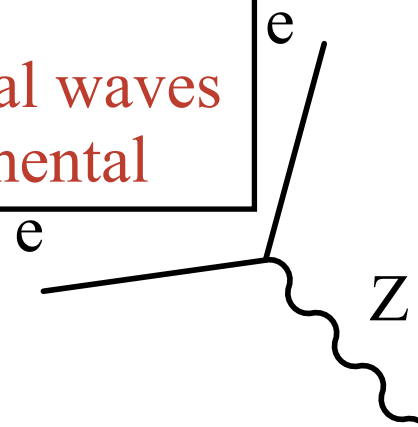
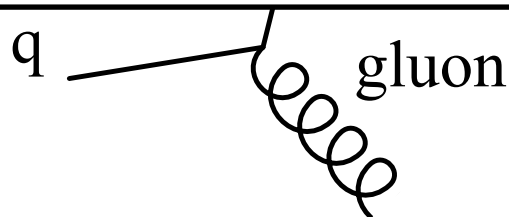
bosons
fermions



Strong Interaction

Weak Interaction

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The Standard Model

Matter Particles (Fermions)

Spin = 1/2

Leptons:

$$\begin{pmatrix} \nu_e \\ e \end{pmatrix}$$

Quarks:

$$\begin{pmatrix} u \\ d \end{pmatrix}$$

Interactions “Force carriers” (Bosons)

Spin = 1

Gauge bosons:

γ

W

Z

g

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Beautiful (complicated) mathematics governs nature interactions

Dictated by principles of symmetry (*Much direct consequence QM + R*)

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$$\begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}$$

$$\begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}$$

Quarks:

$$\begin{pmatrix} u \\ d \end{pmatrix}$$

$$\begin{pmatrix} c \\ s \end{pmatrix}$$

$$\begin{pmatrix} t \\ b \end{pmatrix}$$

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Gauge bosons:

γ

W

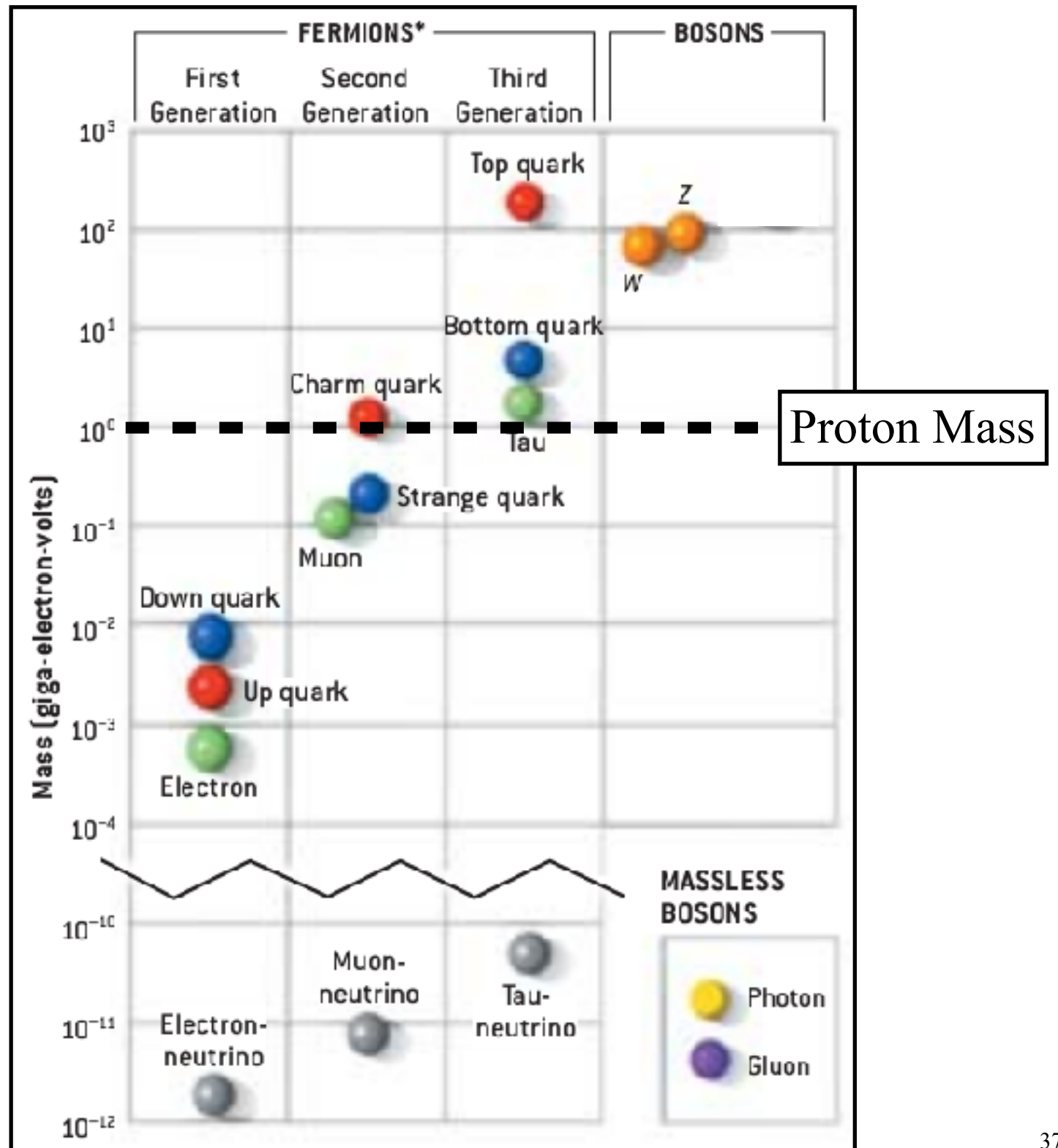
Z

g

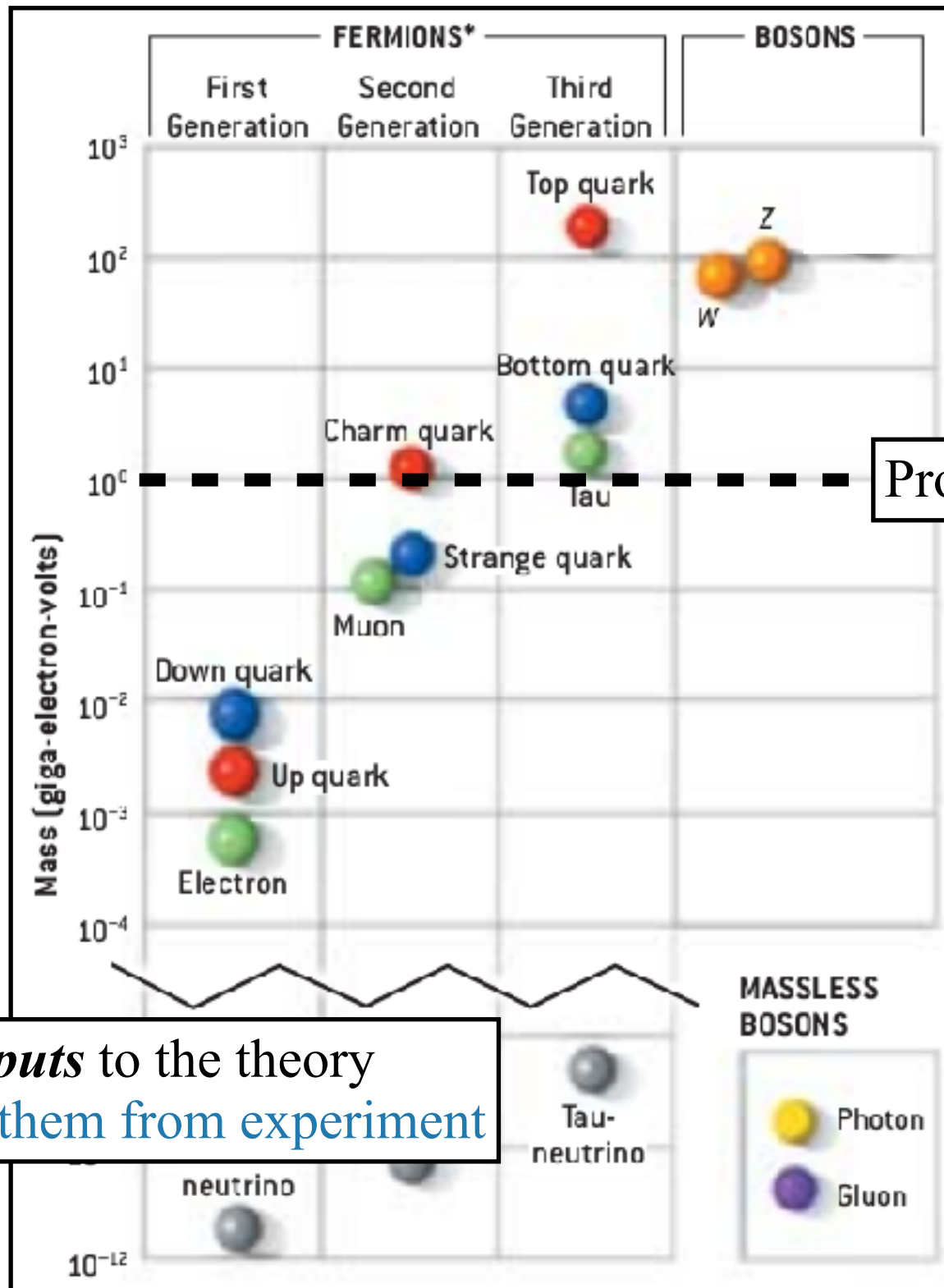
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Masses



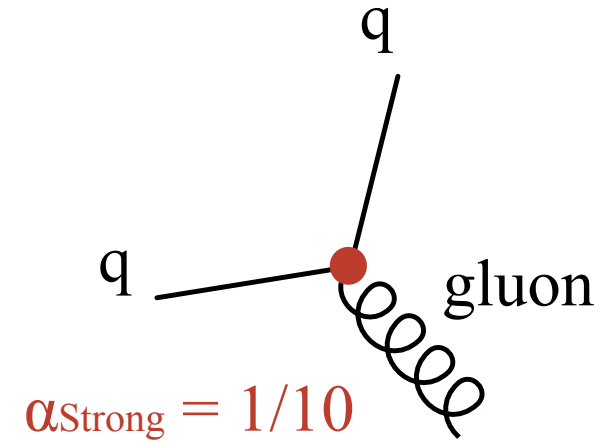
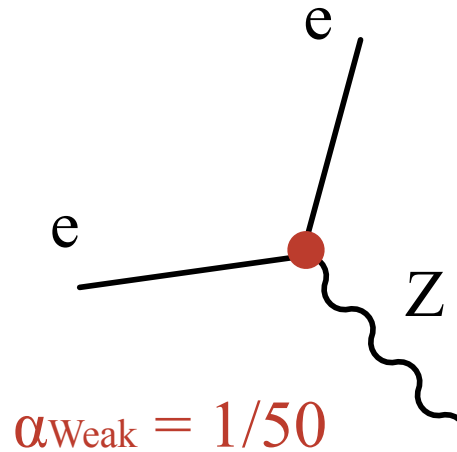
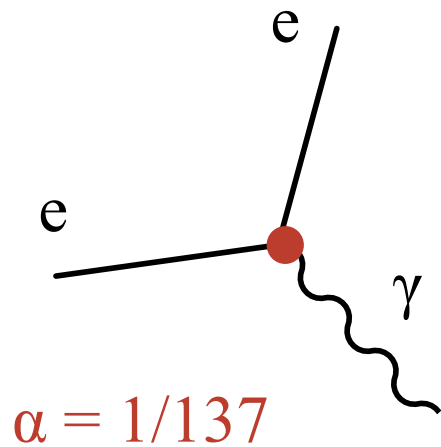
Masses



These masses are *inputs* to the theory
 Need to determine them from experiment

Interaction Strengths

Each interaction vertex characterized by number:

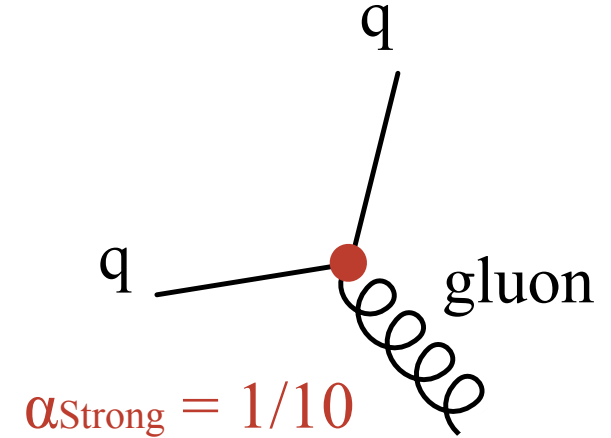
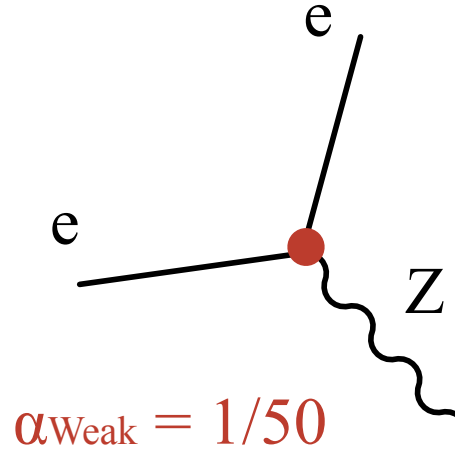
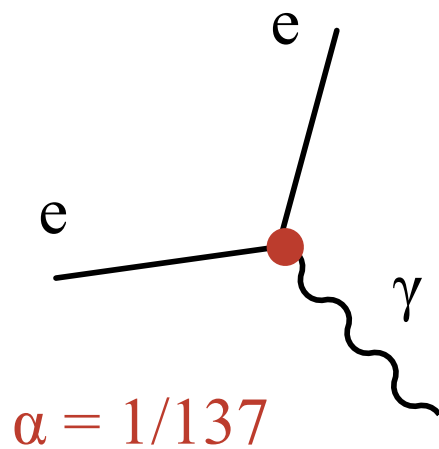


Sets the overall strength of the different interactions

- Directly related to the probability for the processes to occur

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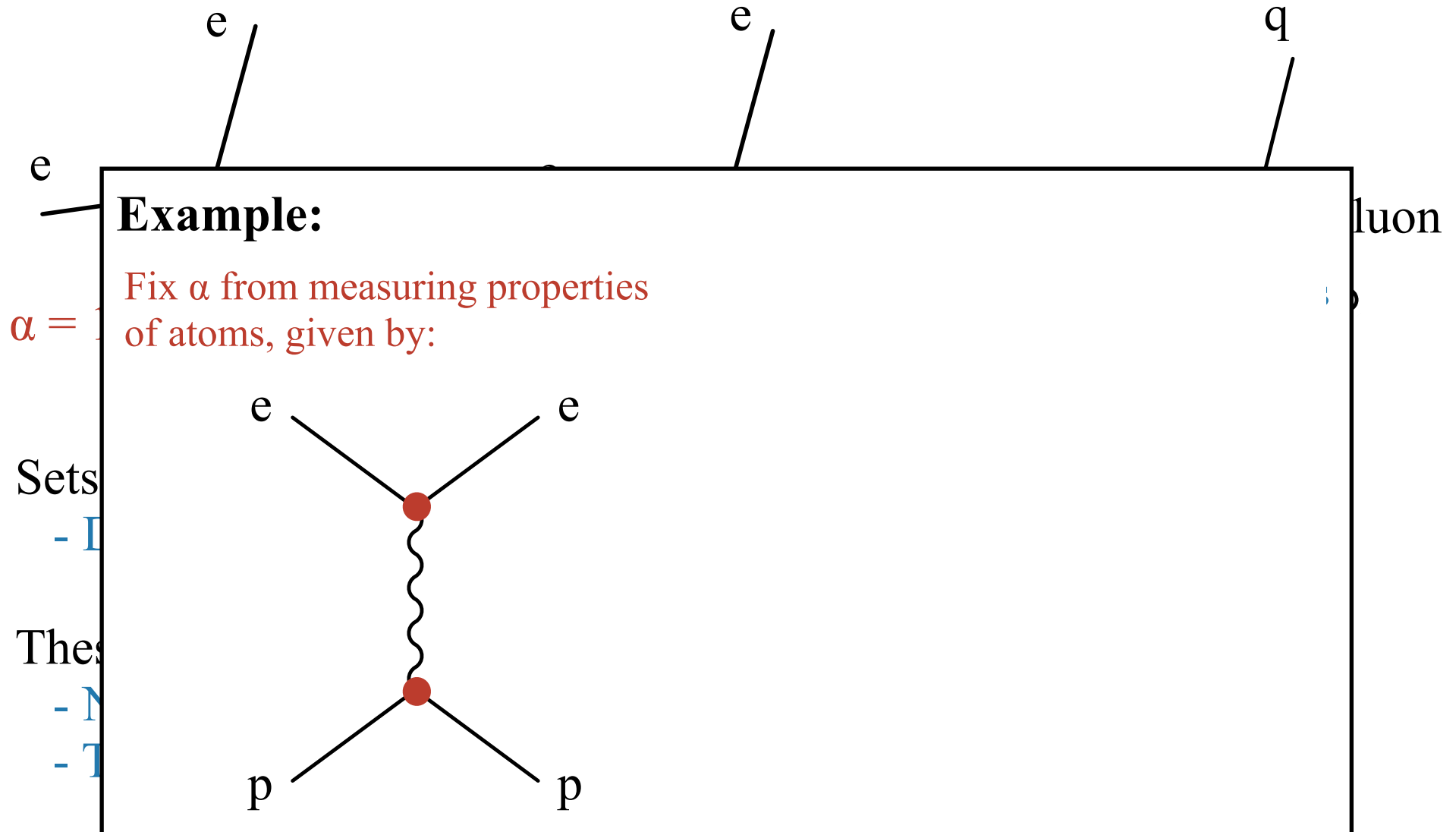
- Directly related to the probability for the processes to occur

These numbers are *inputs* to the theory

- Need to determine them from experiment
- Then use them as input in other calculations.

Interaction Strengths

Each interaction vertex characterized by number:



Interaction Strengths

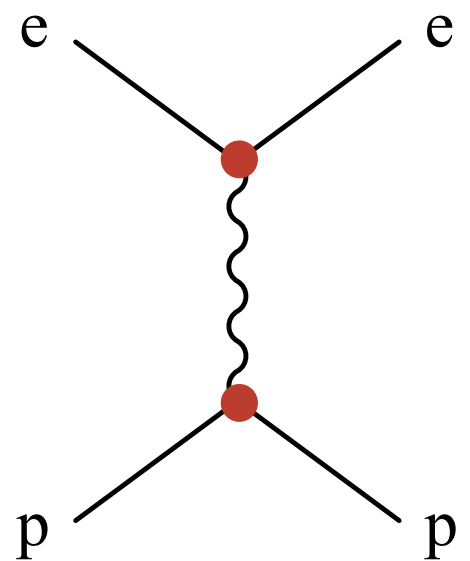
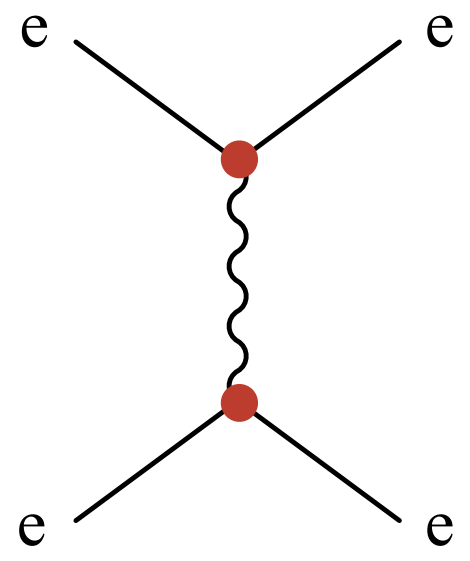
Each interaction vertex characterized by number:

e
e
q

Example:

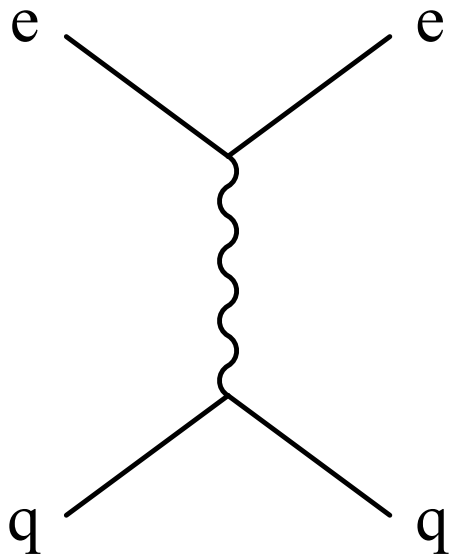
Fix α from measuring properties of atoms, given by:

Then predict all other EM probabilities (eg: how electrons (or anti-e) scatter)

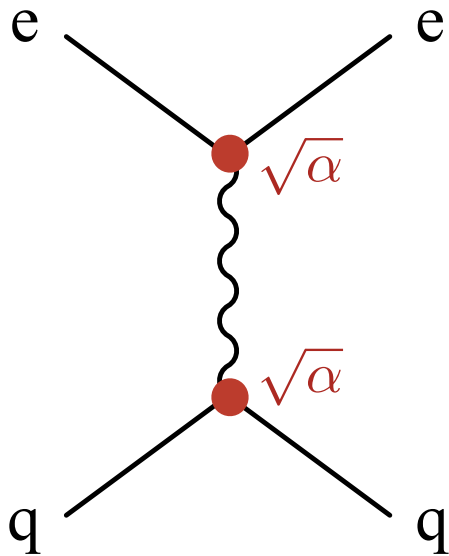
Output of the Theory (Details)

Feynman Diagrams: Pictures of what happens
Invaluable Tool for calculation



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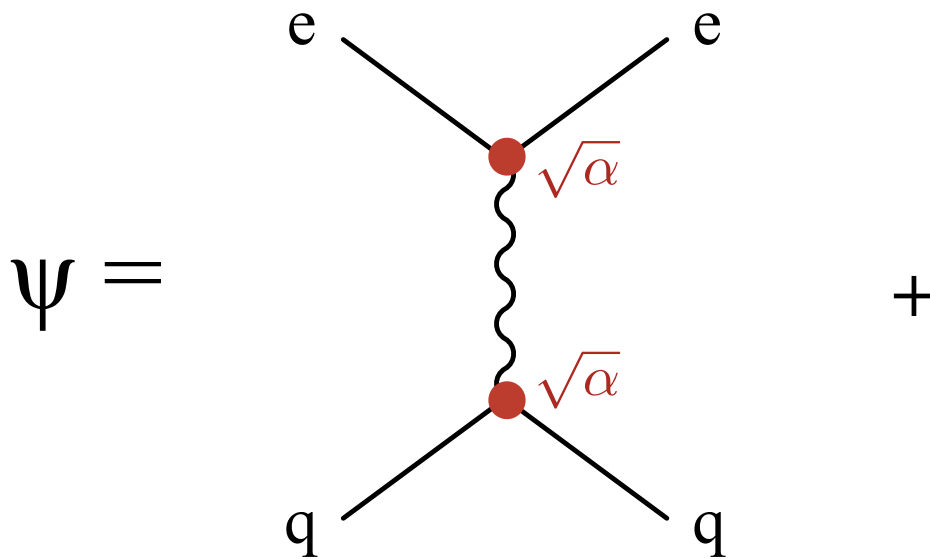
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- Theory give prescription for assigning numerical value to diagram.
Other rules associated to the lines / Sum overall possible configurations

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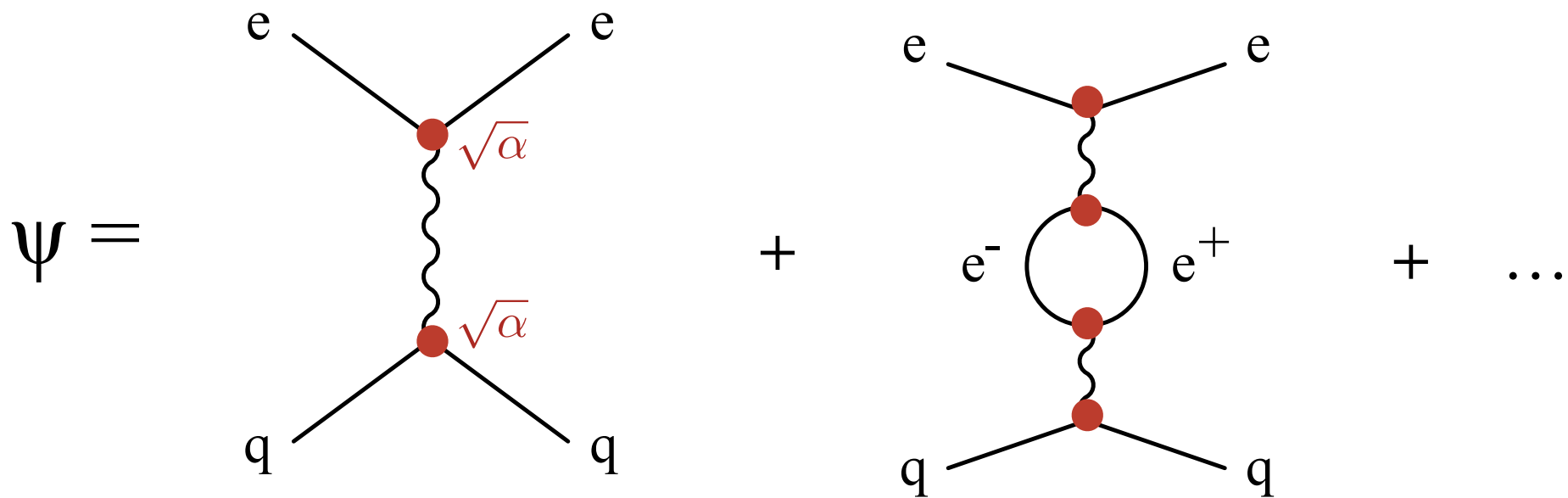
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- Theory give prescription for assigning numerical value to diagram.
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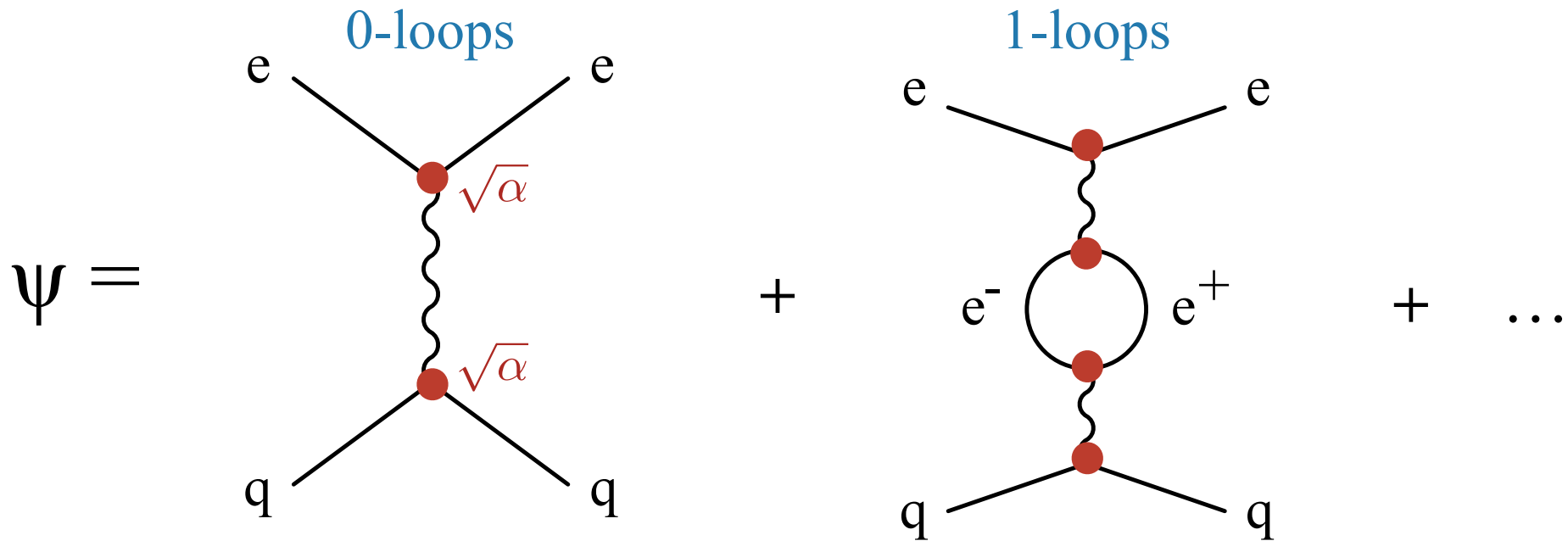
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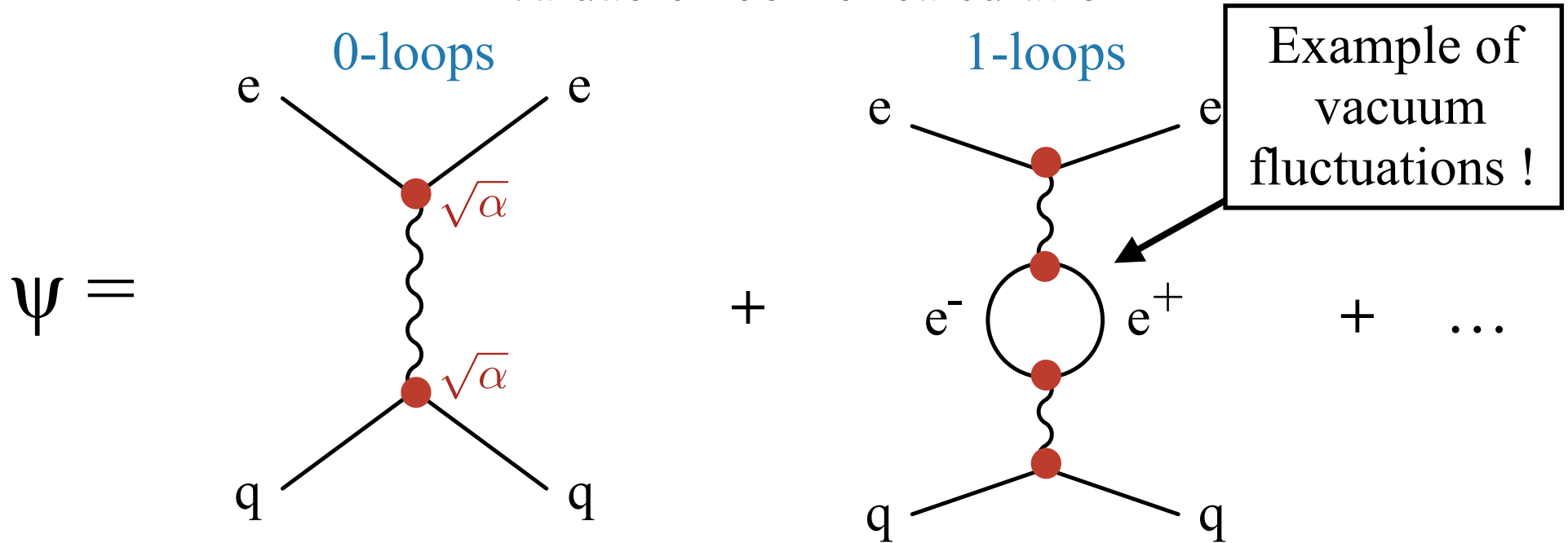
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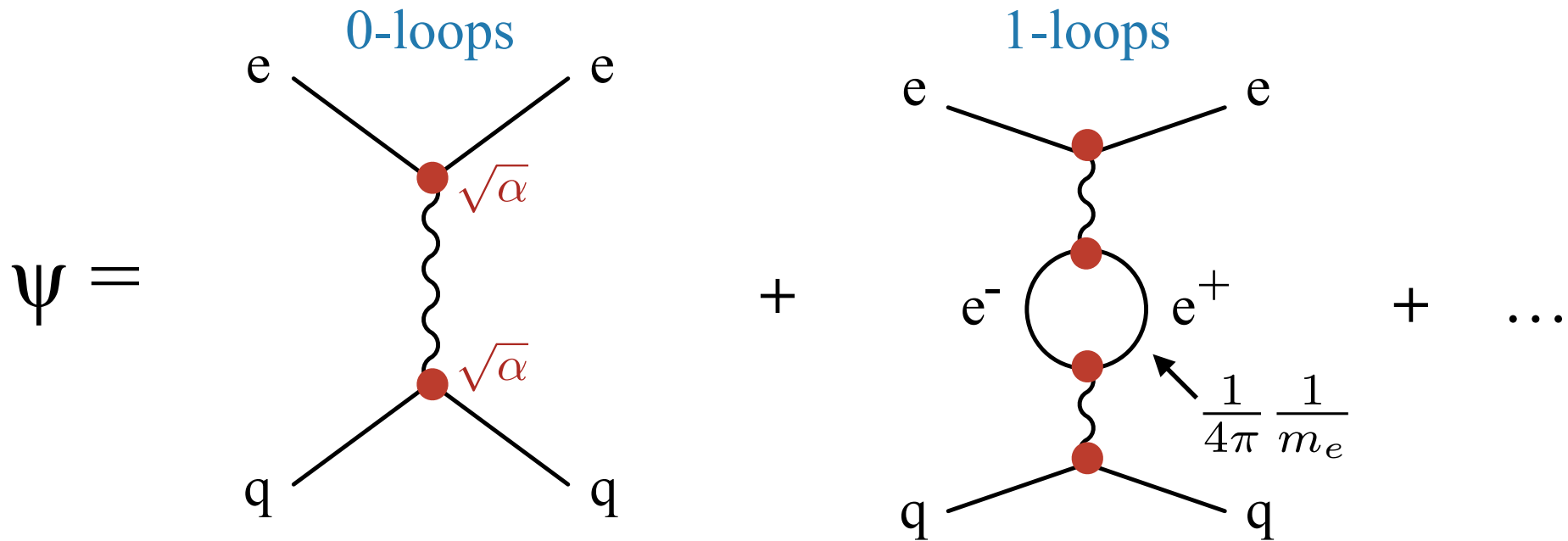
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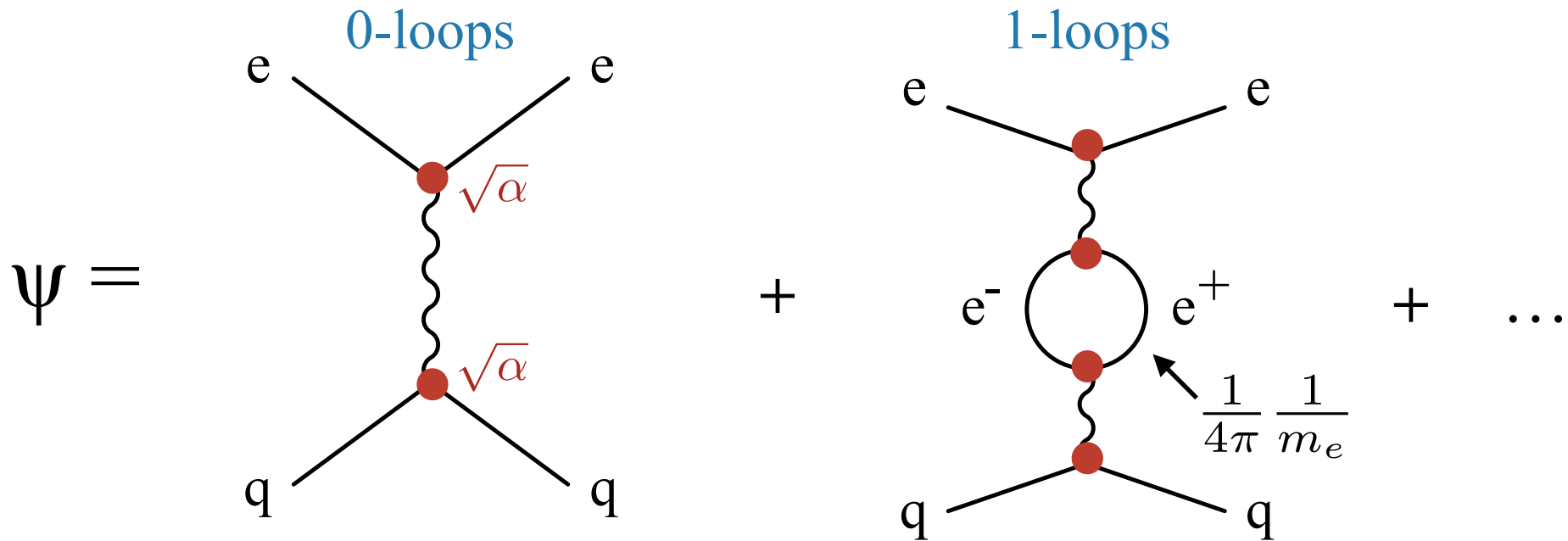
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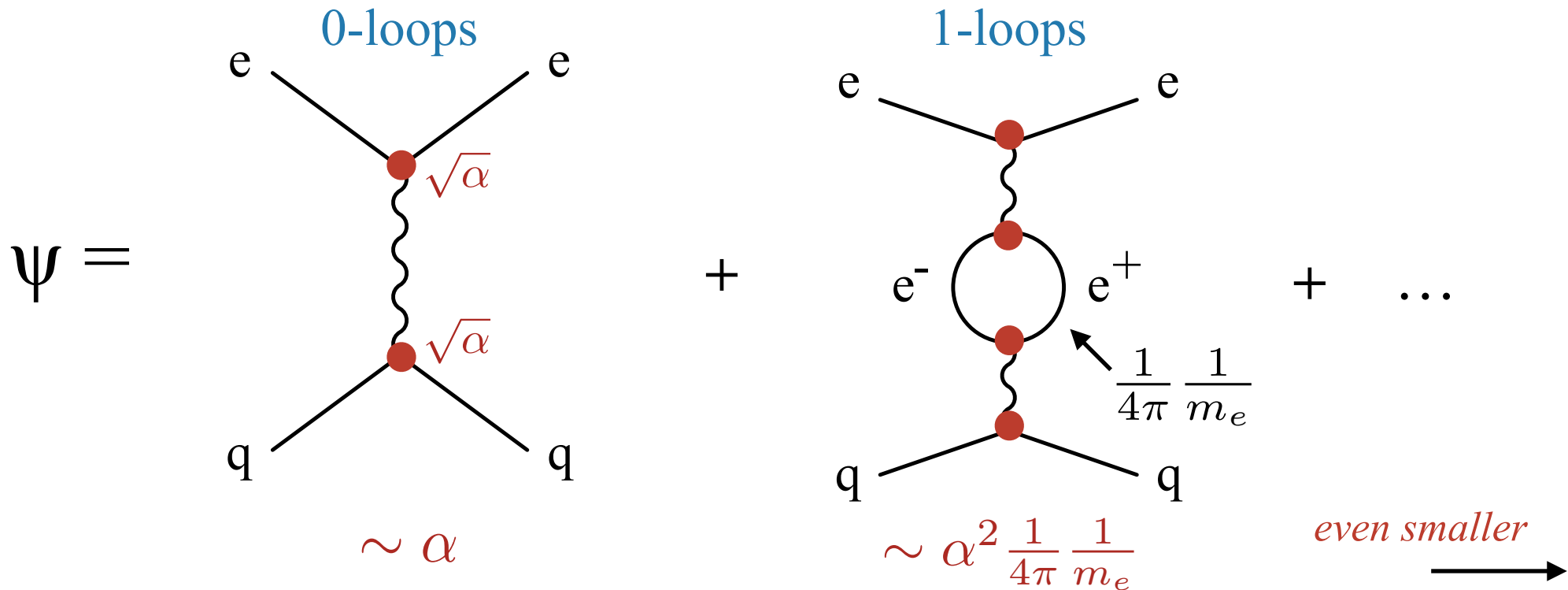
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 Other rules associated to the lines / Sum overall possible configurations
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- Really infinite sum. In practice, only the first few terms dominate

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Feynman Diagrams: Pictures of what happens
 Invaluable Tool for calculation



- Theory give prescription for assigning numerical value to diagram.
 Other rules associated to the lines / Sum overall possible configurations
- Sum of diagrams (# associated with diagrams) is ψ
- Really infinite sum. In practice, only the first few terms dominate

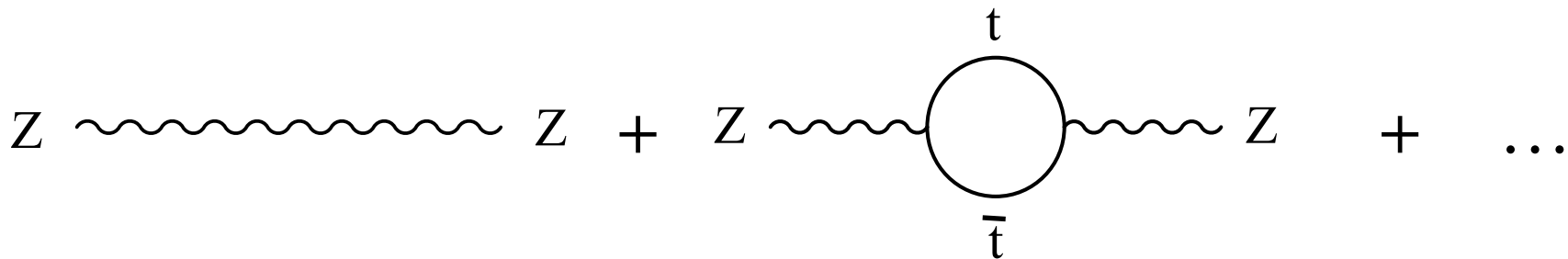
Output of the Theory (Details)

Just saw example of calculating interaction between particles
Can also calculate basic properties of particles

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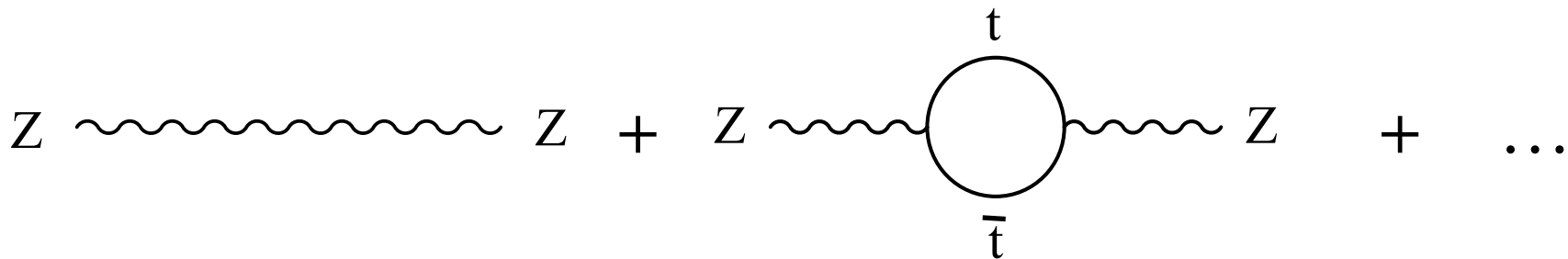
Example: *Contribution to mass Z boson*



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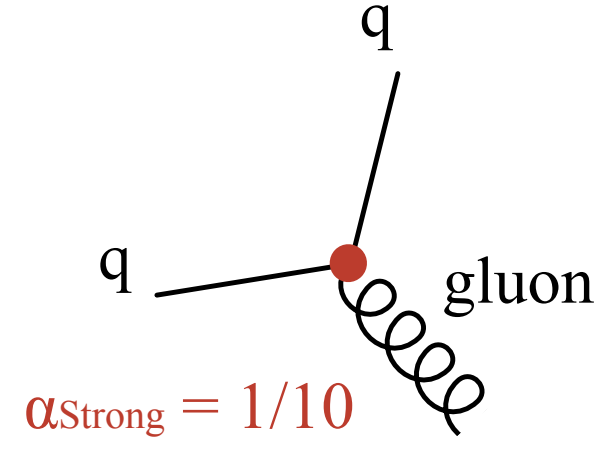
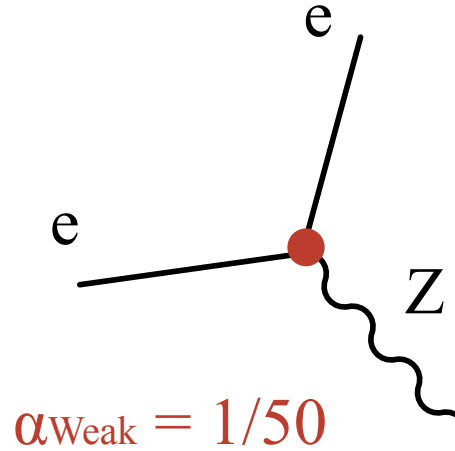
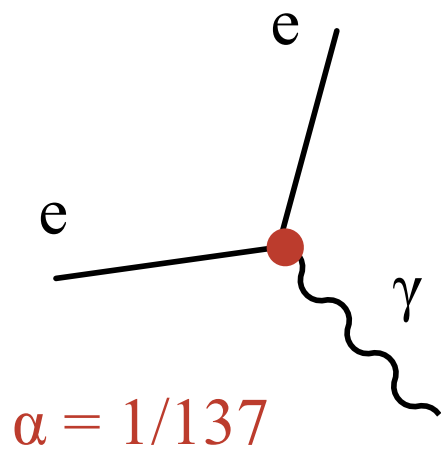
Example: *Contribution to mass Z boson*



- Seems impossible given $m_{top} > m_Z$
- Allowed by Quantum theory (Uncertainty principle $\Delta E \Delta t \geq \hbar$)
- “Quantum Corrections” to mass
- Confirmed observable consequences

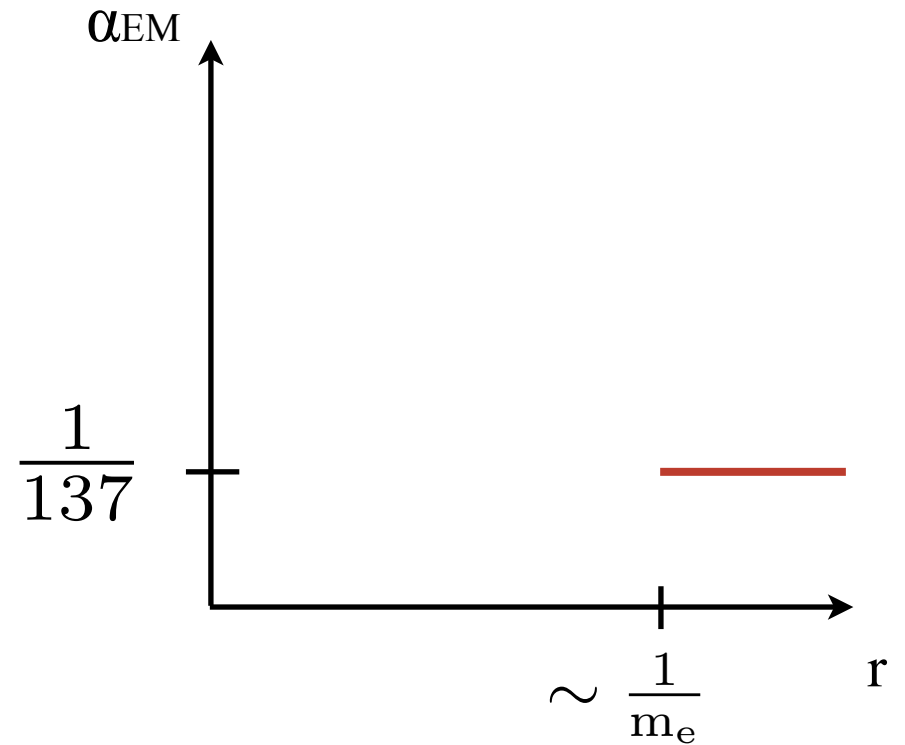
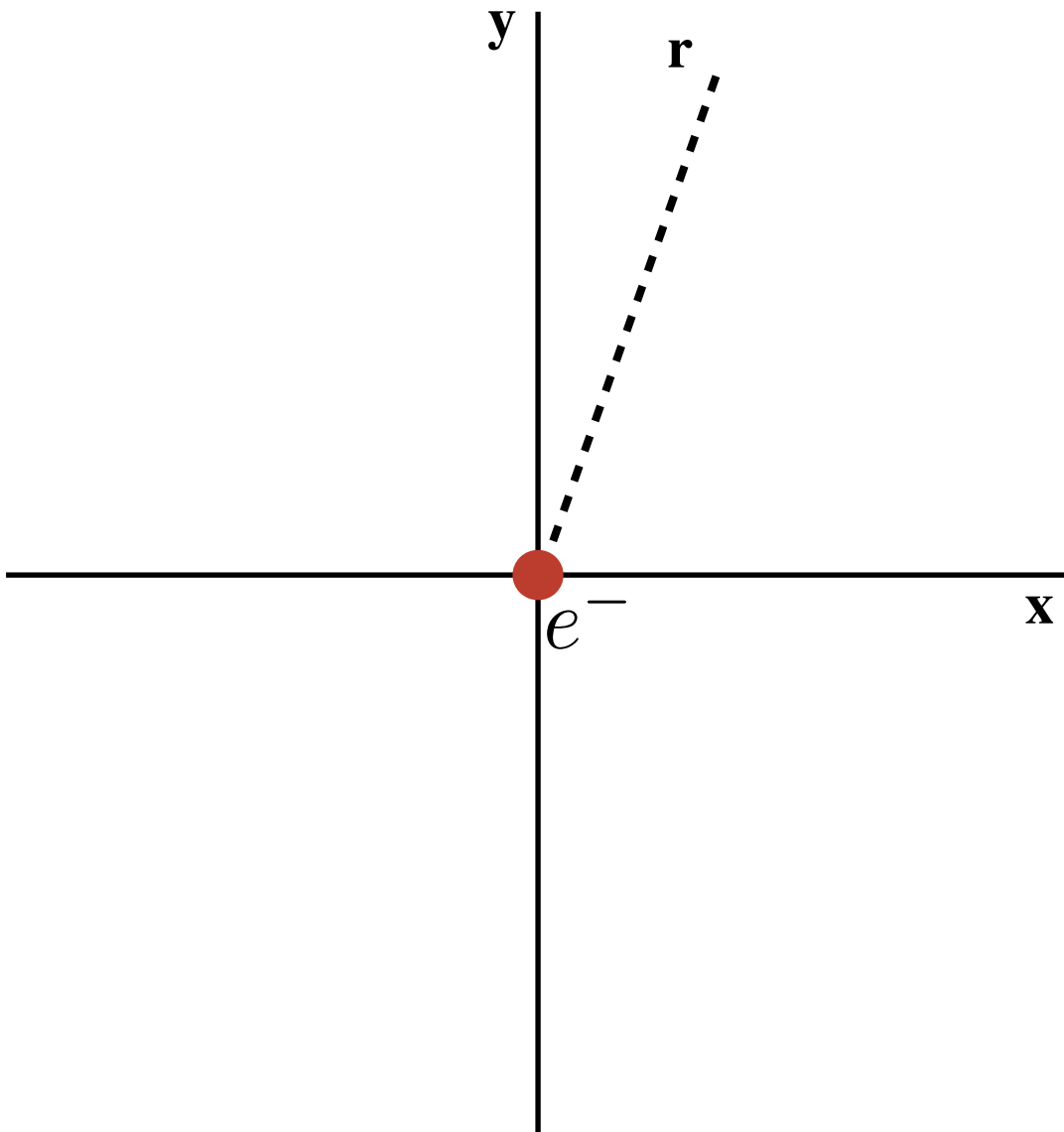
Forces Common Language

First time that we see that all forces described in same basic way.

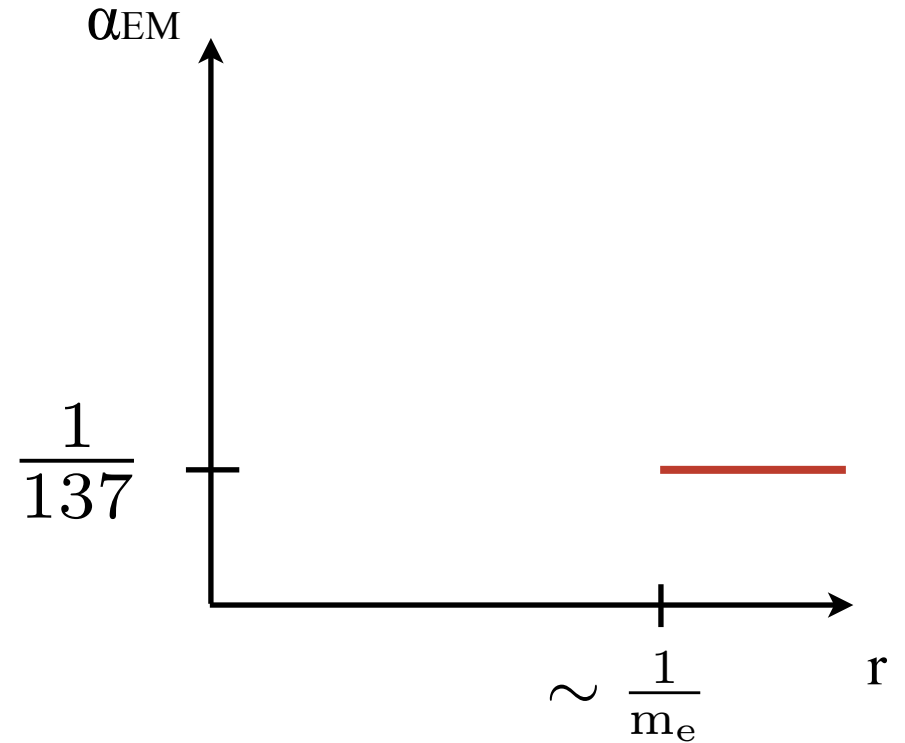
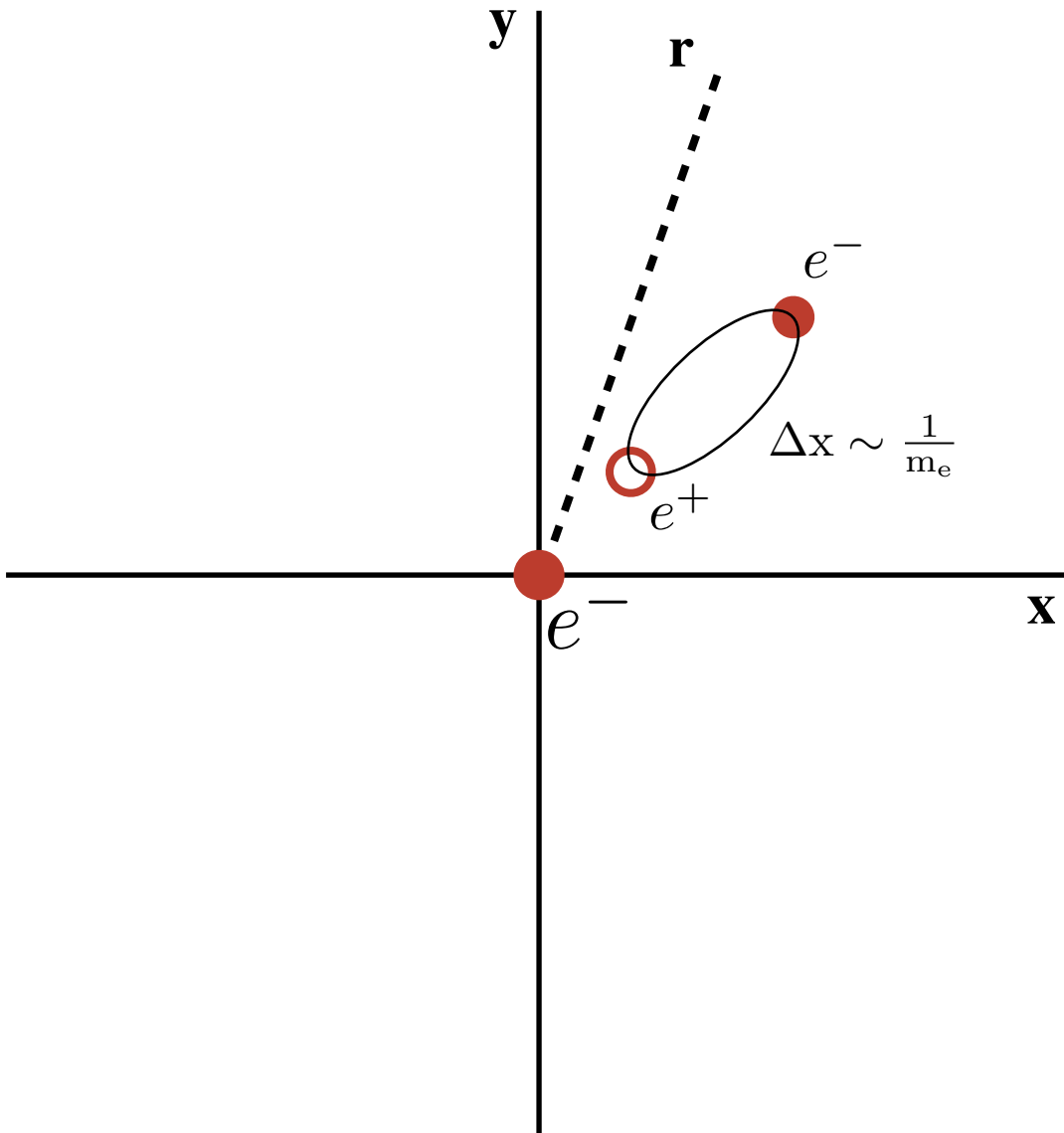


Forces look very different to us...

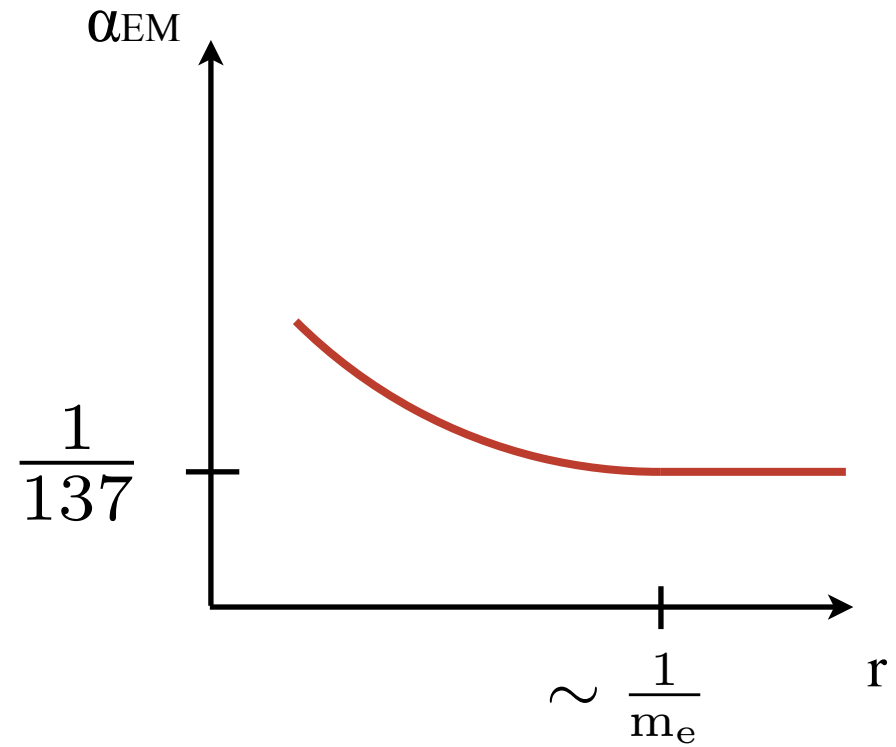
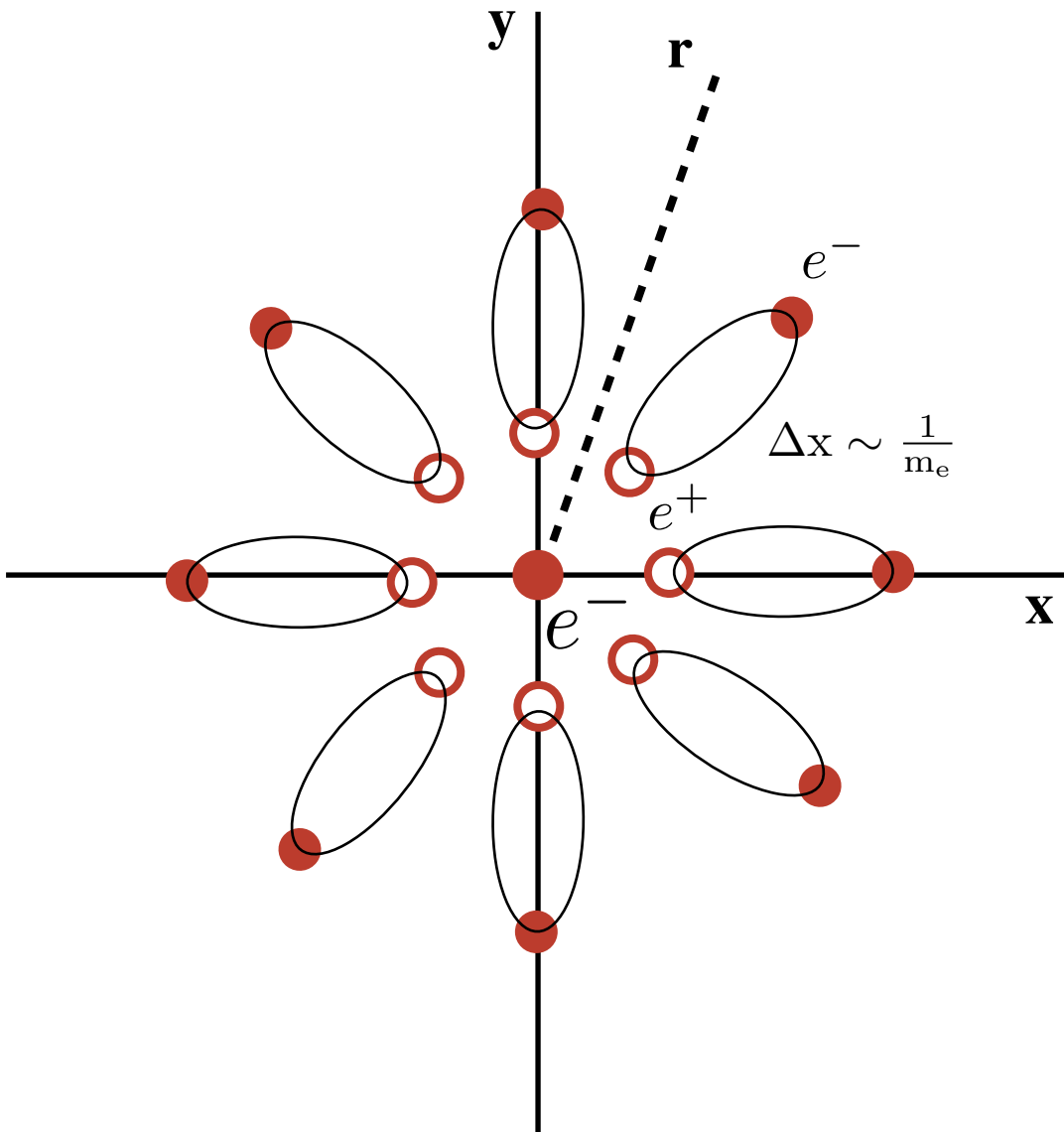
EM Strength w/Distance



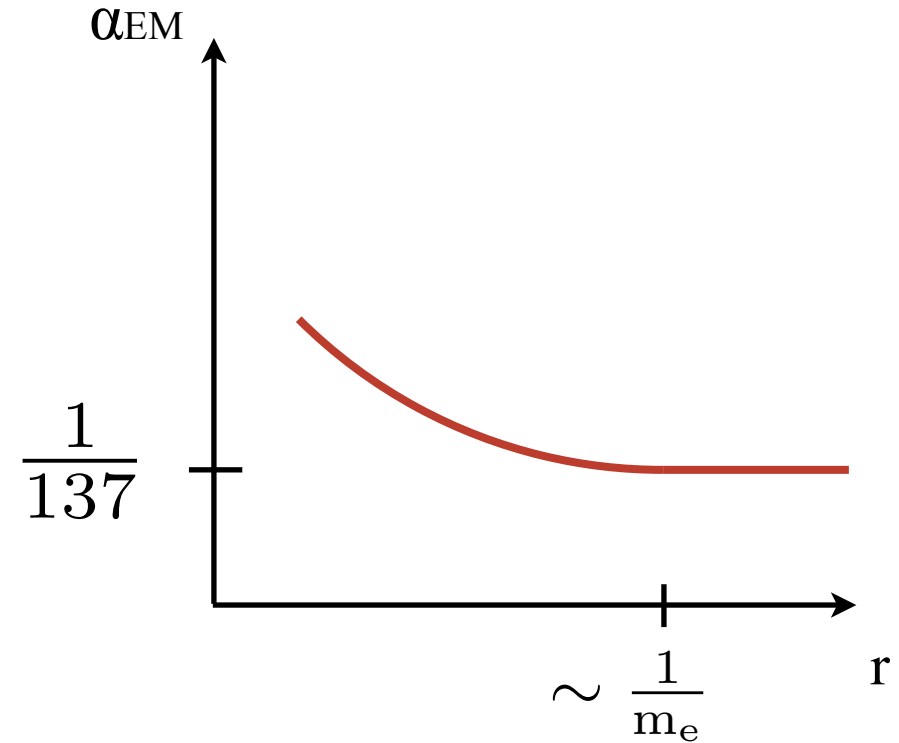
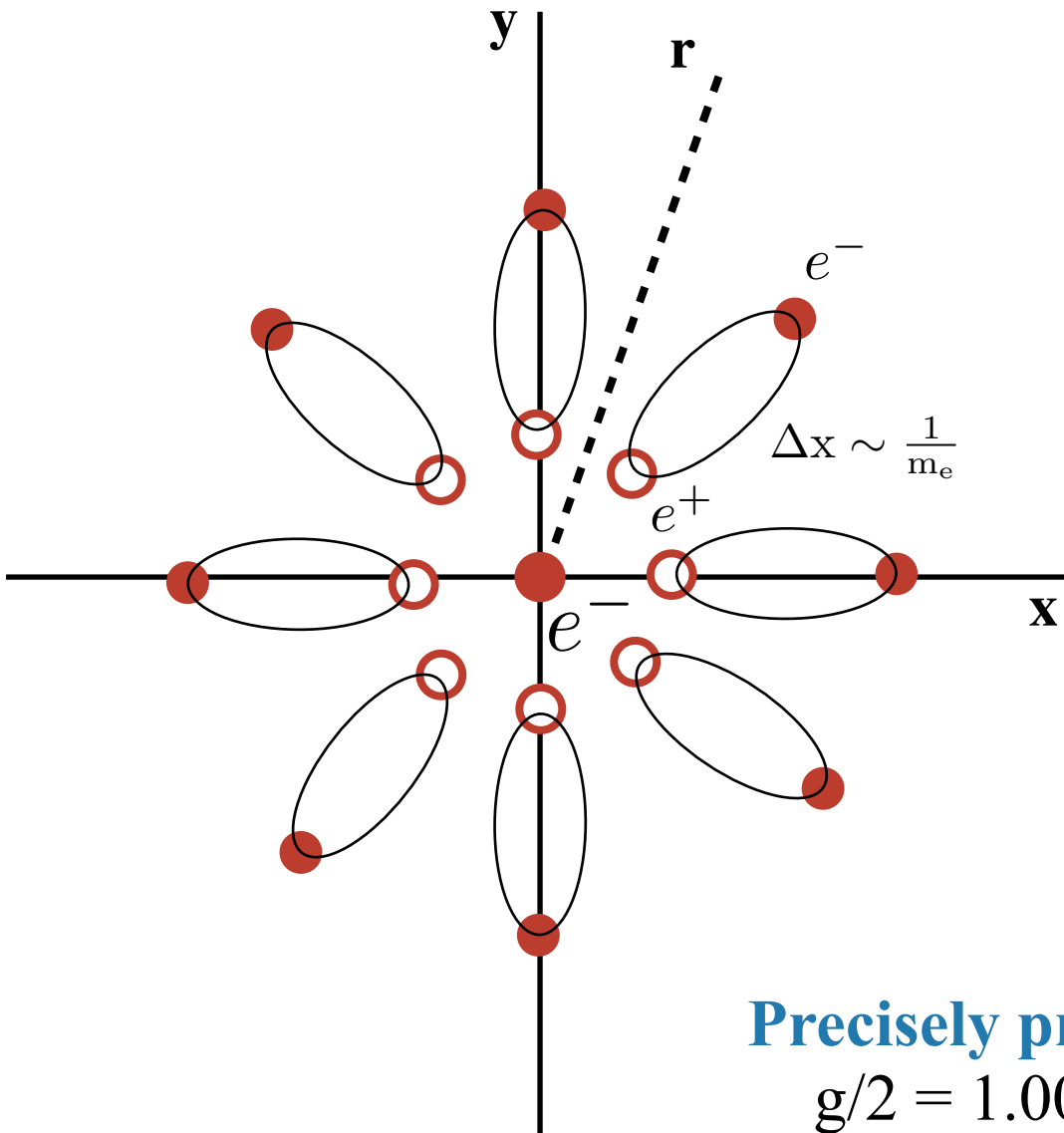
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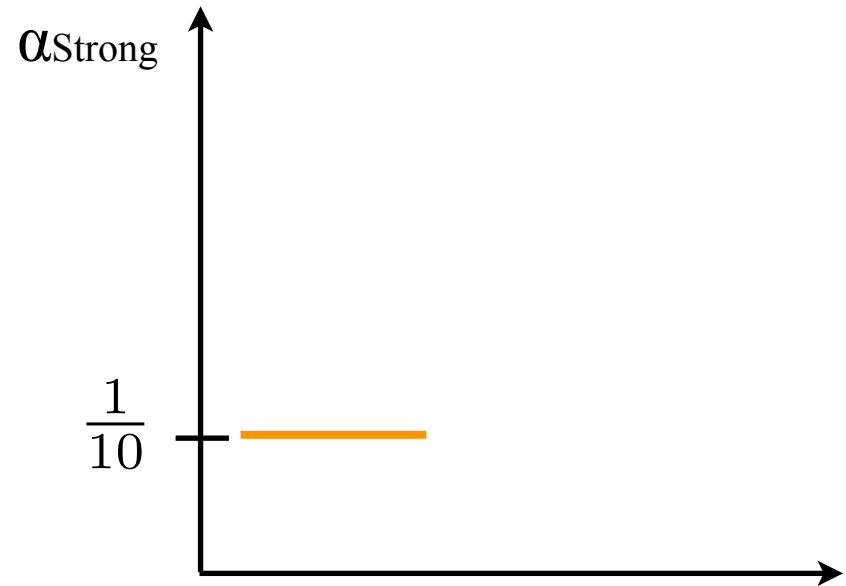
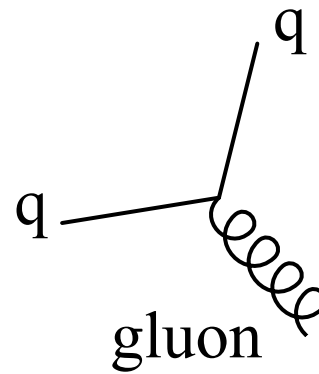
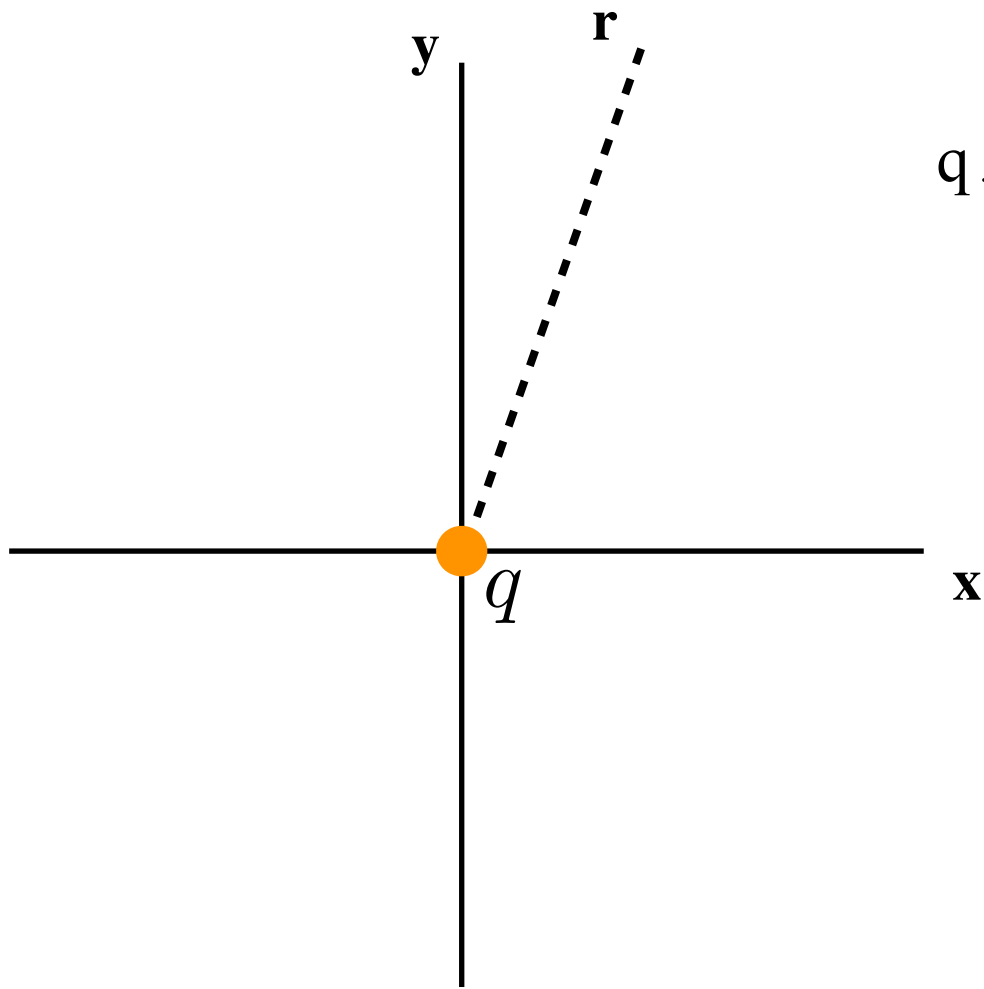


Precisely predict magnetic properties

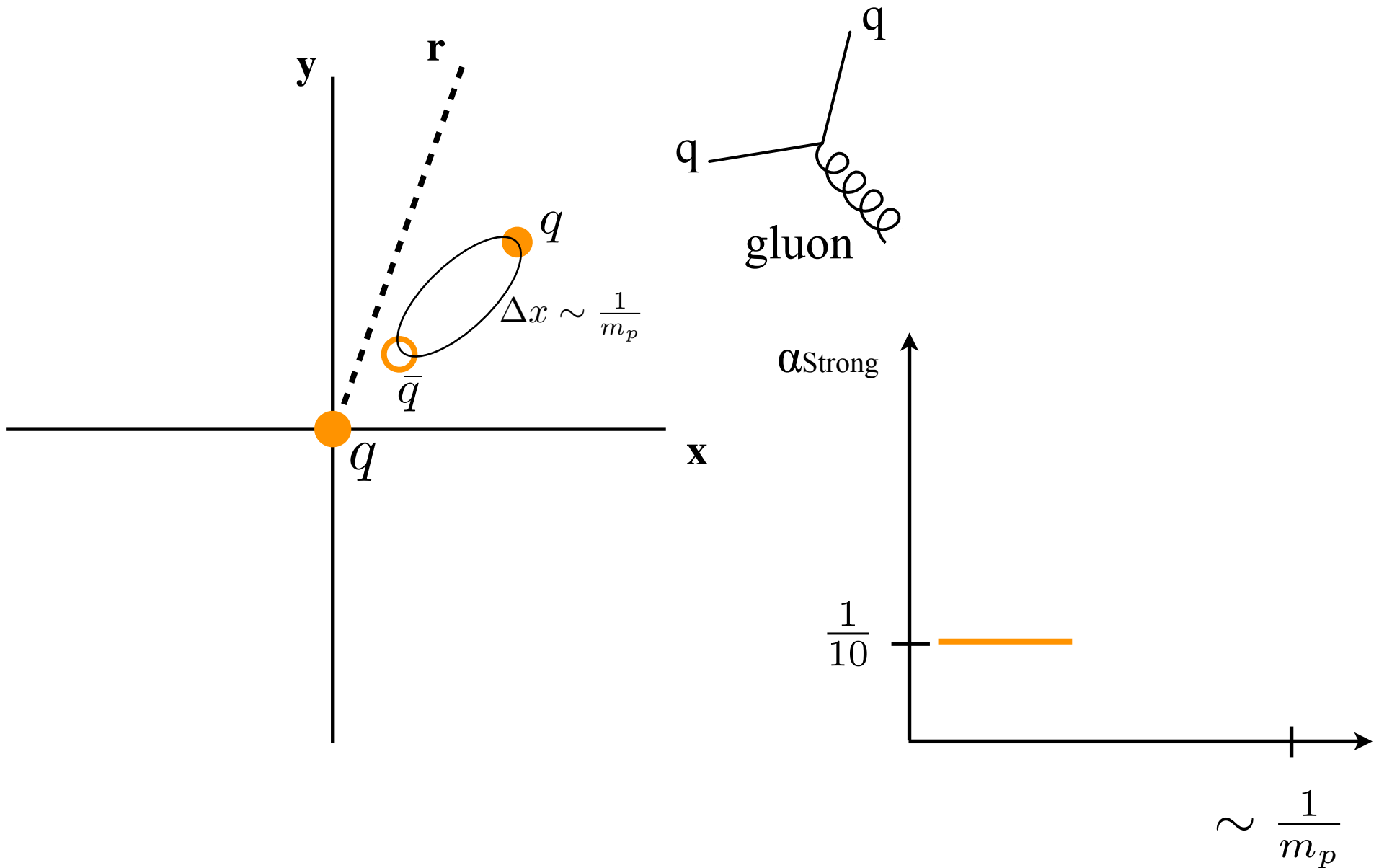
$$g/2 = 1.0011596521809(8),$$

(Agree to better than one part in a trillion.)

Strong Interaction w/Distance

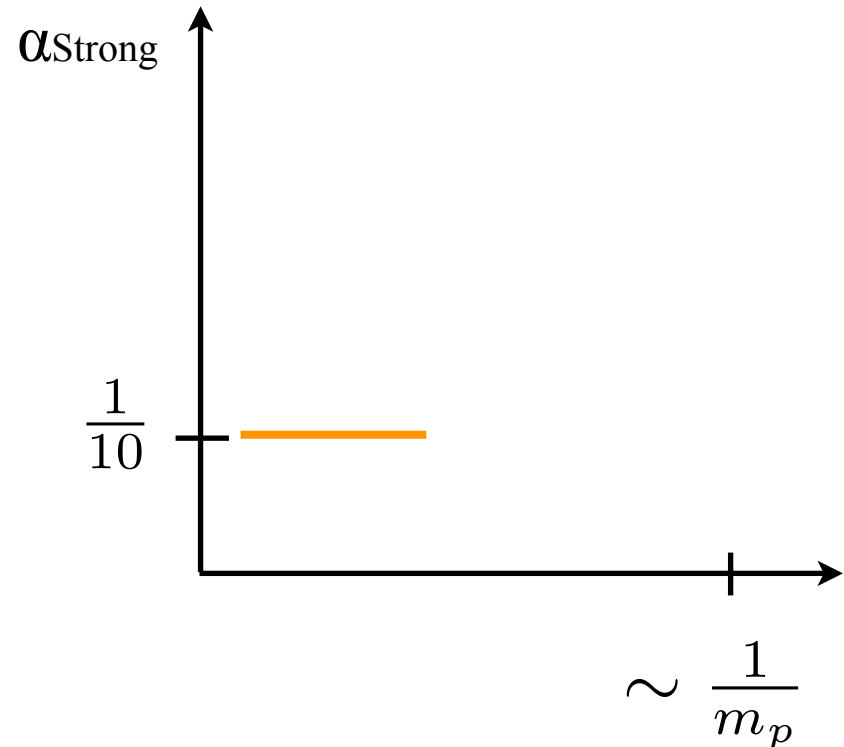
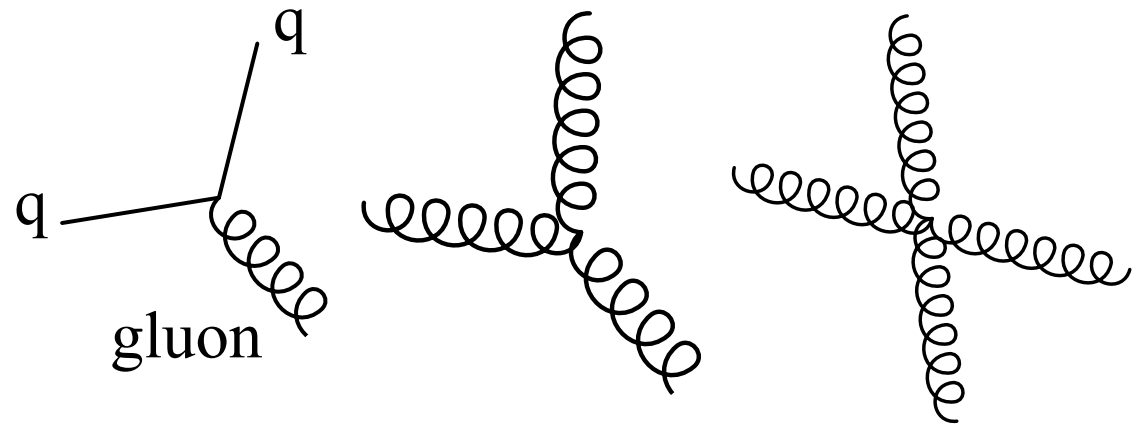
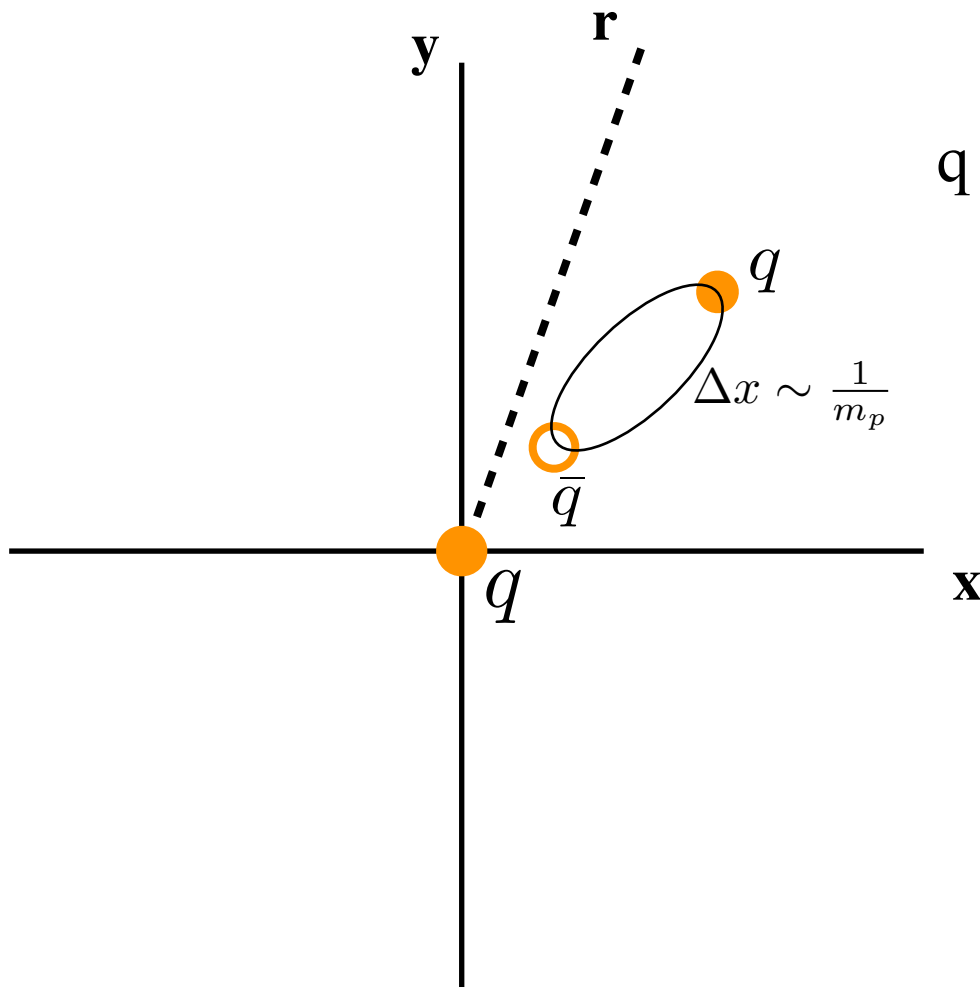


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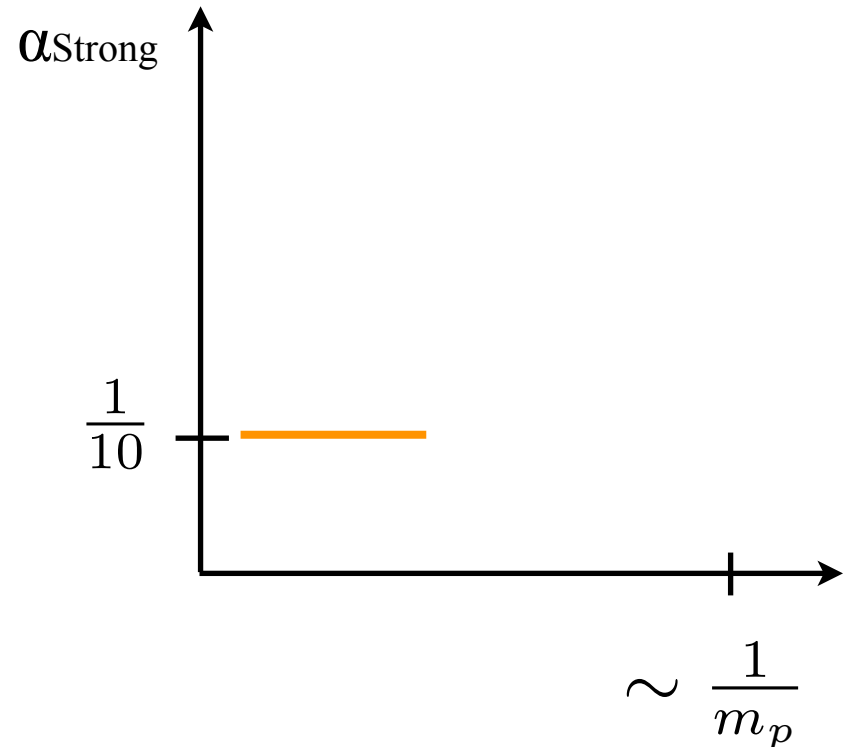
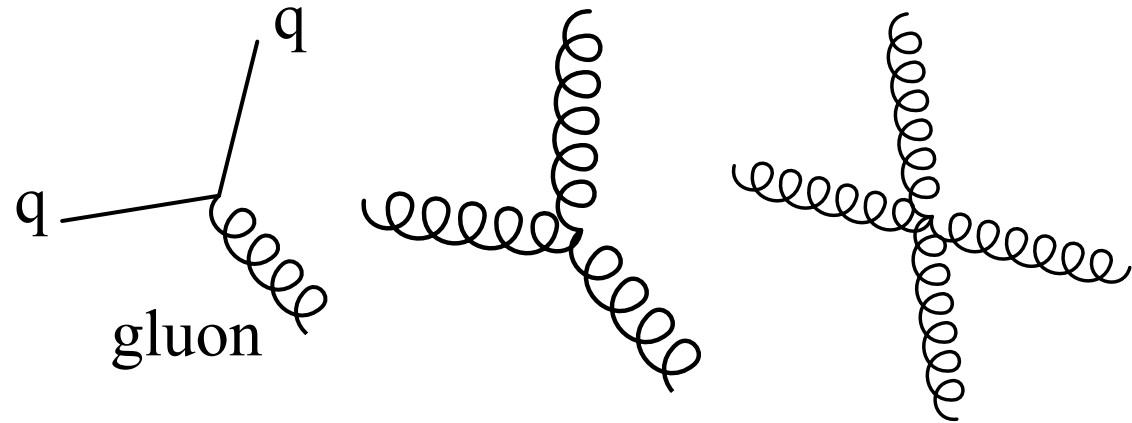
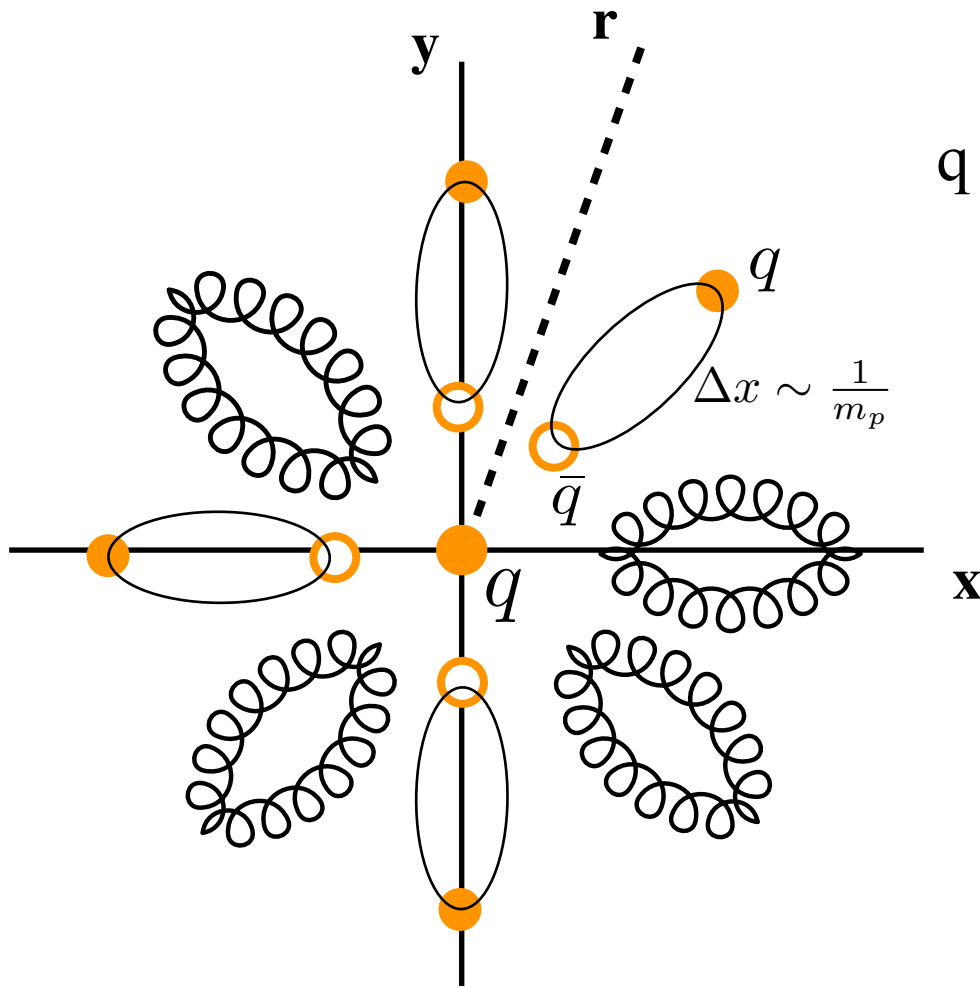
Strong Interaction w/Distance

Unlike photons, gluons can self interact.



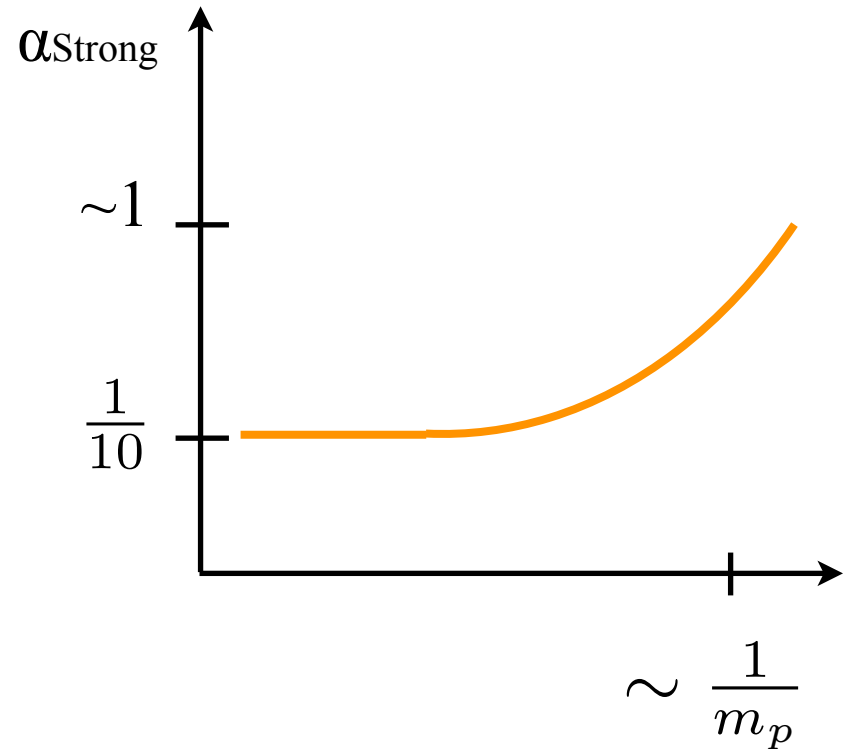
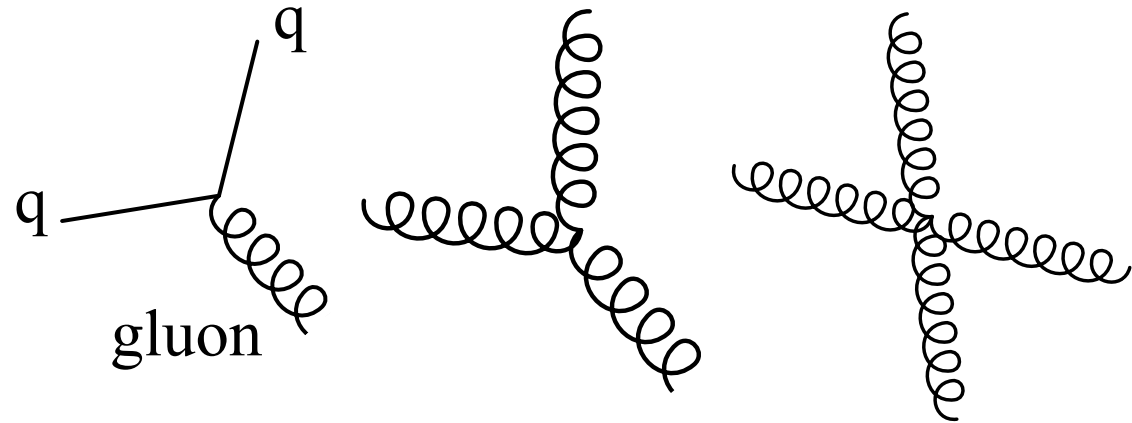
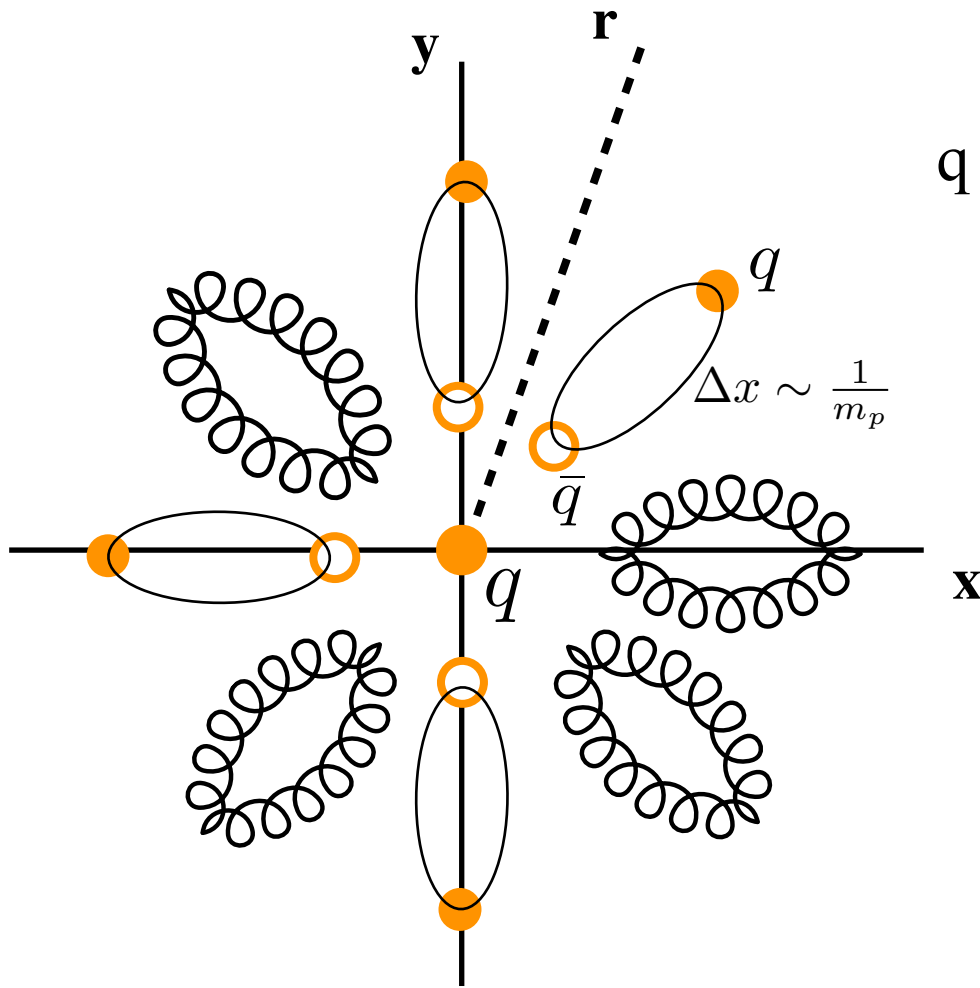
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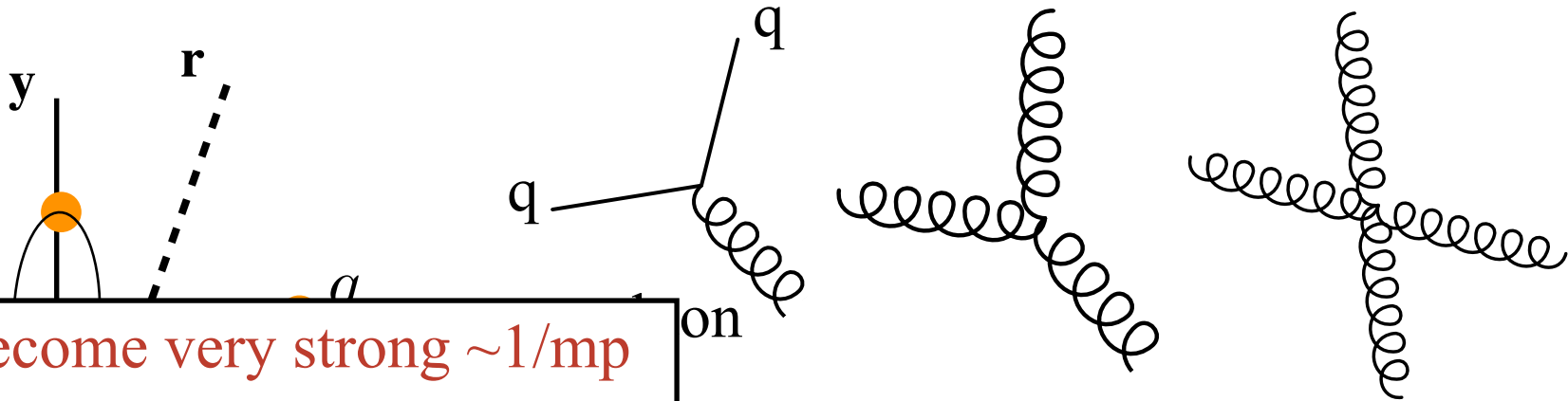
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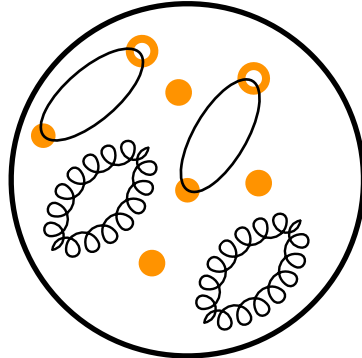
Strong Interaction w/Distance

Unlike photons, gluons can self interact.



Interaction become very strong $\sim 1/m_p$

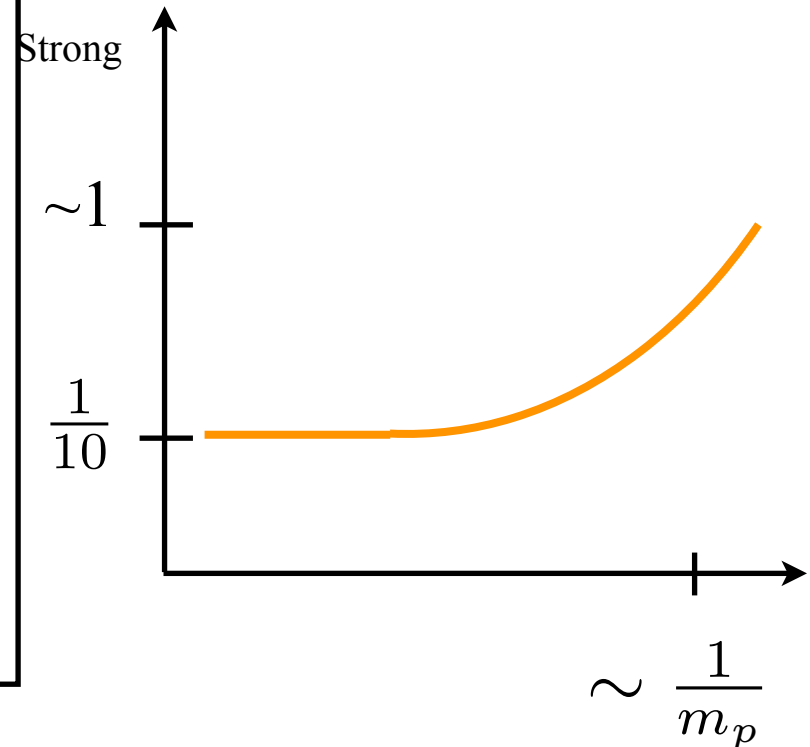
Proton:



B/c force grows with distance:

- Cant pull them out of the proton
- q and gluons “confined”

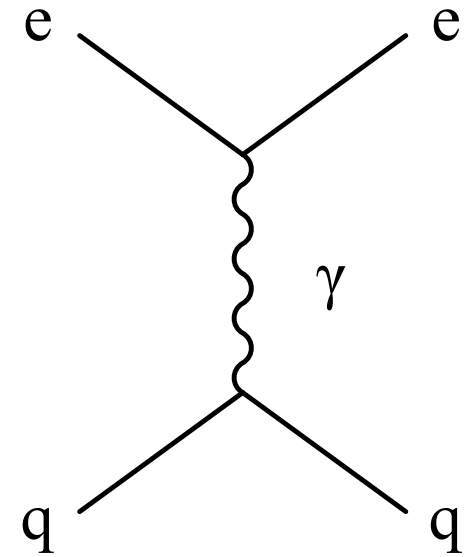
Sets the size of protons (neutrons)



Back to EM Interaction

Electron high probability to emit γ when:

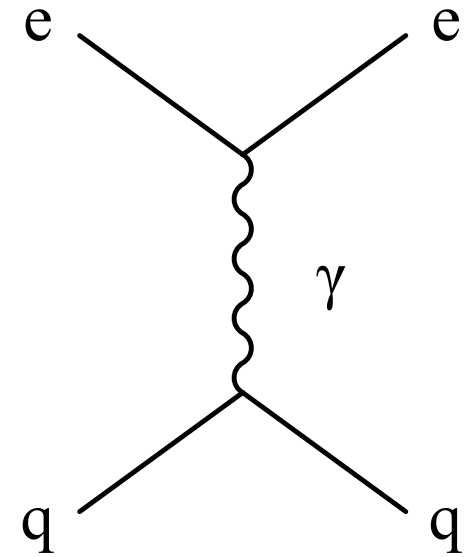
Electro-magnetic Force



Back to EM Interaction

Electron high probability to emit γ when:
 $E \times r < h/c$ (*consistent with $\Delta E \Delta t > h$*)

Electro-magnetic Force



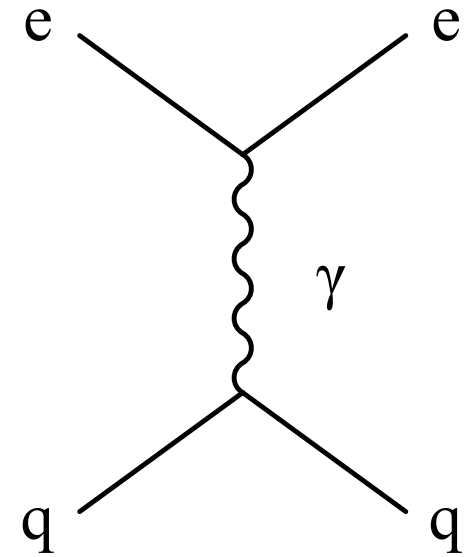
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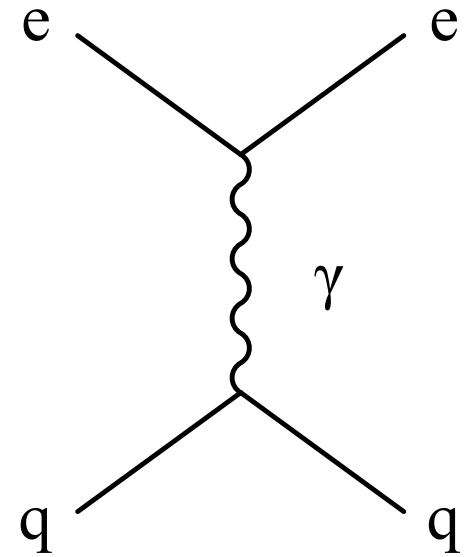
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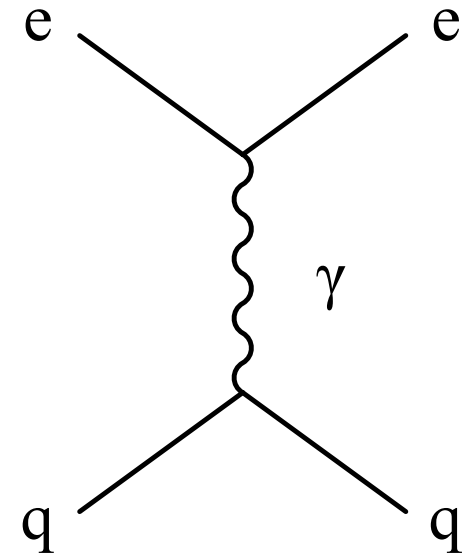
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when $p \rightarrow 0$ then $r \rightarrow \infty$

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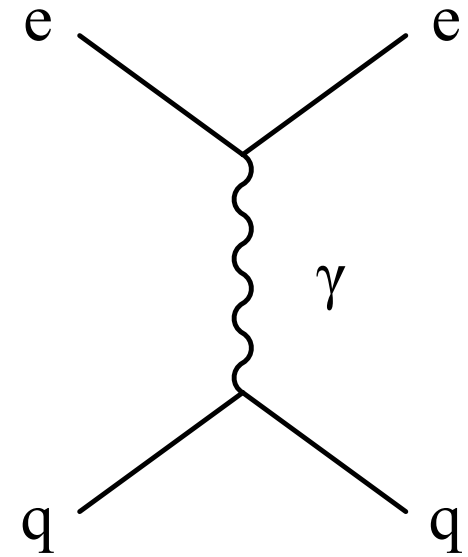
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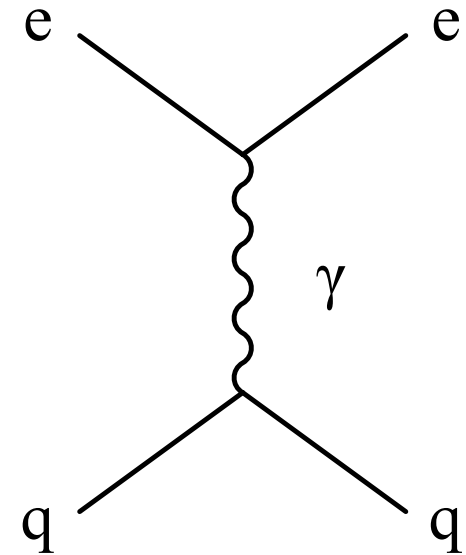
when $p \rightarrow 0$ then $r \rightarrow \infty$

$F (= -\Delta p)$ on q can extend to $r = \infty$

Of course, force get smaller ($p \rightarrow 0$)

(Gives precisely inverse square law)

Electro-magnetic Force



Weak Interaction

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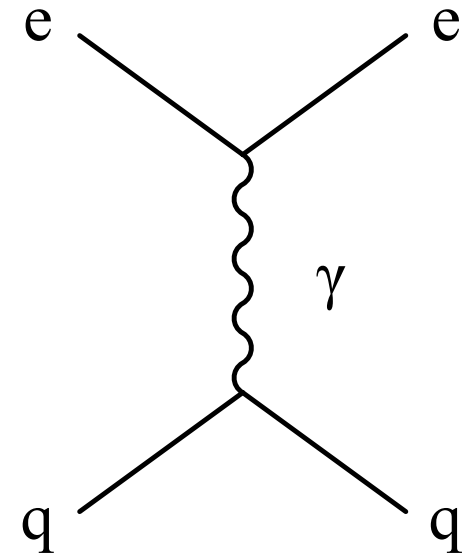
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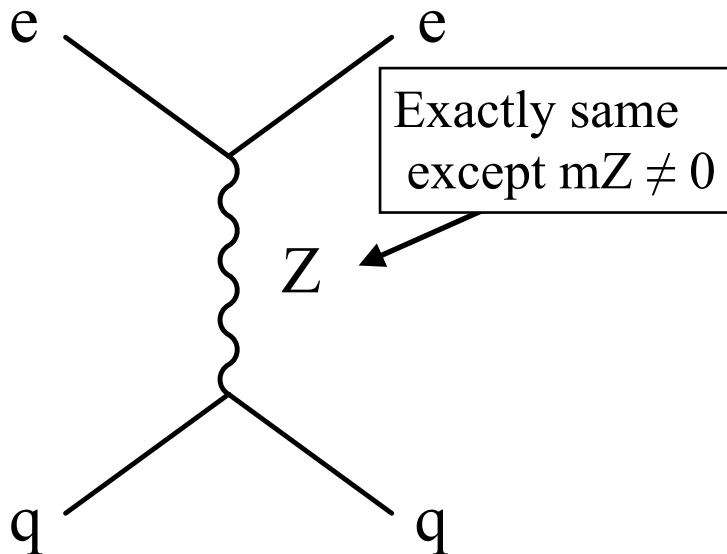
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Electro-magnetic Force



Weak Force



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Weak Interaction

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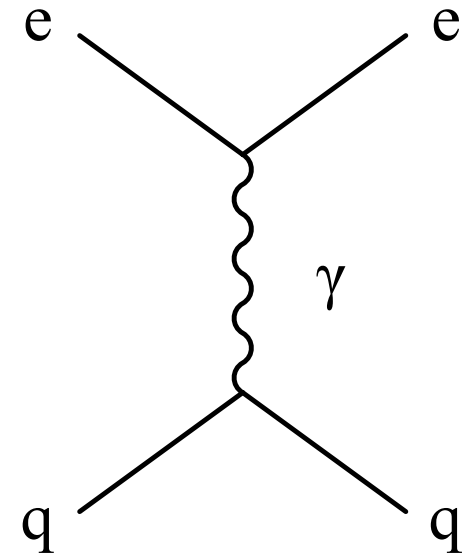
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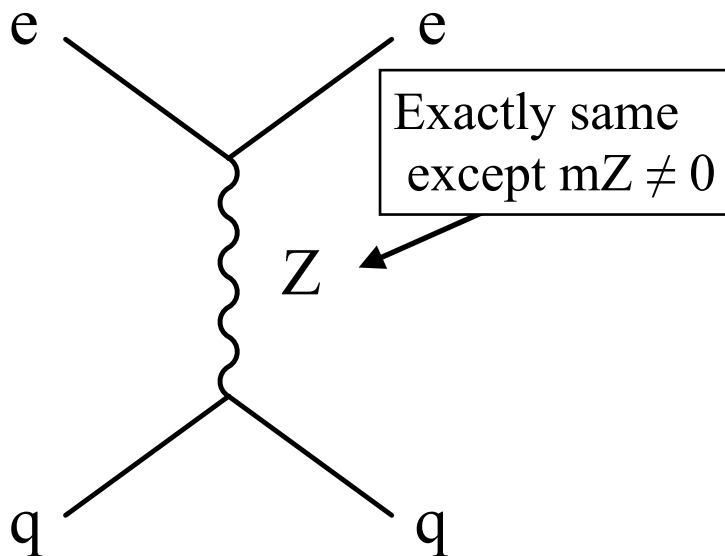
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Weak Force



Electron high probability to emit Z when:

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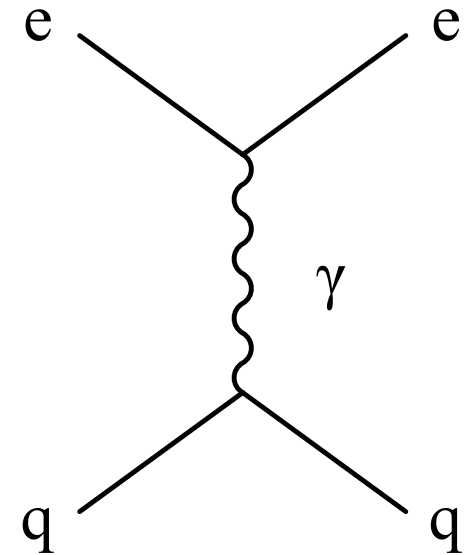
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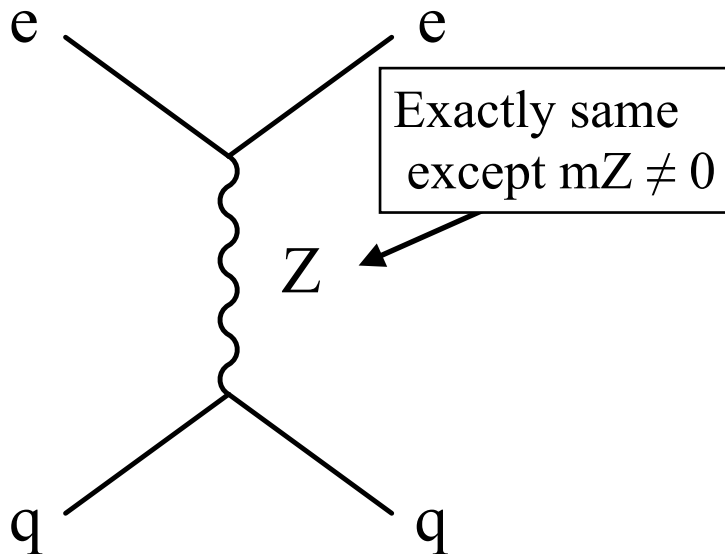
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Electro-magnetic Force



Weak Force



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when $p \rightarrow 0$ then $r \rightarrow \sim 1/mZ$

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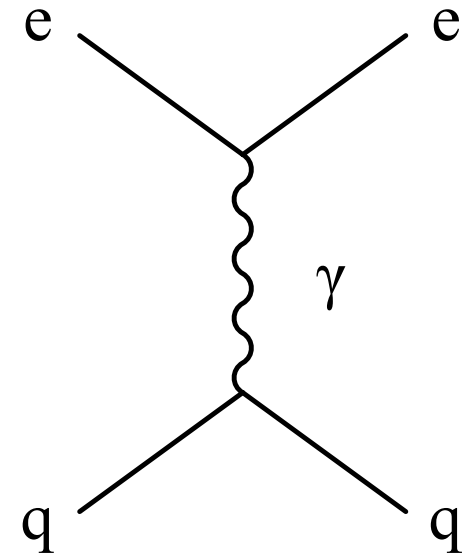
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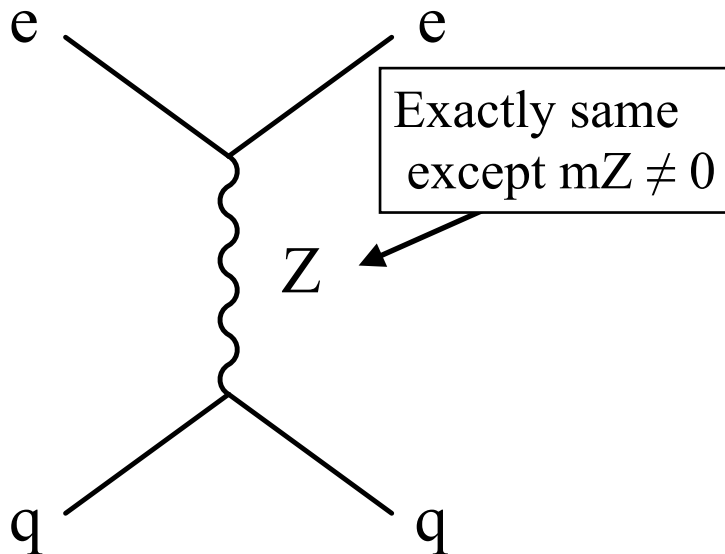
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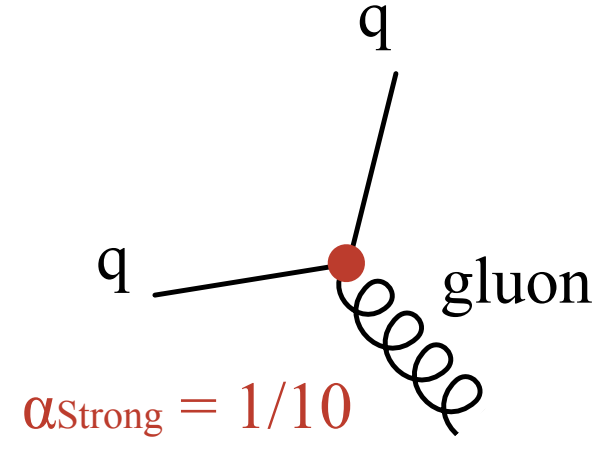
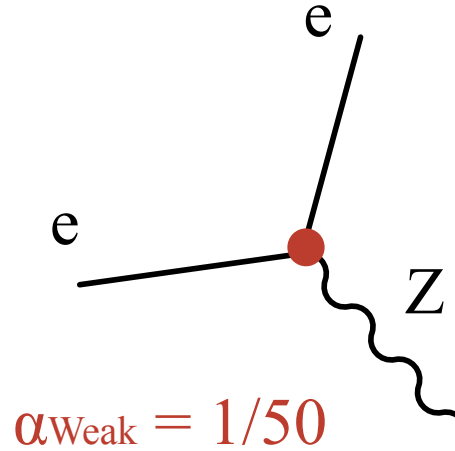
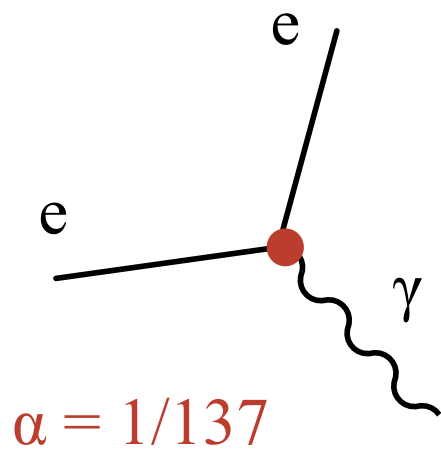
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F ($= -\Delta p$) on q cannot extend to $r = \infty$

Mass of Z makes weak force short ranged.

Forces Common Language

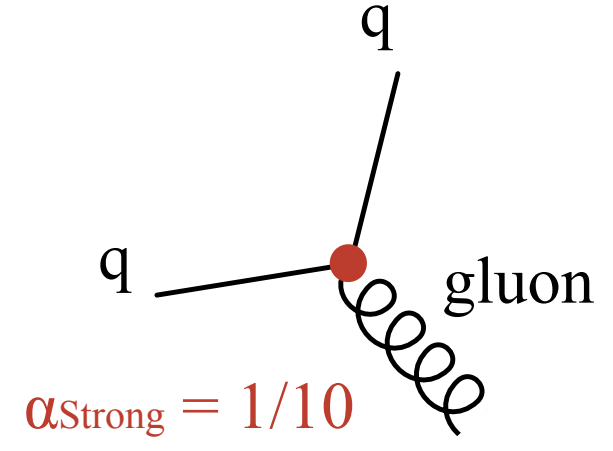
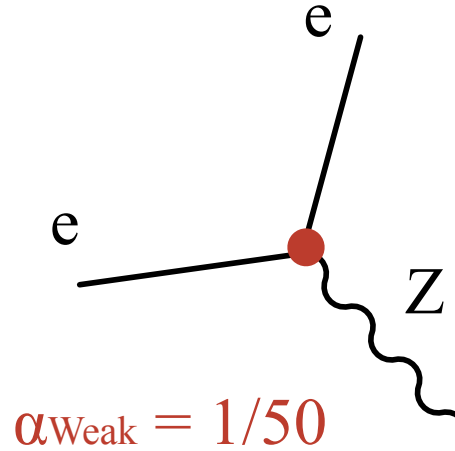
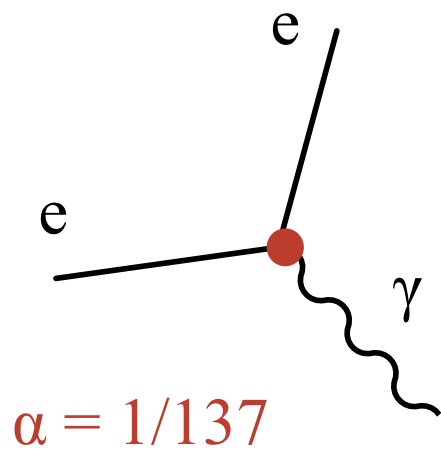
First time that we see that all forces described in same basic way.



Forces look very different to us...

Forces Common Language

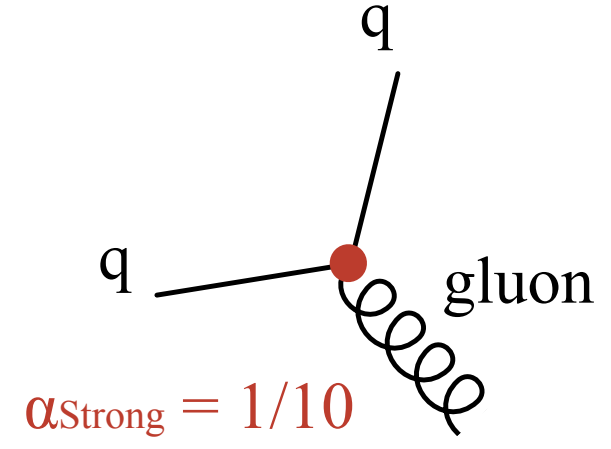
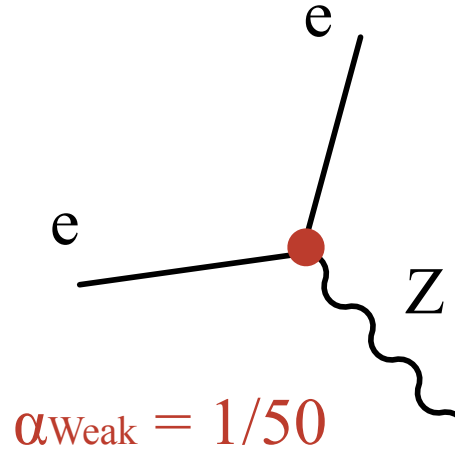
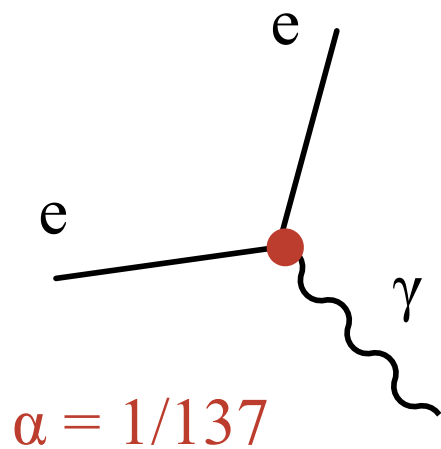
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Forces look very different to us... **is a long distance illusion!**

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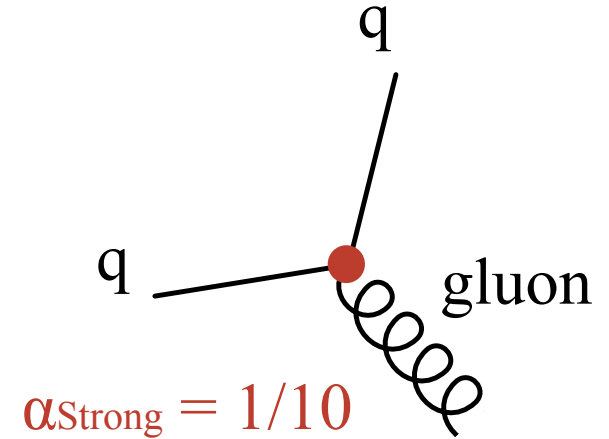
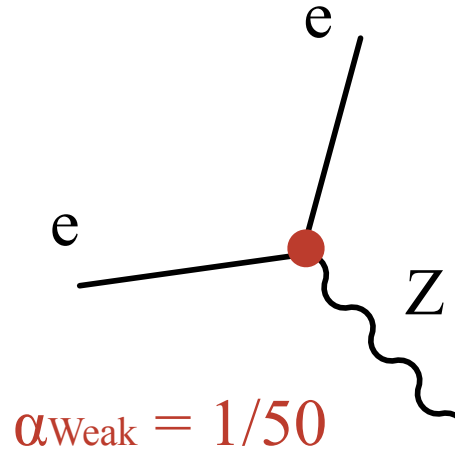
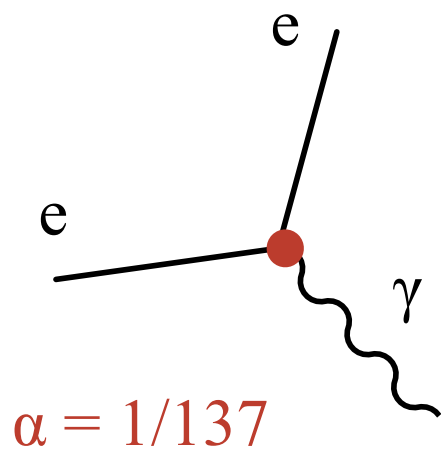
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- Strong force: anti-screening / confinement
- Weak force: massing force carriers

At short distance ($\sim 1/m_Z$) all look the forces start to look the same

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Forces look very different to us... **is a long distance illusion!**

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At short distance ($\sim 1/m_Z$) all look the forces start to look the same

This is the reason we build colliders! Unity at small scales.

The Standard Model

The Standard Model took on modern form in 60s - 70s.

Makes very precise predictions, shown to be highly accurate.

Consistent theory of electromagnetic, weak and strong forces ...

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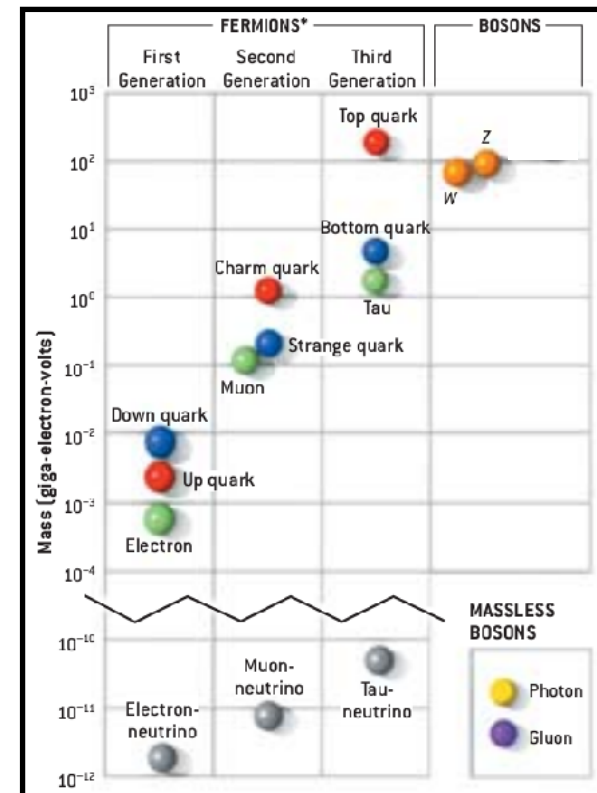
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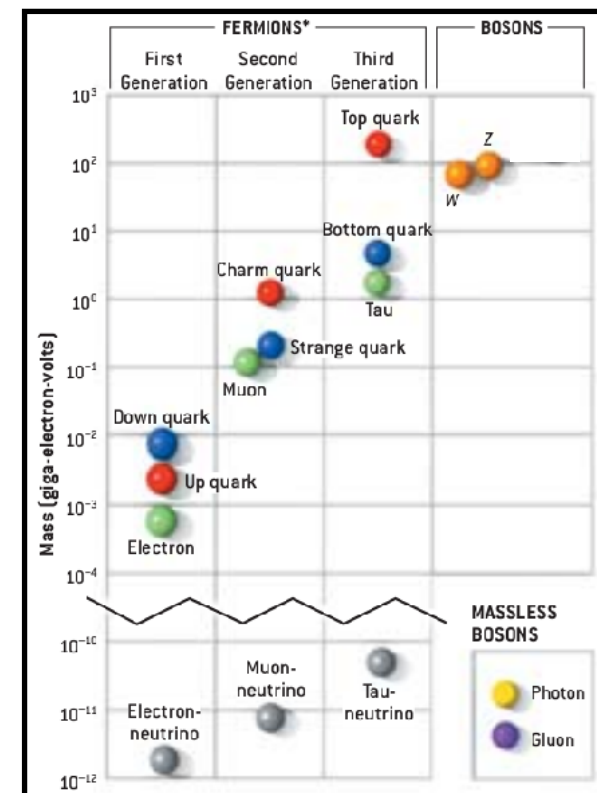
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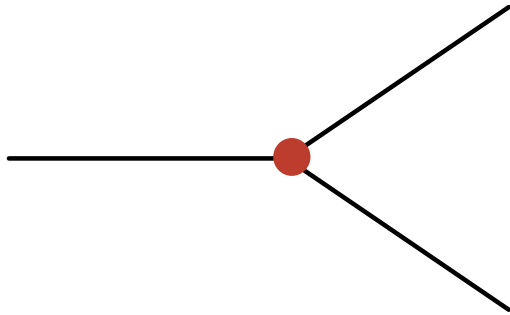
*Serious problem as matter and
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Pick up here next time.



Bonus

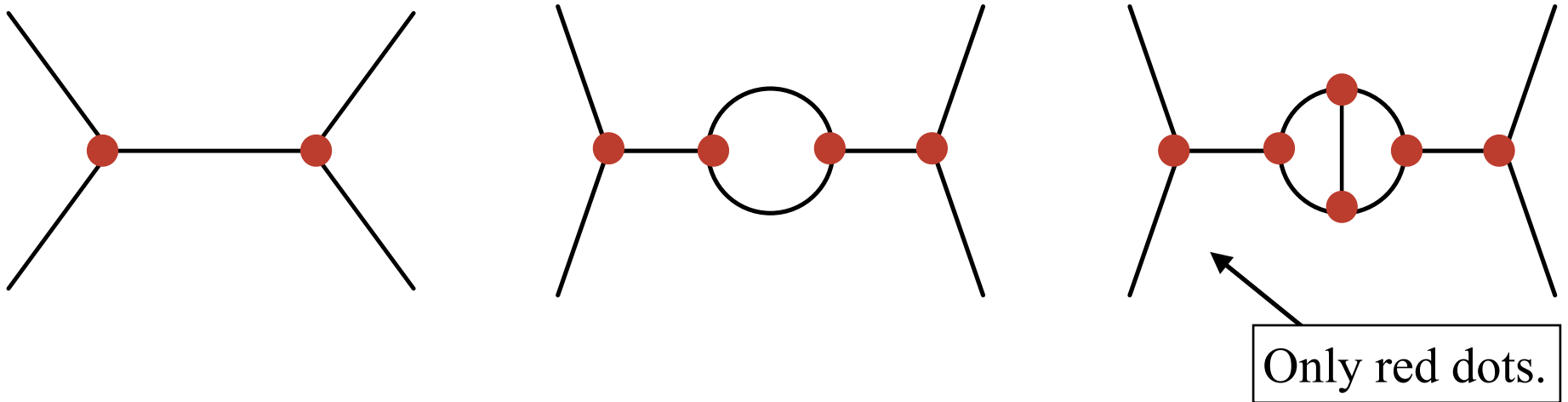
Number of Parameters



Vertex interaction strength input to the theory
- Taken from data

QFT \Rightarrow Only this “three point” interaction relevant

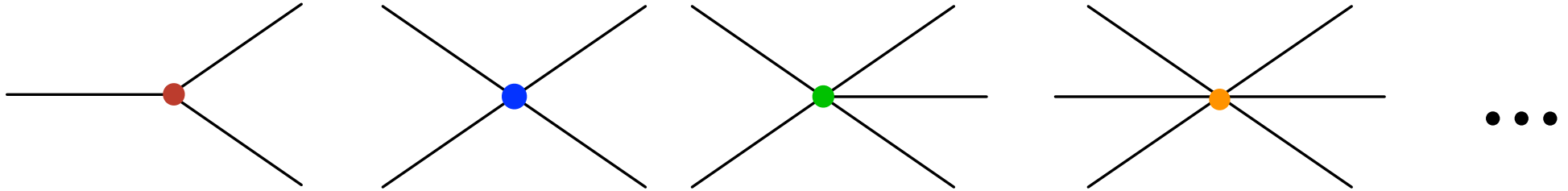
All calculations done by just stitch together this one basic vertex



One parameter (●) is enough to calculate all graphs

Number of Parameters

If all vertices relevant (as in NR QM)



Each term introduces a new unknown parameter.
Lose predictive power

