



# *Bio-Functionalized Surfaces*



# *Hard / Soft Interfaces*

Electronic structure, absorption and reactivity properties are tunable

- Change due to interface correlations
- Ionic multilayers screen fields
- Interactions with Applied Electric Fields
- Multiple Dielectric Interfaces

Change the behavior of polymers in the vicinity of the hard, wet surface

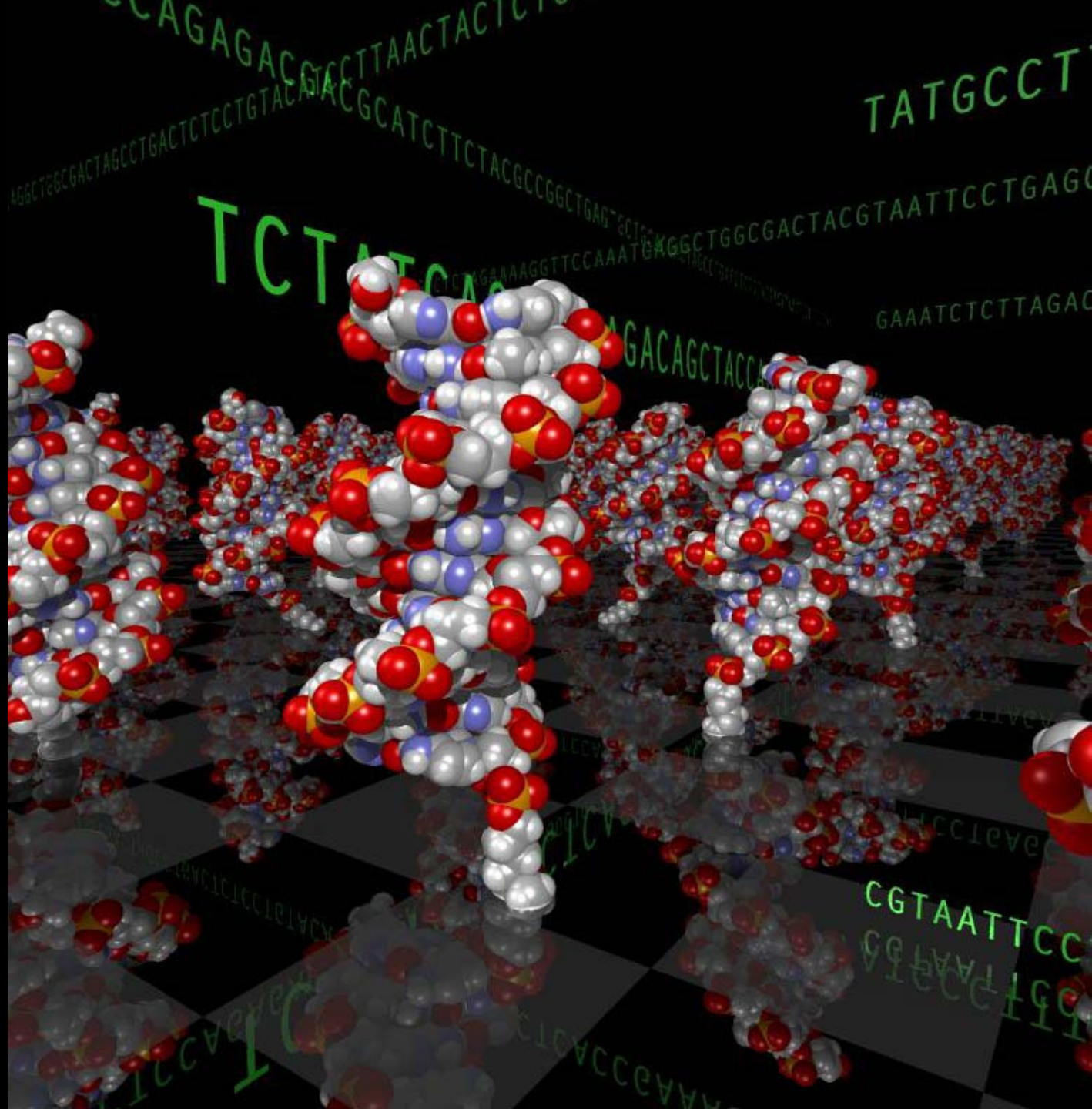
# *Interfaces:*

## *Nano Heterogeneity*

Surfaces, Beads, Shells...

- Changes in Species
- Large Changes in Electric Fields
- Changes in Density

Natural Place for Chemical Work



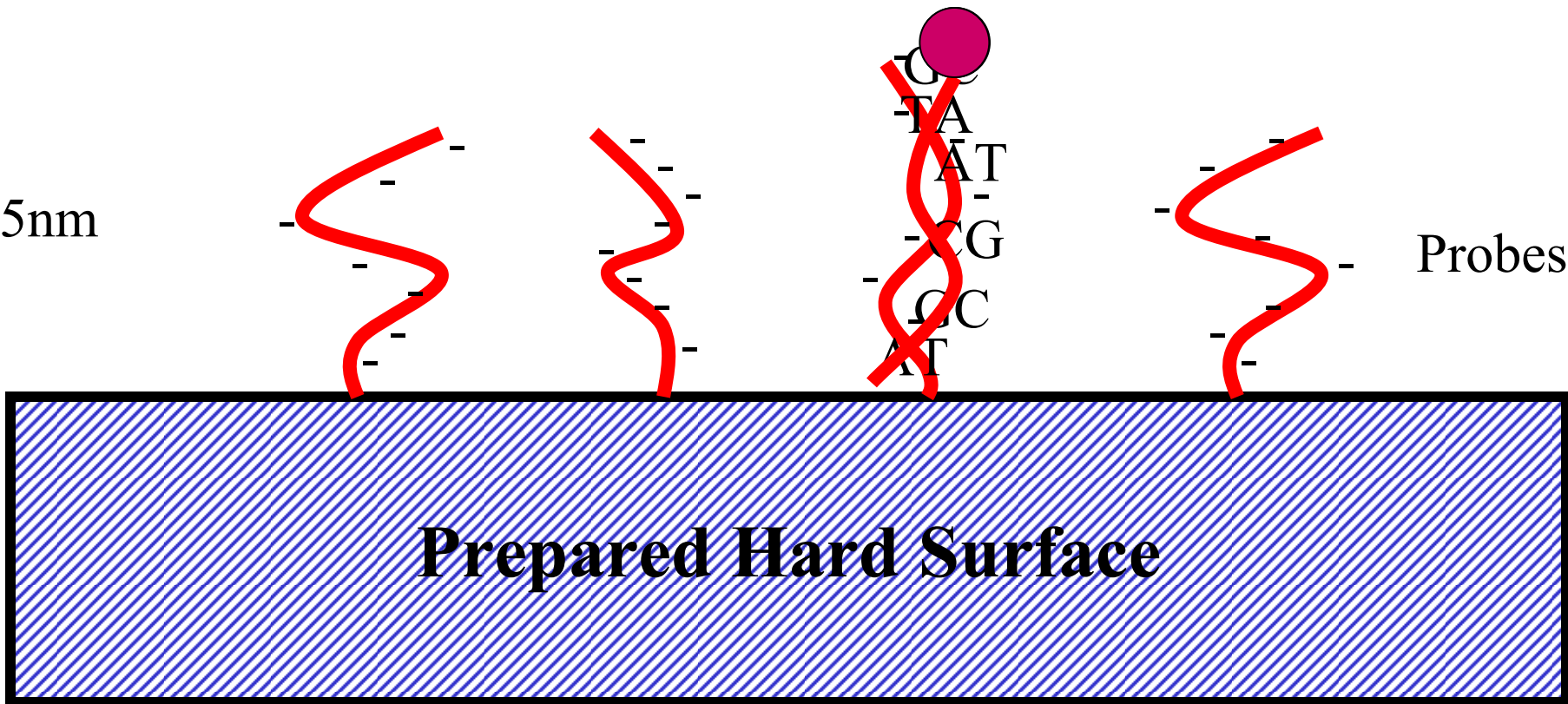
*Salt Water*

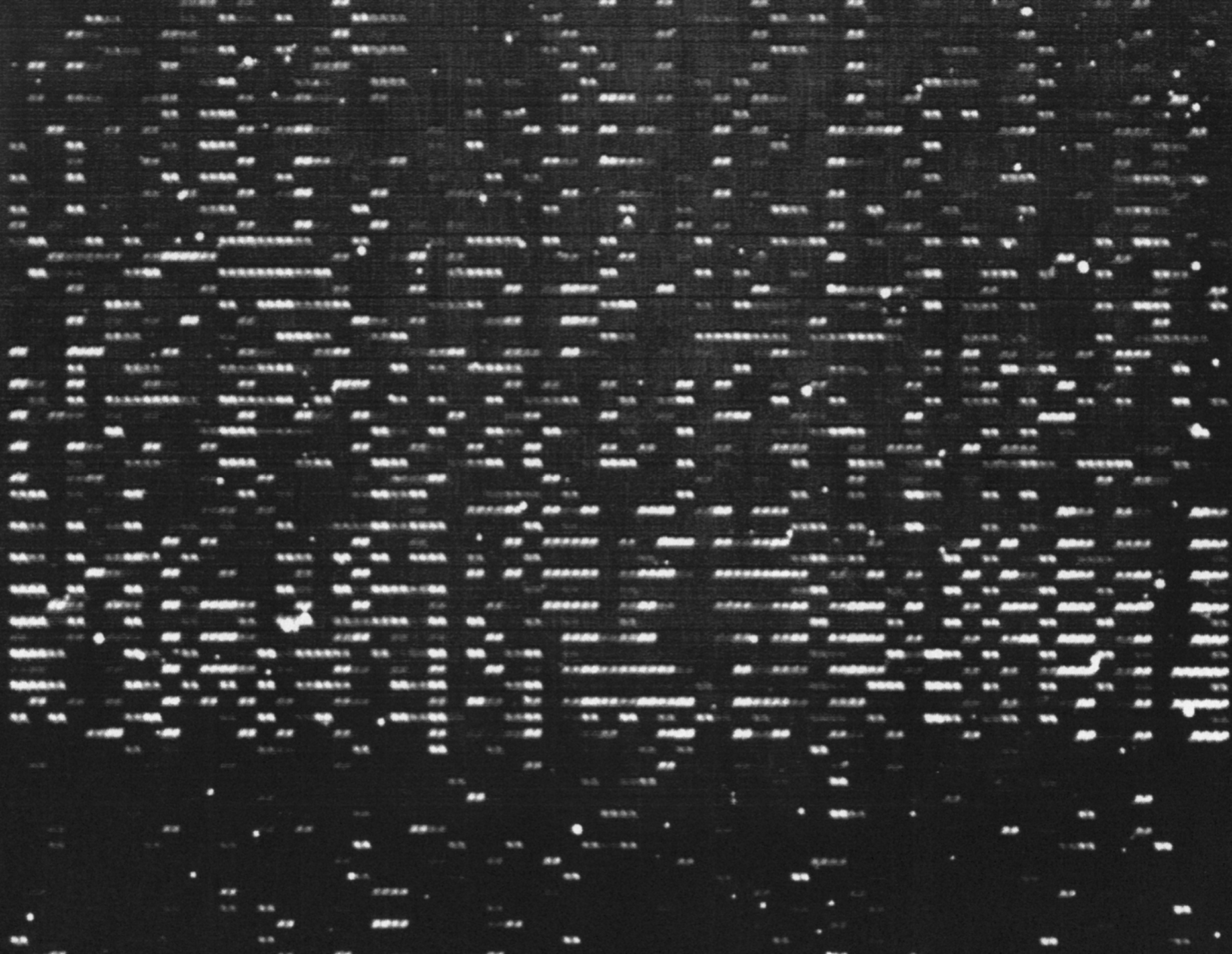
Targets

5nm

Probes

**Prepared Hard Surface**







# ***DNA & Protein Microarrays***

are useful for a variety of tasks

- Genetic analysis
- Disease detection
- Synthetic Biology
- Computing

# *Problems in Microarrays*

## Cross platform comparisons

- Controls
- Validation
- Data bases for comparisons

Nearly impossible due changes in physics  
and chemistry at the surface



# *Central Theoretical Issue:*

Binding (recognition) is different in the presence of a surface than in homogeneous solution.

The surface determines:

Polarization fields

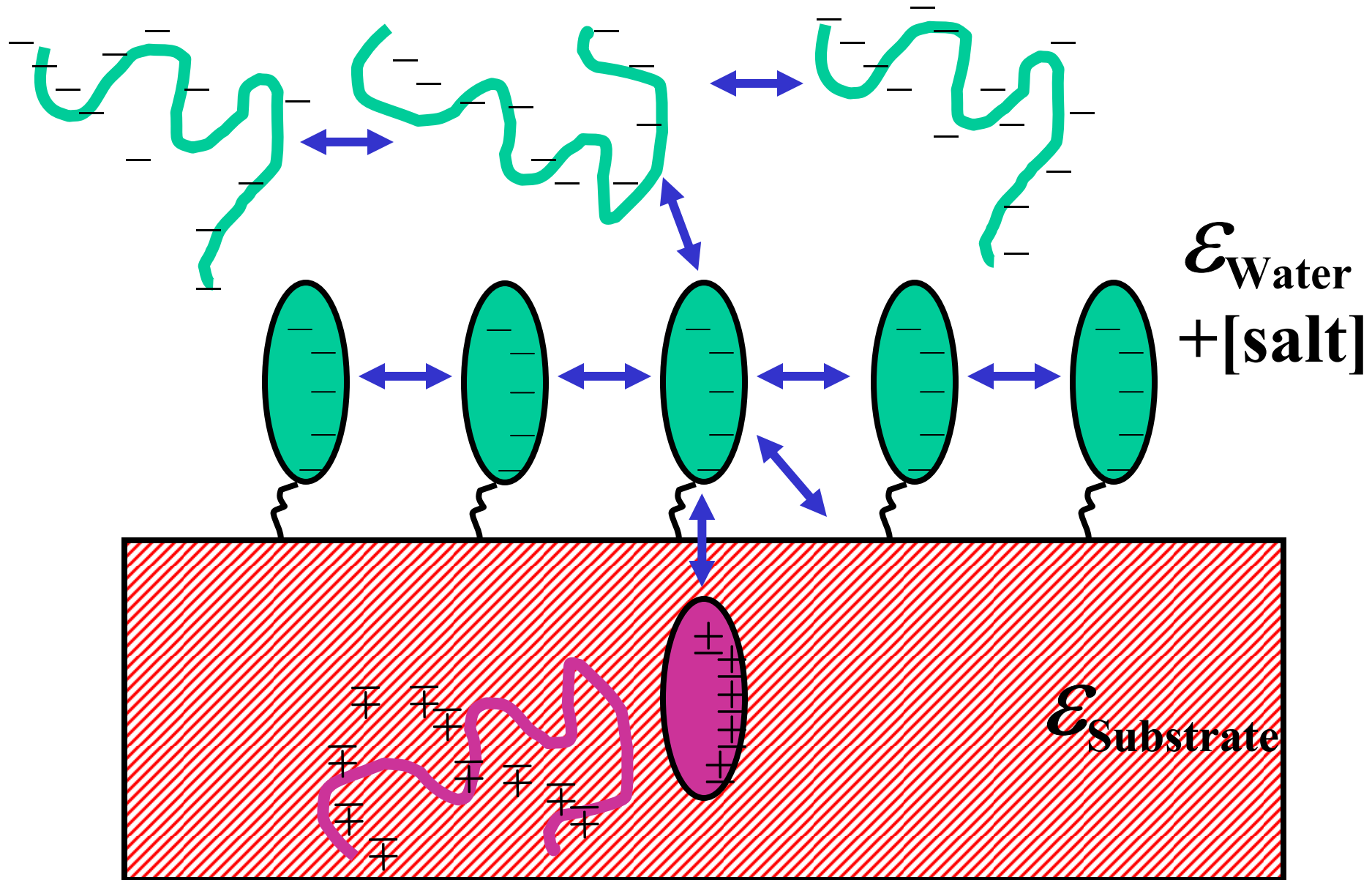
Ionic screening layers

Ultimately: Device response

# *Simulations, Theory and Data Processing*

- *Simulations at the Atomic Level*
  - *Detailed, Accurate*
  - *Expensive Time consuming*
- *Theory*
  - *Approximate Rules of Thumb*
- *Processing the Image Data*
  - *Must be Fast and Accurate*

# *Forces: Surface and Solution*

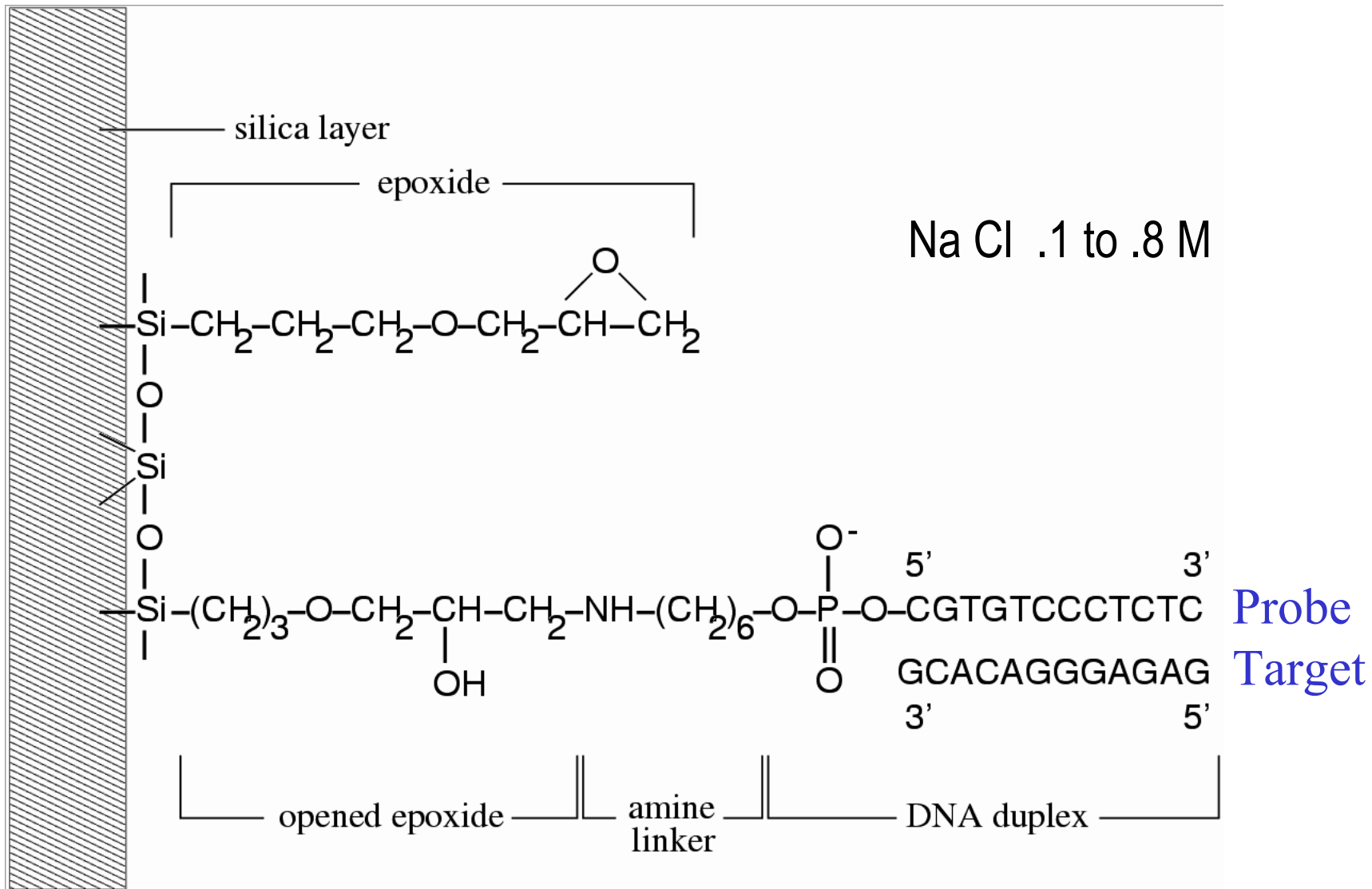


# *Simulations or Theories of Bio Chips*

Set up must include

- Substrate (Au, Si, SiO<sub>2</sub> ...)
- Electrostatic fields
- Surface modifications
- Spacers (organic)
- Probe and Target Bio (DNA or protein) strands
- Salt and lots of Water

# *The Chemistry*



# *Simulate a simple classical force field*

Model the interactions between atoms

- **Bonds** - 2 body term
  - harmonic, Hooke's law spring

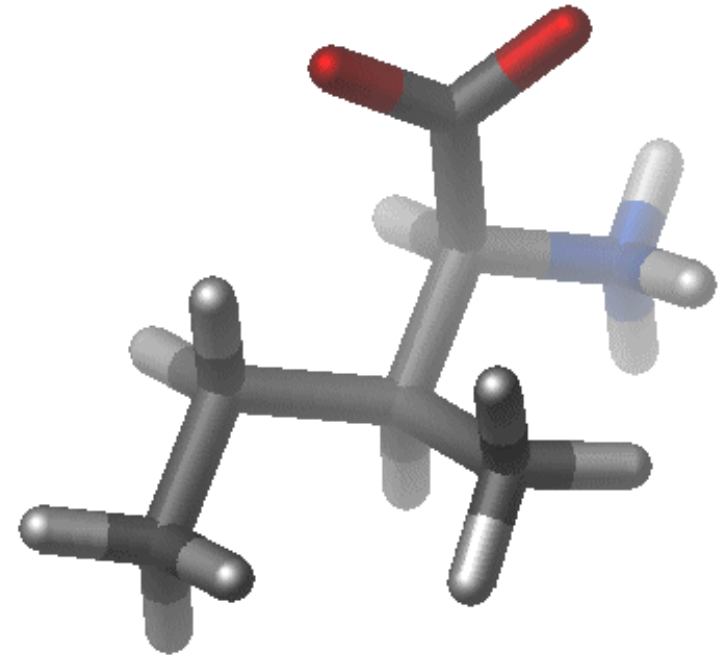
$$\sum_{bonds} K_b (r - r_e)^2$$

- **Angles** - 3 body term

$$\sum_{angles} K_\theta (\theta - \theta_e)^2$$

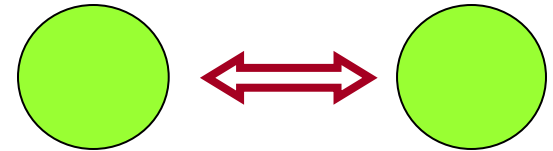
- **Dihedrals** - 4 body term

$$\sum_{torsions} K_\phi (1 + \cos(n\phi + \delta))$$



Source: [http://www.ch.embnet.org/MD\\_tutorial/](http://www.ch.embnet.org/MD_tutorial/)

## Nonbonded Terms



- 2 body terms
- van der Waals (short range) & Coulomb (long range)

$$\sum_{\substack{\text{Nonbonded} \\ \text{pairs of atoms}}} 4\epsilon_{ij} \left( \left( \frac{\sigma_{ij}}{r} \right)^{12} - \left( \frac{\sigma_{ij}}{r} \right)^6 \right) + \frac{q_i q_j}{r}$$

- Coulomb interaction consumes > 90% computing time

Ewald Sum electrostatics to mimic condensed phase screening

- Periodic Boundary Conditions

Electrostatic Forces Dominate Behavior



$$\mathbf{F} = m\mathbf{a} \quad \text{or}$$

$$-\nabla V(\mathbf{r}) = m\ddot{\mathbf{r}}$$

With a classical Molecular Mechanics  
potential,  $V(\mathbf{r})$

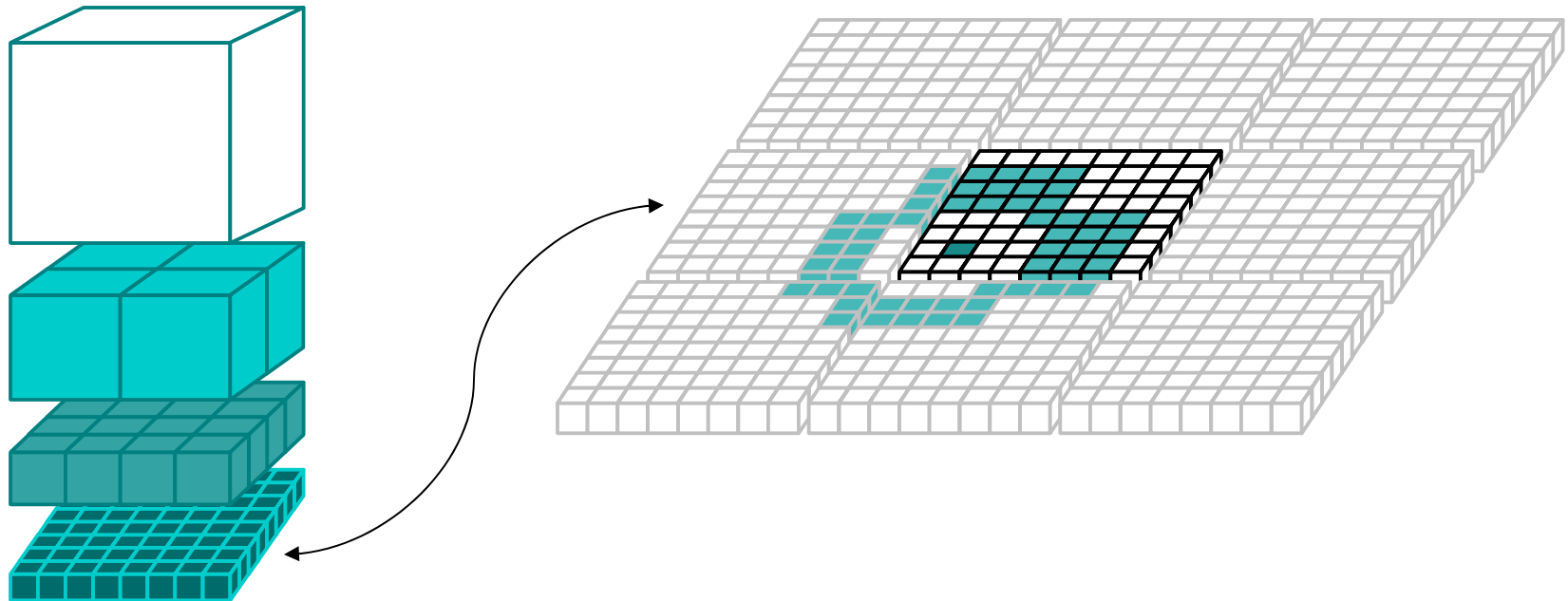
These potentials have only *numerical* solutions.

$$\mathbf{r}(t + \Delta t) = \mathbf{r}(t) + \dot{\mathbf{r}}(t)\Delta t + \frac{1}{2!}\ddot{\mathbf{r}}(t)\Delta t^2 + O(\Delta t^3)$$

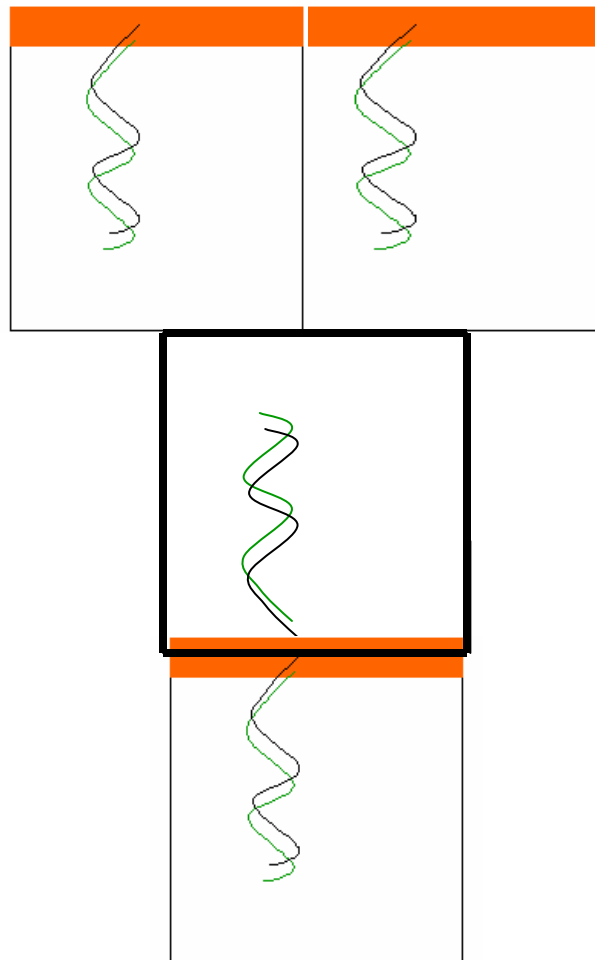
$\Delta t$  must be small,  $10^{-15}\text{s}$

# *Ewald Fast Multipole*

- Insist on deterministic trajectories
- Relative precision  $\Delta F_{ij} < 10^{-6}$  wrt Ewald
- Very fine grain communications  
overlapping and inverse message pulling
- 40x over optimized Ewald for 100K atoms



# Periodic Boundaries for Surfaces: Change symmetry



Skew BCs

0 ns



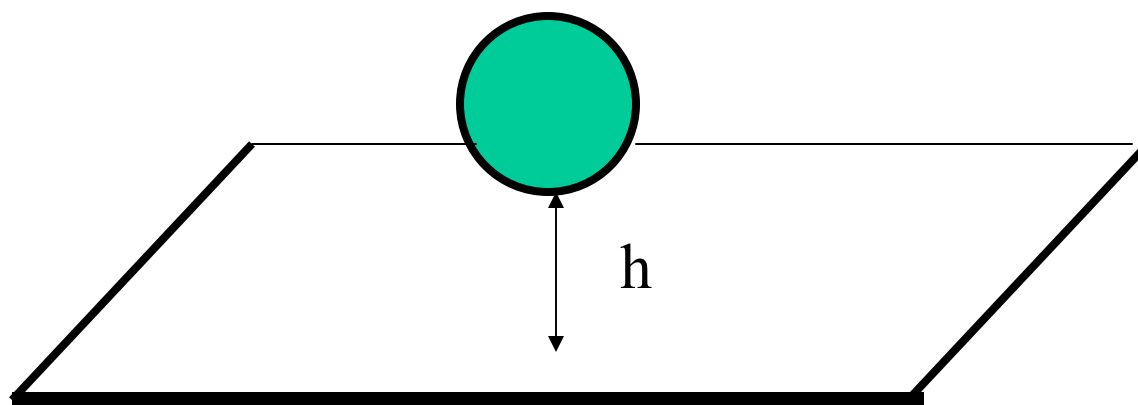
# *Implications*

- Colloidal behavior affects
  - synthesis / fabrication
  - and binding
- Tilt restricts possible geometries of pairing
- Low fraying consistent with high affinity and good specificity at low target concentration

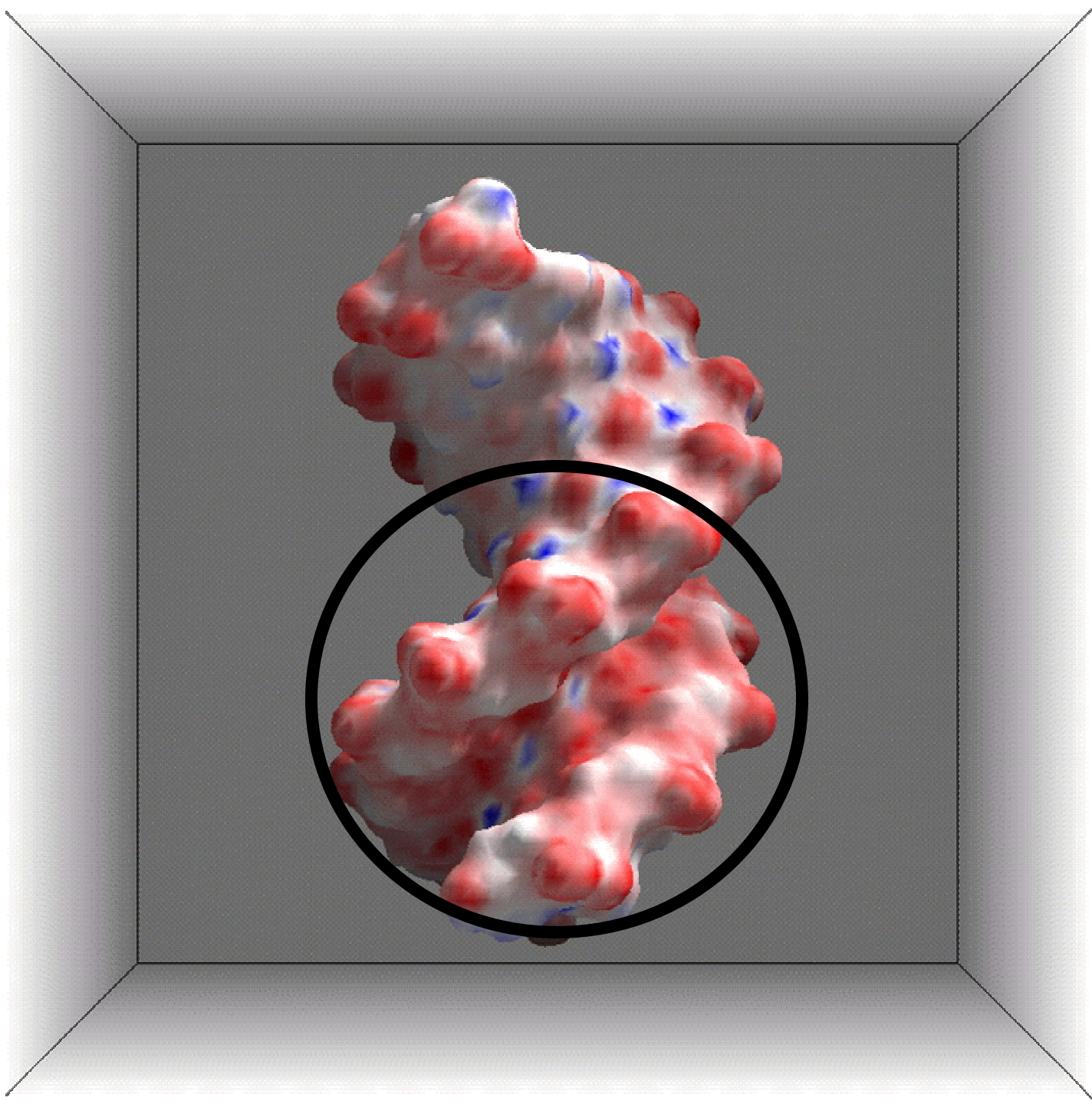
**$\Delta G$  &  $\Delta\Delta G$**

# *A Simple Model*

- Ion permeable, 20 Å sphere over a plane/surface
  - 8 bp in aqueous saline solution over a surface
- Linear Poisson-Boltzmann has an  
**analytic solution**



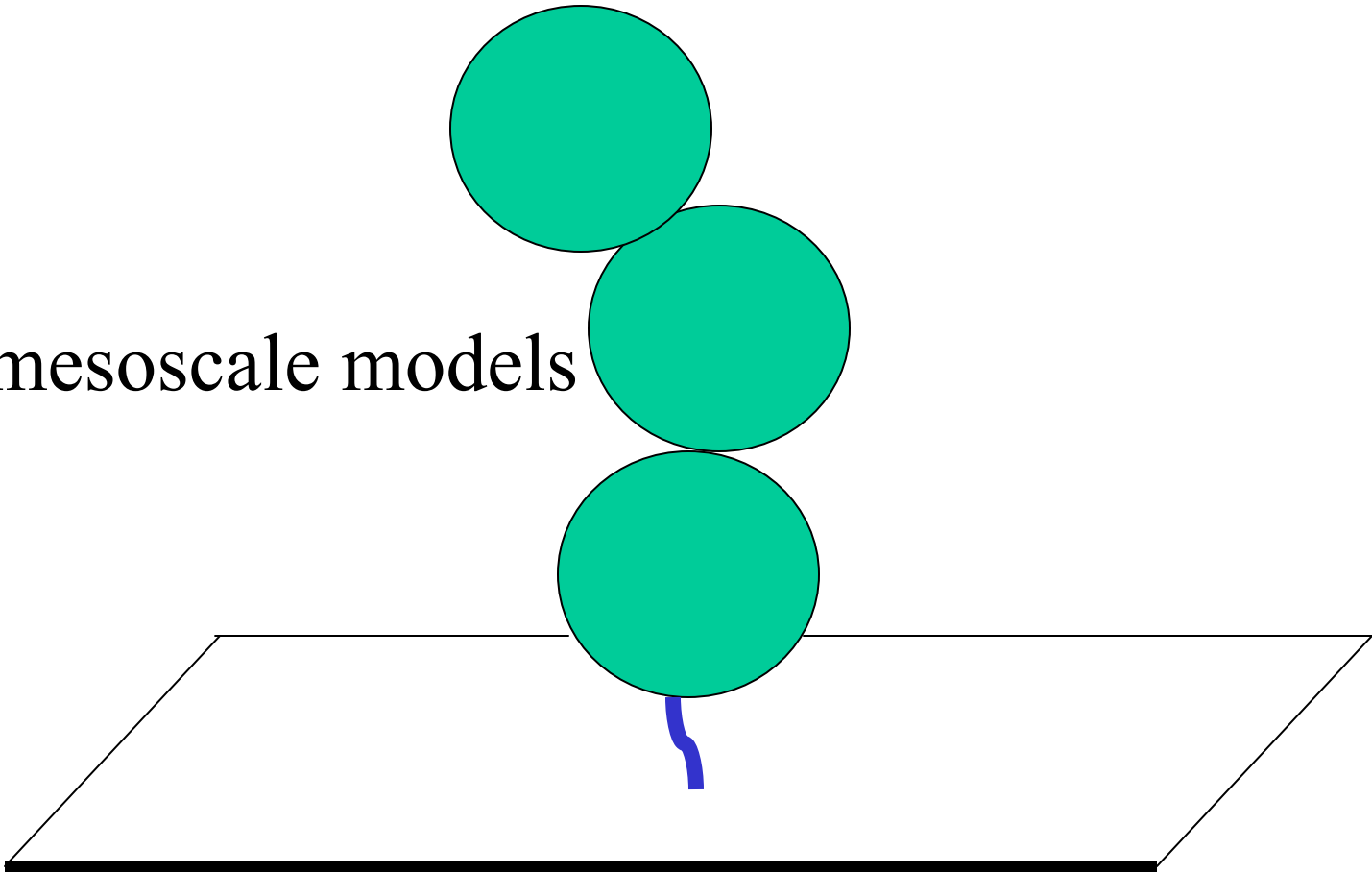
Poly - Ohshima and Kondo, '93  
DNA - Vainrub and Pettitt, CPL '00  
Ellipse - Garrido and Pettitt, CPC, 07



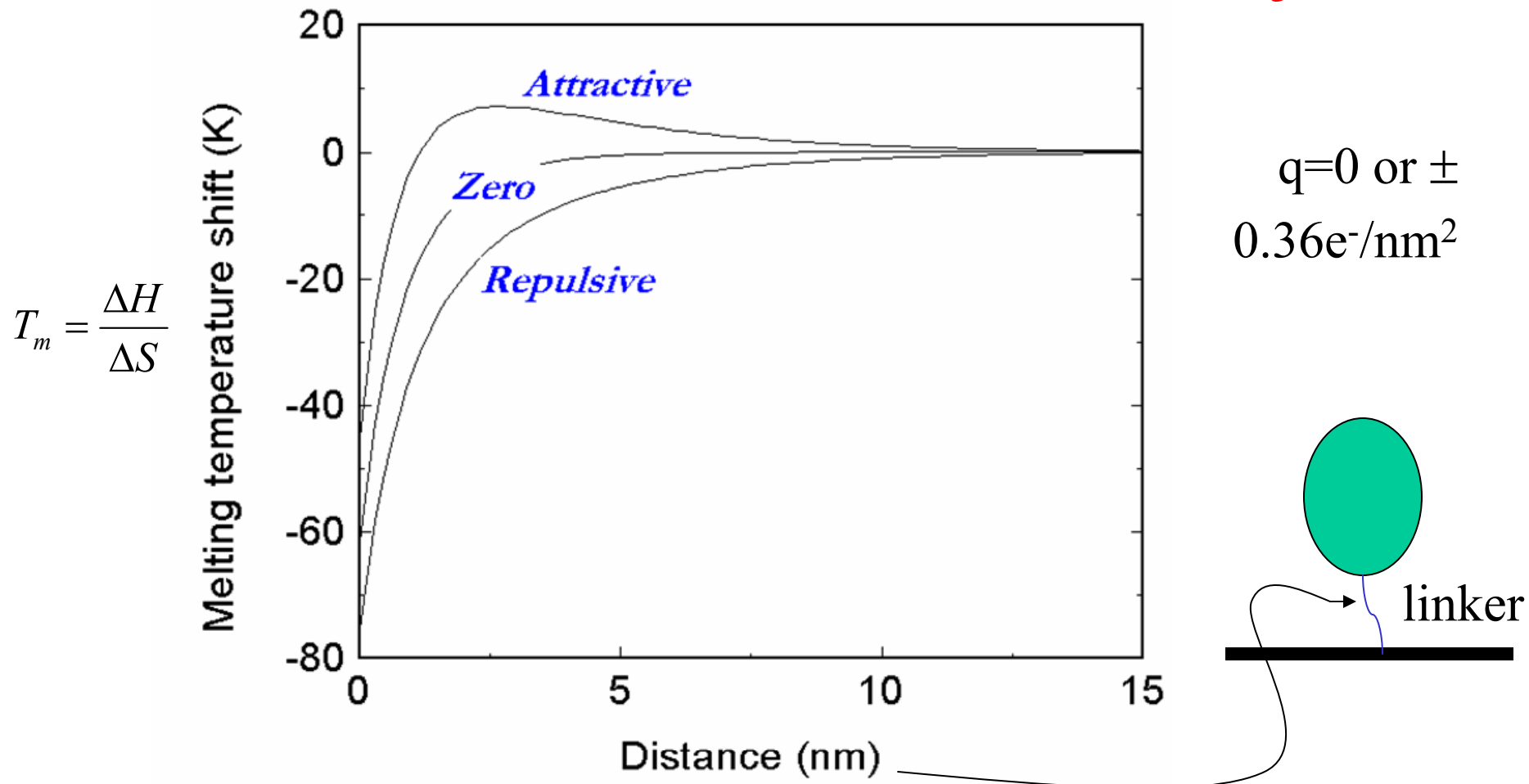


# Longer Sequences are possible

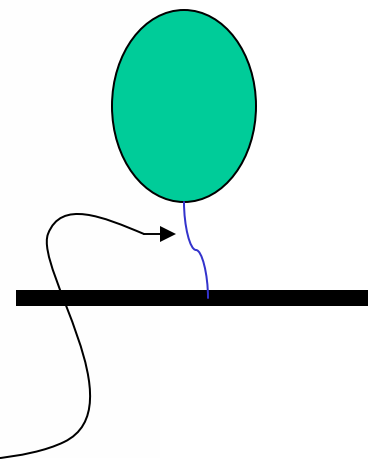
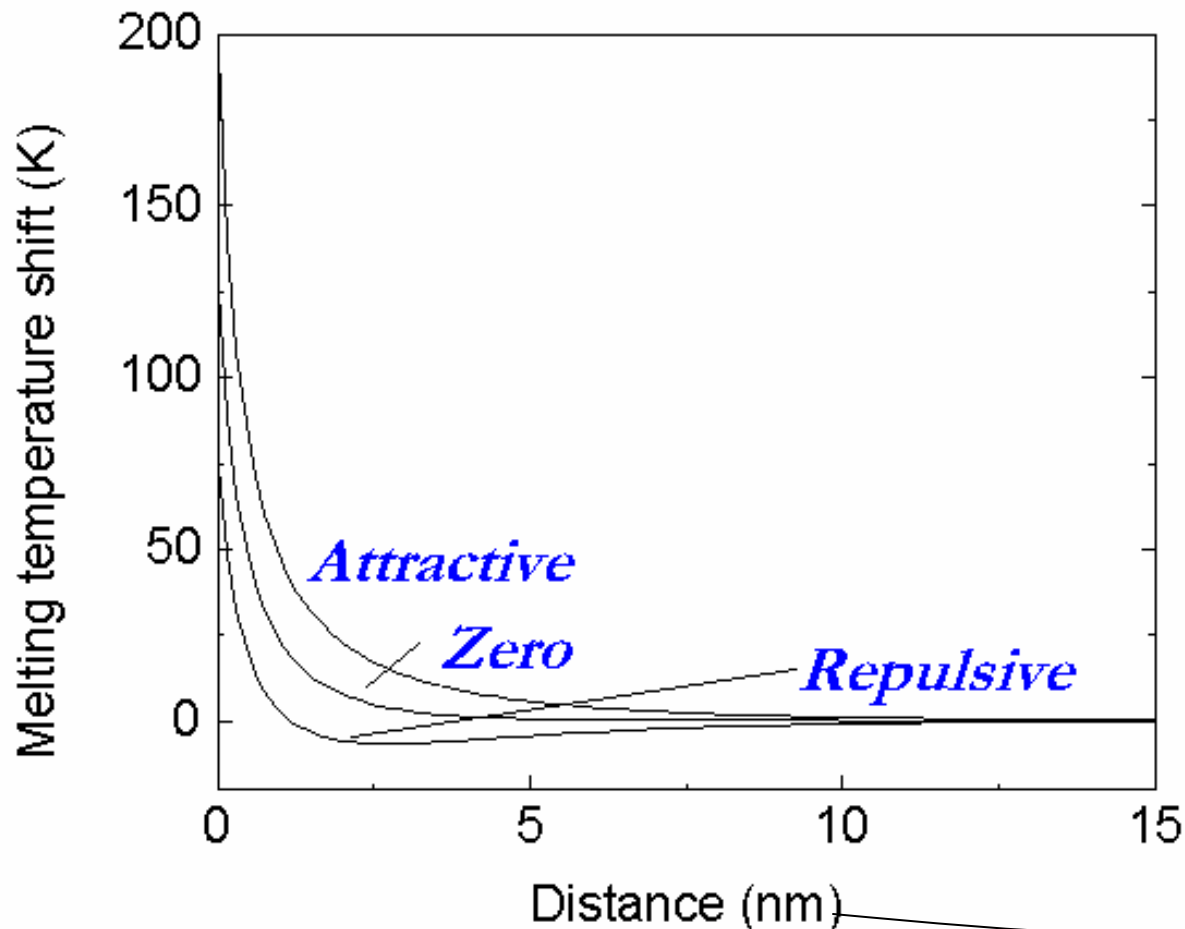
True mesoscale models



The shift of the dissociation free energy or temperature for an immobilized 8 base pair oligonucleotide duplex at 0.01M NaCl as a function of the distance from a *charged dielectric surface*

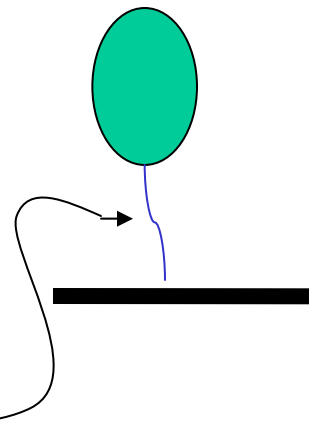
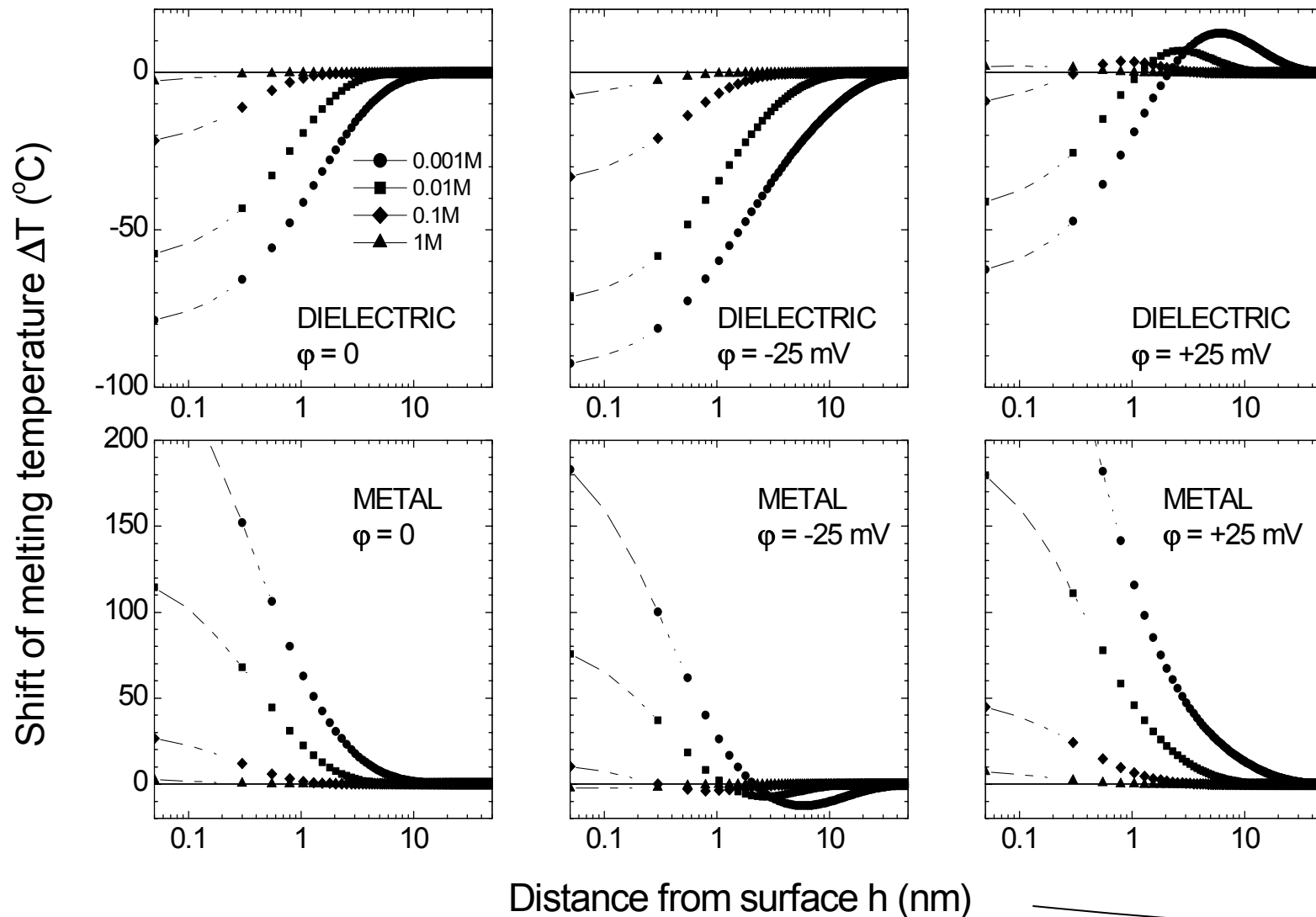


# Surface at a constant potential for a *metal* coated substrate @ .01 M NaCl



# *Response to E-fields*

## Salt and Substrate Material Effects on 8-bp DNA



# *Finite Concentration and Coverage*

$$\nabla^2 \phi = \kappa^2 \phi$$

outside the sphere and plane,

$$\nabla^2 \phi = \kappa^2 \phi - (\rho / \epsilon \epsilon_0)$$

inside the sphere,

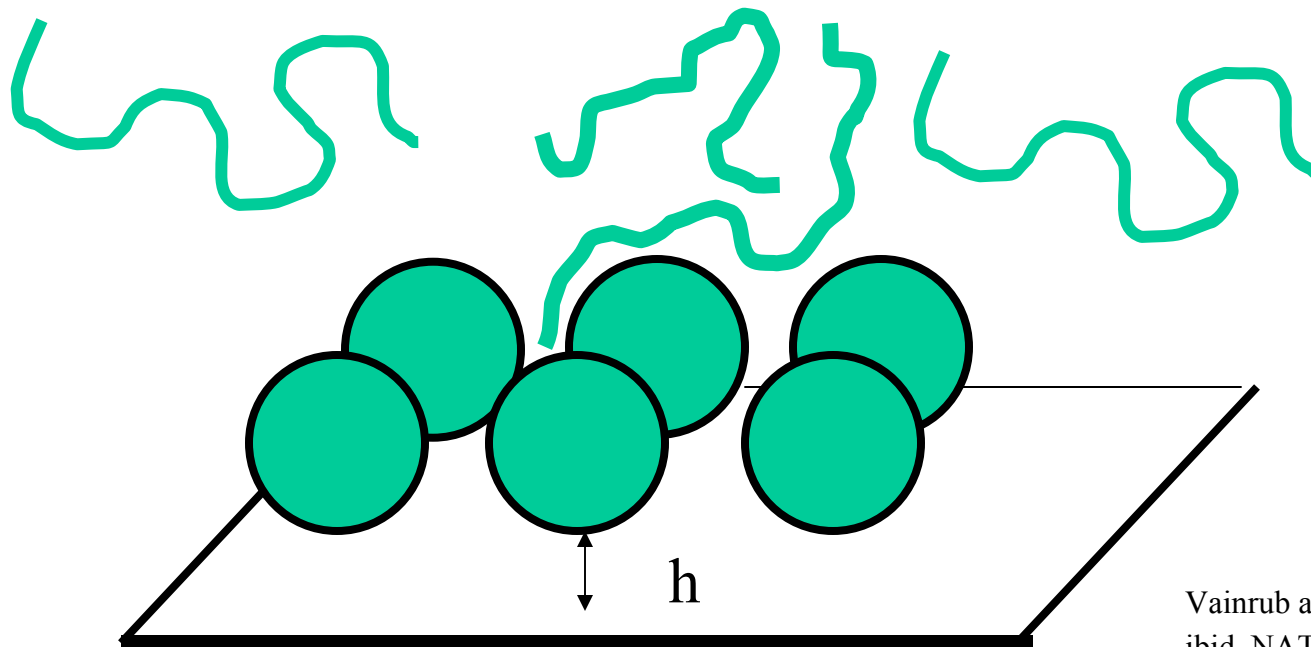
$$\phi|_{r=a+} = \phi|_{r=a-}, \quad r \phi|_{r=a+} = r \phi|_{r=a-}$$

on the sphere,

$$\phi|_{z=0+} = \phi|_{z=0-}, \quad z \phi|_{z=0+} - r \phi|_{z=0-} = -\sigma / \epsilon \epsilon_0$$

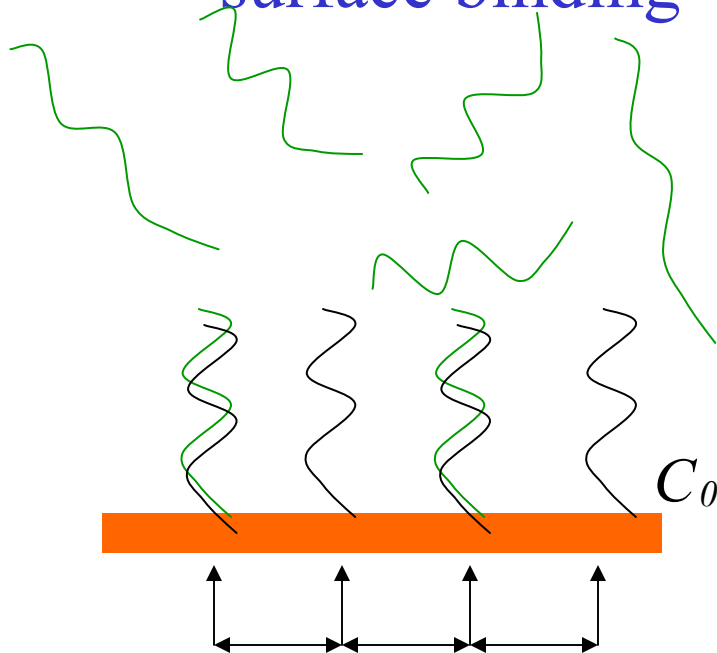
on the plane.

Different from O & K

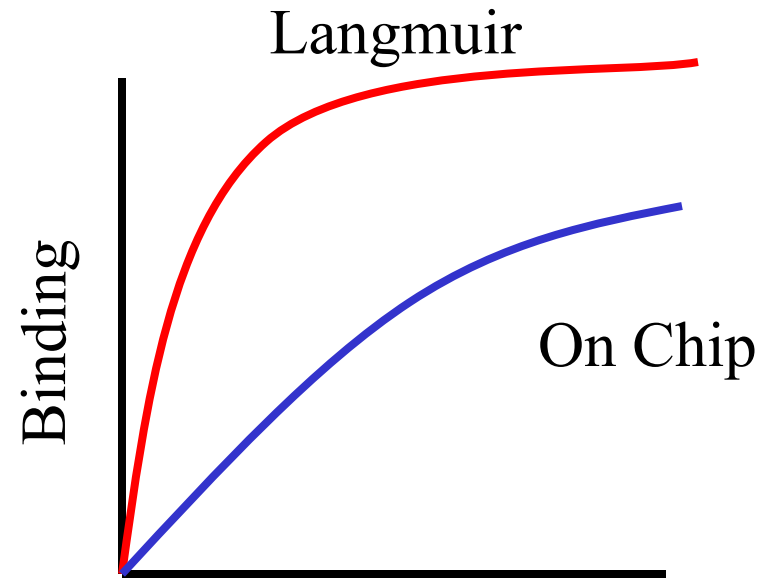


# *Coulomb Blockage Dominates Optimum DNA spacing*

High negative charge density repels target surface binding



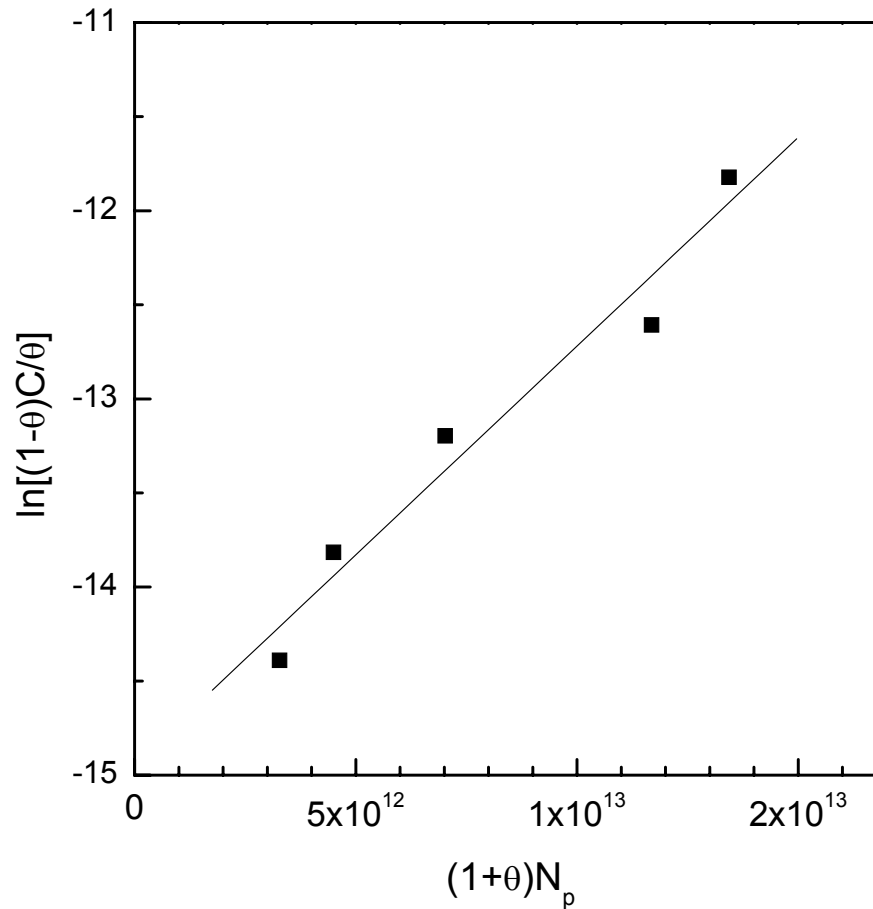
Probe surface density



$$C_0 = \frac{\theta}{1 - \theta} \exp\left(\frac{\Delta H_0 - T\Delta S_0}{RT}\right) \exp\left[\frac{wn_p Z_P (Z_P + Z_T \theta)}{RT}\right]$$

hybridization efficiency  $\theta$  ( $0 \leq \theta \leq 1$ )  
target concentration  $C_0$

# *Fit with Experimental Isotherm*



## **Accord with experiments:**

- Low on-array hybridization efficiency (Guo et al 1994, Shchepinov et al 1995)
- Broadening and down-temperature shift of melting curve (Forman et al 1998, Lu et al 2002)
- Surface probe density effects (Peterson et al 2001, Steel et al 1998, Watterson 2000)



# Melting curve temperature and width

Analytic wrt surface probe density (coverage)

**In solution**

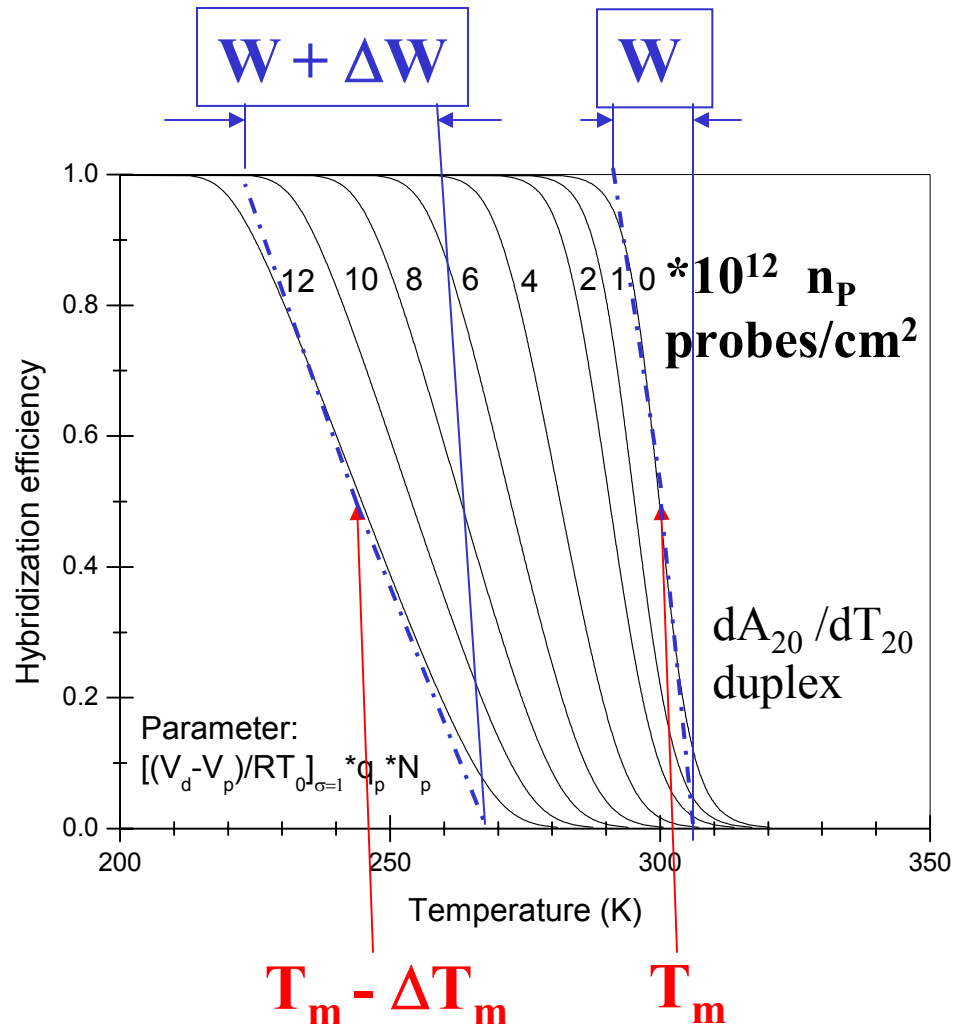
$$T_m = \Delta H_0 / (\Delta S_0 - R \ln C)$$

$$W = 4RT_m^2 / \Delta H_0$$

**On-array: Isotherms**

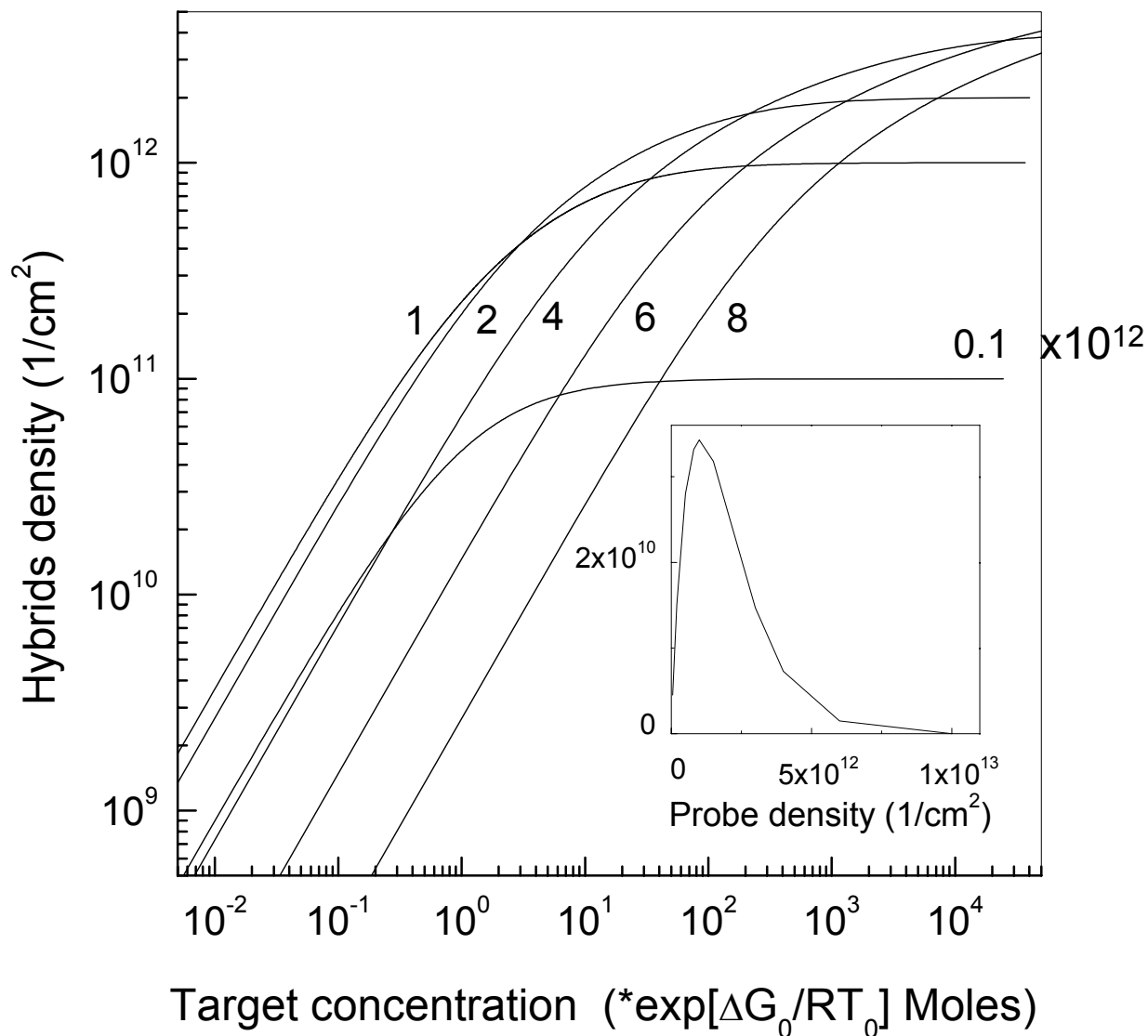
$$\Delta T_m = \frac{3wZ^2n_p}{2\Delta H_0 + 3wZ^2n_p}$$

$$\Delta W = \frac{2}{3} \Delta T_m$$



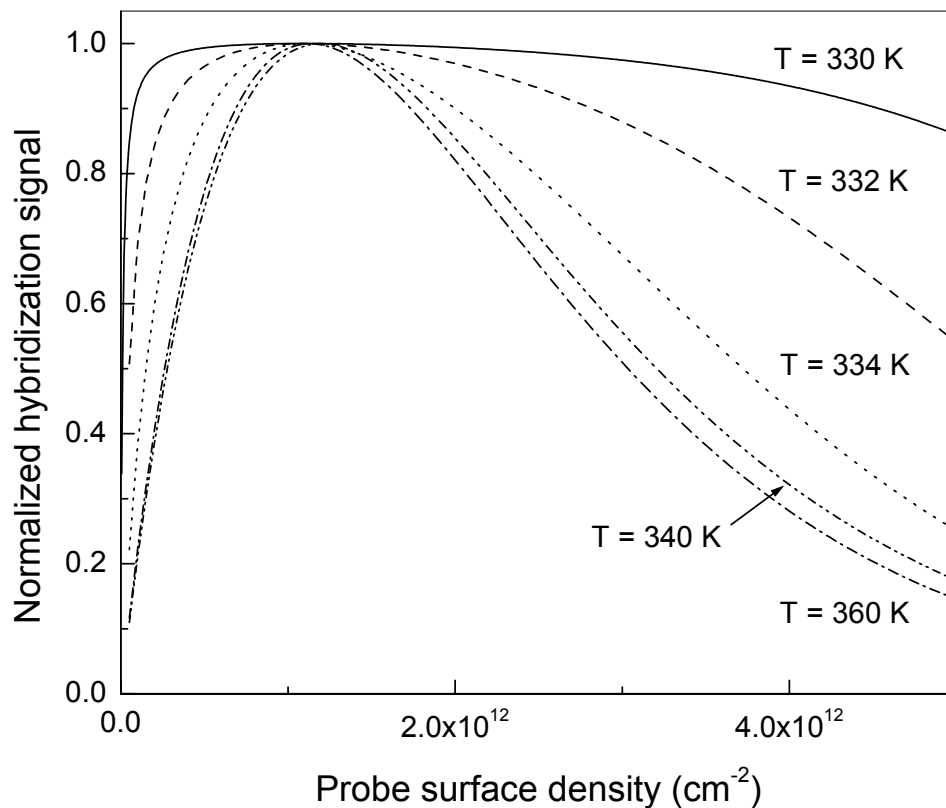
Critical for SNP detection design

# *Strength and linearity of hybridization signal*

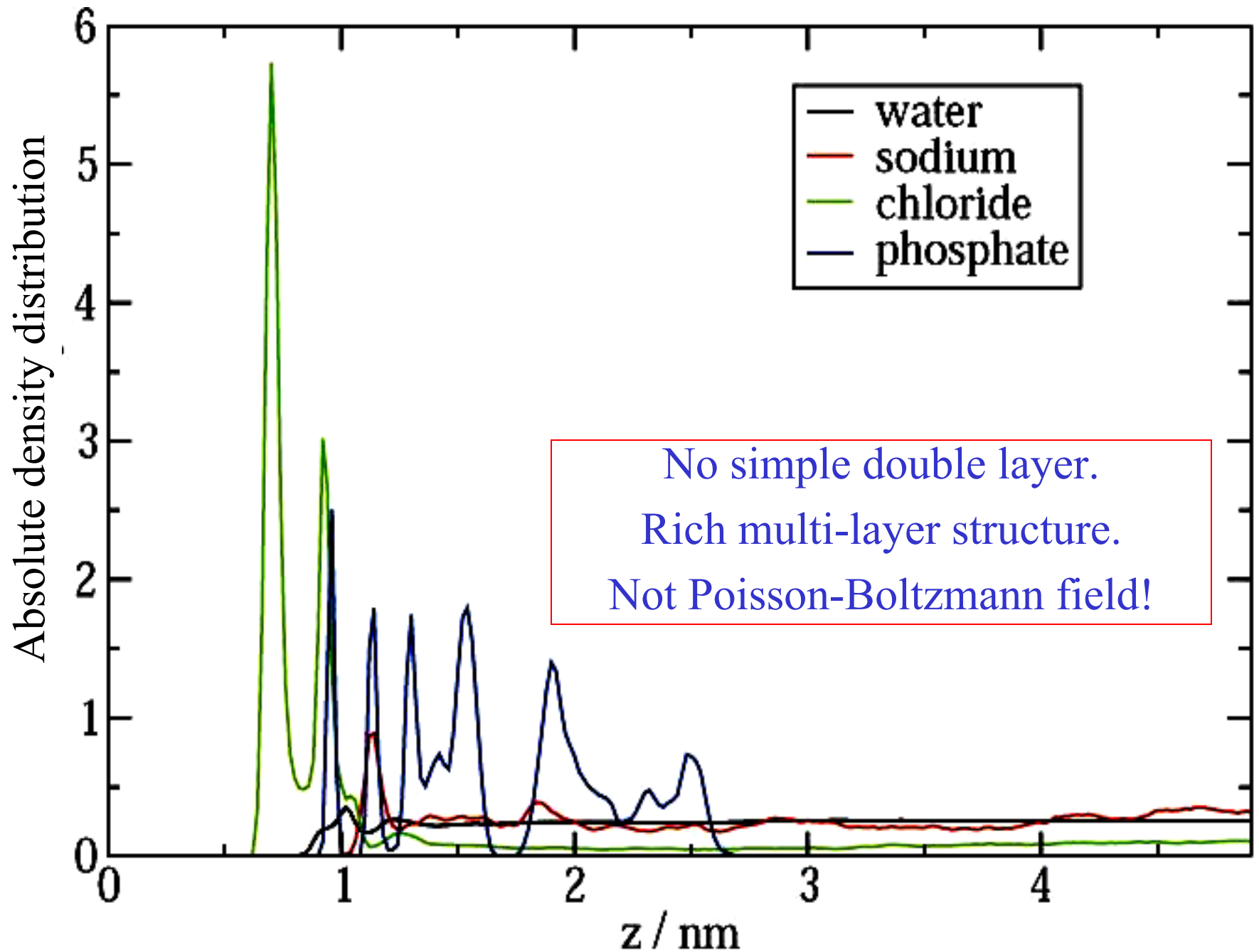


# *Peak of sensitivity also Analytic*

$$n_p = \frac{RT}{wZ_p^2}$$



## *Density Waves at a +ve charged Surface*



# *We Have Strong Correlations*

- Concentration is a poor variable
- Activity is required
- Many non mean field correlations are important
- Multiple length scales competing

# *To design for Affinity and Specificity*

- Use Electric fields
  - Effects of DNA with poly cations
- Use surface effects
  - Layered hard materials
- Use more quantitative theories
  - non m.f.

# *Conclusion*

To control the surfaces we must use cleaner environments:

Micro and nano features for bio chips deserve the same standards as the computer chip industry

Clean rooms with wet and dry facilities

*Bio + Nano*







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*Keck Center for Computational Biology*

Mike Hogan, Lian Gao,  
Rosina Georgiadis,  
Yuri Fofanov

Thanks to NIH, NASA, DOE,  
Welch Foundation, ARP  
&SDSC, PNNL, PSC, NCI, MSI



