

# **Causal inference and** discovery

with perspectives in Earth sciences



### **Prof. Dr. Jakob Runge**



### HELMHOL



Group leader Causal Inference at Institute of Data Science Jena



Chair of Climate Informatics at



# **Causal inference group at DLR and TU Berlin**

### Mission

Developing theory, methods, and accessible tools for causal inference in Earth system sciences and beyond







 $\rightarrow$  open positions: climateinformaticslab.com



**Object classification and localization** 



**Turing-Award** 2018 LeCun, Hinton, Bengio





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Reichstein et al. 2019



Turing-Award 2018 LeCun, Hinton, Bengio

Reichstein et al. 2019



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Krich. 2021



Understand ecosystem respiration





**1. Experimentation:** Randomized controlled trials, gene knockout experiments, etc



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**2. Simulation models:** Based on underlying physics (if available)



embryonic stem cells with targeted gene disruption

microiniection

implant injected blastocysts into uterus of pseudo-pregnant

blastocust

foster mother

inner cell mass

mouse with tissue contribution from both

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Ethical issues, expensive, compliance, not possible, ...

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Expensive, time consuming, and only approximation of reality, ...



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Ethical issues, expensive, compliance, not possible, ...

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Expensive, time consuming, and only approximation of reality, ...

**3. Causal inference:** Based on observational <u>and/or</u> experimental data



## **Causal inference**

Causal inference is a framework to answer causal questions from observational <u>and/or</u> experimental data.





J Pearl **Turing-Award 2011** 



Spirtes, Glymour, Scheines



JD Angrist and GW Imbens *Nobel prize 2021* 

III. Niklas Elmehed © Nobel Prize Outreach

# **Causal inference**

# Causal inference is a framework to answer causal questions from observational <u>and/or</u> experimental data.

Pearl's hierarchy	Activity	Questions	Examples	JUDEA PEARL MINNER OF THE TURING AWARD AND DANA MACKENZIE
3. Counterfactuals	Retrospection,	Why? What If	Did climate change cause this extreme event?	THE
P(y' <sub>x'</sub>  x, y)	Imagining, Understanding	I nad done	Was it aspirin that stopped my headache?	BOOK OF WHY
2. Intervention	Intervening	What if I do?	What causes what in the data? Infer underlying mechanisms, future impacts of	a b THE NEW SCIENCE OF CAUSE AND EFFECT
P(y do(x))			What if I take aspirin?	Construction
1. Association	Seeing	What is? How	Pattern recognition, correlation networks, statistical weather forecast (if the system is	-
P(y x)		related?	not changing)	



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 $X_{\rm A} := f_{\rm A}(X_{\rm E}, \eta_{\rm A})$  $X_{\rm C} := f_{\rm C}(X_{\rm A}, X_{\rm E}, \eta_{\rm C})$  $X_{\rm E} := f_{\rm E}(\eta_{\rm E})$ 

where the graph is <u>acyclic</u> and noise terms are <u>independent</u>. This SCM entails a factorized distribution  $P(\mathbf{X}) = P(X_{\rm C}|X_{\rm A}, X_{\rm E})P(X_{\rm A}|X_{\rm E})P(X_{\rm E})$ 



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An experiment / intervention is then represented by the intervened SCM

$$egin{aligned} X_\mathrm{A} &:= x' \ X_\mathrm{C} &:= f_\mathrm{C}(X_\mathrm{A}, X_\mathrm{E}, \eta_\mathrm{C}) \ X_\mathrm{E} &:= f_\mathrm{E}(\eta_\mathrm{E}) \end{aligned}$$

Which results in the interventional distribution that defines causal effects:

 $P(X_{\rm C}|do(X_{\rm A}=x')) \neq P(X_{\rm C}|X_{\rm A}=x')$ 

Two types of tasks:

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### Two types of tasks:

 Utilize qualitative causal knowledge in form of directed acyclic graphs including observed and unobserved / latent variables



2. Learn causal graphs based on general assumptions





<u>Causal effect estimation</u>: Given causal graph and data, compute causal effect of intervention from observational distribution P(V)



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'Correlation' regression



Causal regression

$$Y = \boxed{\beta_{YX \cdot Z}} X + \beta_{YZ \cdot X} Z$$



**Optimal** causal effect estimators (Runge NeurIPS 2021)



**Task:** Given data and *general assumptions*, estimate causal graph from observational distribution P(V)



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**Task:** Given data and *general assumptions*, estimate causal graph from observational distribution P(V)

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  - → Constraint-based causal discovery (Spirtes et al. 2000)

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- Assumptions on functional dependencies and noise distributions
   → *Restricted structural causal modeling* (Peters et al. 2018)



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- Score-based Bayesian network learning



**Task:** Given data and *general assumptions*, estimate causal graph from observational distribution P(V)

Time series case:



- $X^2$   $\chi^3$   $M_{M}$   $M_{M}$

**Task:** Given data and *general assumptions*, estimate causal graph from observational distribution P(V)

#### Time series case:

• **PCMCI causal discovery framework** (Runge et al. SciAdv 2019, UAI 2020, Gerhardus and Runge NeurIPS 2020)



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#### Time series case:

- **PCMCI causal discovery framework** (Runge et al. SciAdv 2019, UAI 2020, Gerhardus and Runge NeurIPS 2020)
- Assuming no instantaneous effects

   → Granger causality (Granger 1969)

 $\dots \rightarrow$  see Runge et al. NatComm Perspective (2019)



**Causal inference engine (Pearl):** Given a query, a causal graph and data, output estimand in terms of observational distribution P(V)

$$P(Y|do(X=x)) = \int P(y|x,z)P(z)dz$$



**Causal inference engine (Pearl):** Given a query, a causal graph and data, output estimand in terms of observational distribution  $P(V) \rightarrow estimand can be estimated with (deep) ML$ 

$$P(Y|do(X=x)) = \int P(y|x,z)P(z)dz \qquad \mathbf{X}$$
$$\implies \hat{Y} = \int \hat{f}(X=x, Z=z)p(z)dz$$



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### Causal graph learning:

• ML for non-parametric conditional independence testing (Runge AISTATS 2018, Strobl et al., 2017, ...)



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# testing



- Causal graph learning:
  - ML for non-parametric conditional independence testing (Runge AISTATS 2018, Strobl et al., 2017, ...)
  - Structure learning as continuous optimization problem
    - $\rightarrow$  Brouillard et al., 2020, and many more recently

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### Causal graph learning:

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- ML for non-parametric conditional independence testing (Runge AISTATS 2018, Strobl et al., 2017, ...)
- Structure learning as continuous optimization problem → Brouillard et al., 2020, and many more recently
- Dimension-reduction to reconstruct variables



## **Challenges**



### Runge et al. (2019)



PERSPECTIVE

https://doi.org/10.1038/s41467-019-10105-3 OPEN

Inferring causation from time series in Earth system sciences

#### Challenges

#### Process:

- 1 Autocorrelation
- 2 Time delays
- 3 Nonlinear dependencies
- 4 Chaotic state-dependence
- 5 Different time scales
- 6 Noise distributions

#### Data:

- 7 Variable extraction
- 8 Unobserved variables
- 9 Time subsampling
- 10 Time aggregation
- 11 Measurement errors
- 12 Selection bias
- 13 Discrete data
- 14 Dating uncertainties

7

#### Computational / statistical:

- 15 Sample size
- 16 High dimensionality

4

17 Uncertainty estimation



## Challenges



### Runge et al. (2019)



PERSPECTIVE

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16

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Inferring causation from time series in Earth system sciences

6

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### Schölkopf et al. (2020) **Toward Causal Representation Learning**

This article reviews fundamental concepts of causal inference and relates them to crucial open problems of machine learning, including transfer learning and generalization, thereby assaying how causality can contribute to modern machine learning research.

By BERNHARD SCHÖLKOPF<sup>(D)</sup>, FRANCESCO LOCATELLO<sup>(D)</sup>, STEFAN BAUER<sup>(D)</sup>, NAN ROSEMARY KE, NAL KALCHBRENNER, ANIRUDH GOYAL, AND YOSHUA BENGIO<sup>®</sup>

#### ABSTRACT | The two fields of machine learning and graphical I. INTRODUCTION

applies in the opposite direction: we note that most work in causality starts from the premise that the causal variables are given. A central problem for AI and causality is, thus, causal representation learning, that is, the discovery of highlevel causal variables from low-level observations. Finally, we delineate some implications of causality for machine learncommunities

causality arose and are developed separately. However, there If we compare what machine learning can do to what is, now, cross-pollination and increasing interest in both fields animals accomplish, we observe that the former is rather to benefit from the advances of the other. In this article, limited at some crucial feats where natural intelligence we review fundamental concepts of causal inference and relate excels. These include transfer to new problems and any them to crucial open problems of machine learning, including form of generalization that is not from one data point transfer and generalization, thereby assaying how causality to the next (sampled from the same distribution), but can contribute to modern machine learning research. This also rather from one problem to the next-both have been termed generalization, but the latter is a much harder form thereof, sometimes referred to as horizontal, strong, or outof-distribution generalization. This shortcoming is not too surprising, given that machine learning often disregards information that animals use heavily: interventions in the world, domain shifts, and temporal structure-by and ing and propose key research areas at the intersection of both large, we consider these factors a nuisance and try to engineer them away. In accordance with this, the majority of current successes of machine learning hoil down to large

## Challenges



#### Runge et al. (2019)



PERSPECTIVE

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Inferring causation from time series in Earth system sciences

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#### Computational / statistical:

- 15 Sample size
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### Need for close collaboration between method developers and domain scientists

t-5 t-4 t-3 t-2 t-1 



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> pf<sup>©</sup>, Francesco Locatello<sup>©</sup>, Stefan Bauer<sup>©</sup>, Nan Rosemary Ke, iirudh Goyal, and Yoshua Bengio®

#### machine learning and graphical I. INTRODUCTION

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# Applications

- 1. Learning causal graphs to understand mechanisms
- **2. Quantifying causal mechanisms:** link strength and mediation analysis
- 3. Causally robust forecasting
- 4. Causally validating ML methods
- 5. Evaluating climate models and constraining climate change projections
- 6. Hybrid physical-ML modeling
- 7. Detection and attribution of extreme events
- 8. ...





## **Causal mediation analysis**

 Pathway mechanisms between El Nino and Indian monsoon through sea-level pressure system



### Runge et al., NatComm 2015

## **Causal mediation analysis**

• Pathway mechanisms between **El Nino** and **Indian monsoon** through sea-level pressure system





### Runge et al., NatComm 2015

## **Causal mediation analysis**

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Runge et al., NatComm 2015
# **Simulation model evaluation**

- Simple statistics can be right for the wrong reasons
- Idea: Compare climate models and observations in terms of causal relationships



-292	
COMMUNICATIONS	

ARTICLE		(A) Check
https://doi.org/10.1038/s41467-020-15195-y	OPEN	

Causal networks for climate model evaluation and constrained projections

Peer Nowack@ 1.2.3.4<sup>123</sup>, Jakob Runge @ <sup>5,1</sup>, Veronika Eyring @ <sup>6,7</sup> & Joanna D. Haigh @ <sup>1,2</sup>

#### Nowack et al. NatComm. (2020)

# **Simulation model evaluation**

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- Idea: Compare climate models and observations in terms of causal relationships







• **Causal inference:** Framework to answer causal questions from empirical data



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- Two settings:
  - 1) Utilize qualitative causal knowledge (graphs)
  - 2) Learn causal graphs (then utilize them)



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#### Software:

Tigramite, pcalg, TETRAD, causalfusion, CauseMe, ...





#### **Thank you! Questions?**

