

The worldwide leaf economic spectrum



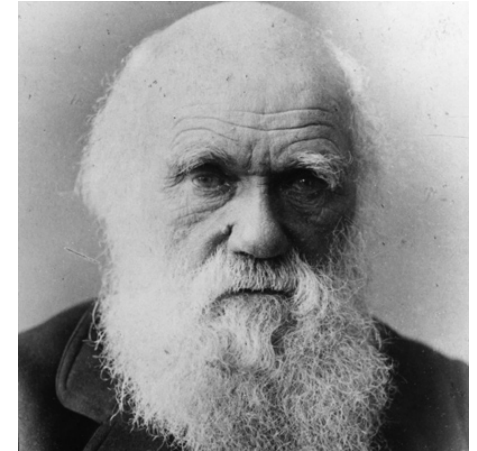
How causal discovery algorithms forced me
to re-imagine its generating causes

Some basic notions from evolutionary ecology...



Sir Ronald Fisher

- Evolutionary fitness
- Adaptive value of a trait



Charles Darwin

Evolutionary fitness

A cohort of individuals having a trait value « x » in environment E

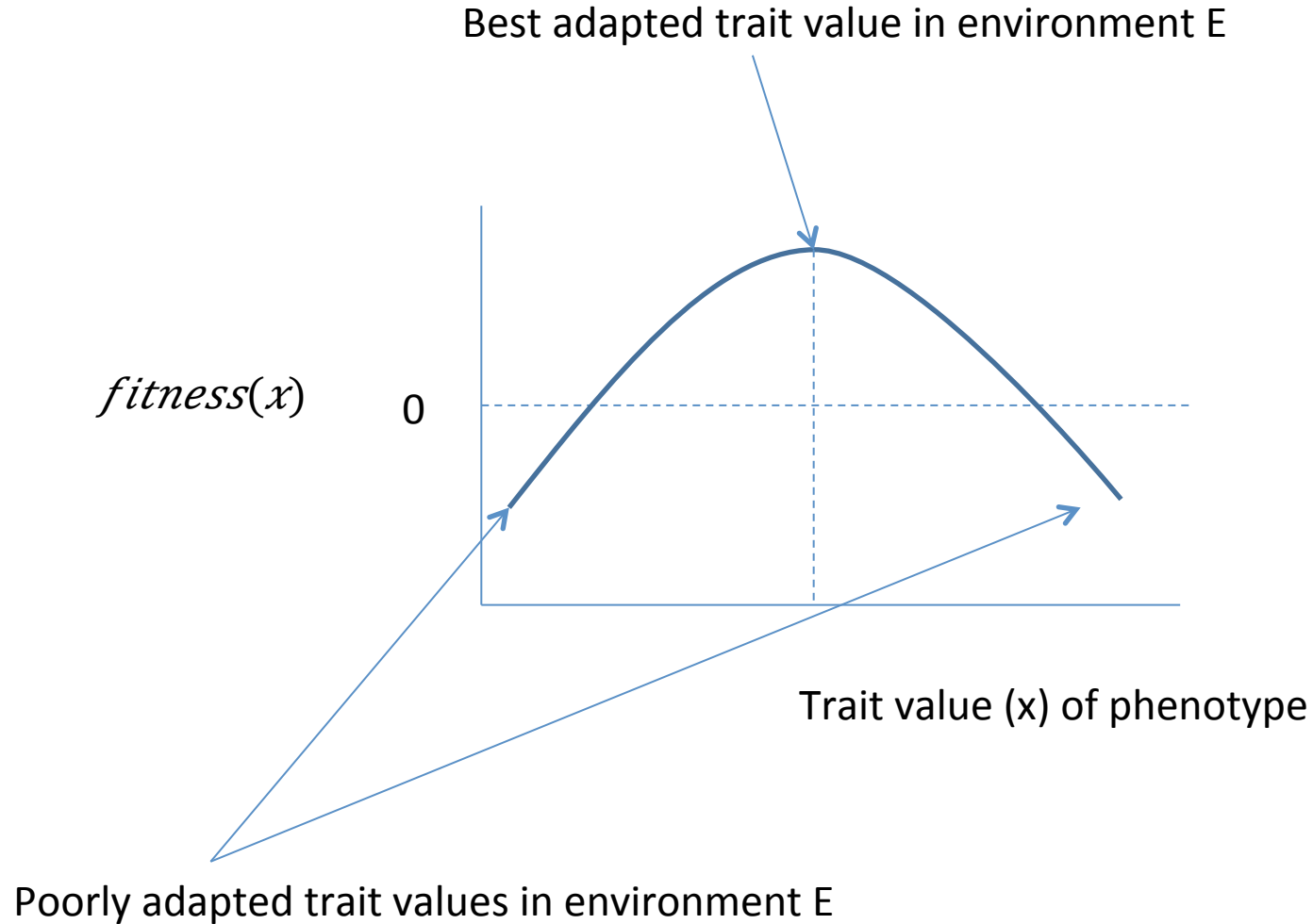
Age	Average # offspring / survival	Prob of surviving to age i	Expected # offspring
1	0	0.8	0x0.8=0
2	2	0.4	2x0.4=0.8
...			
x	3	0.1	3x0.1=0.3

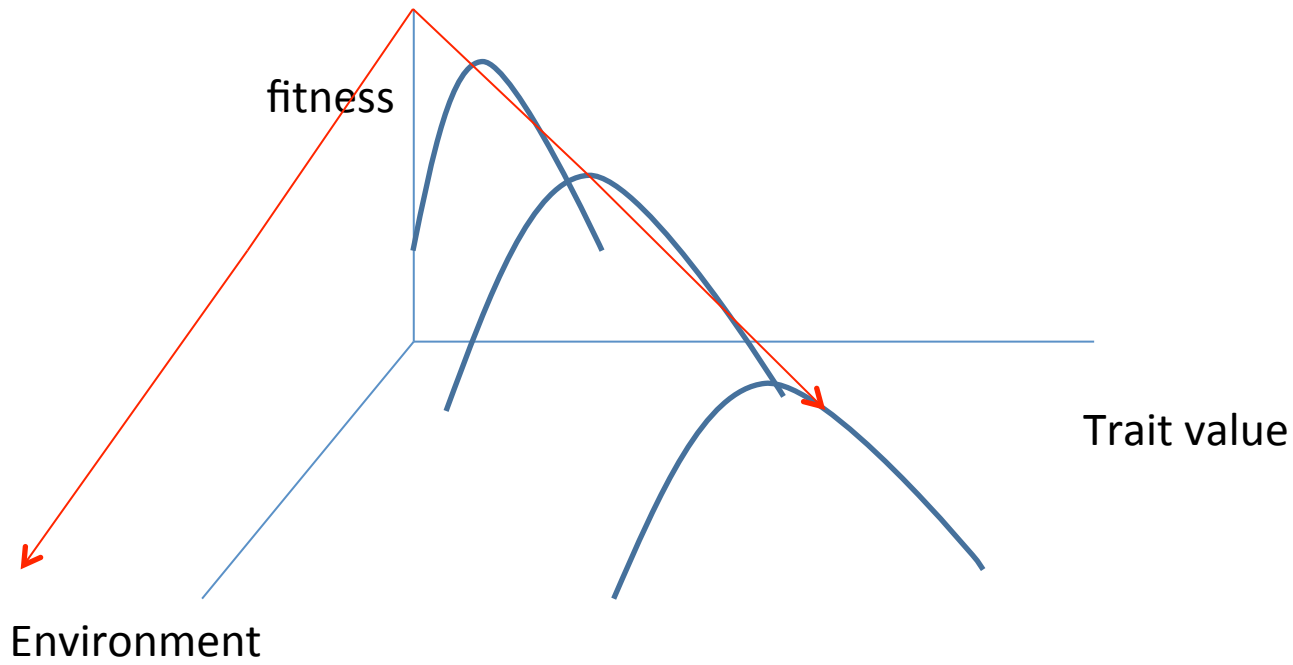
Net reproductive output for this genotype or phenotype:

$$R_0(x) = \sum (\text{average reproduction at age } i) (\text{probability of surviving to age } i)$$

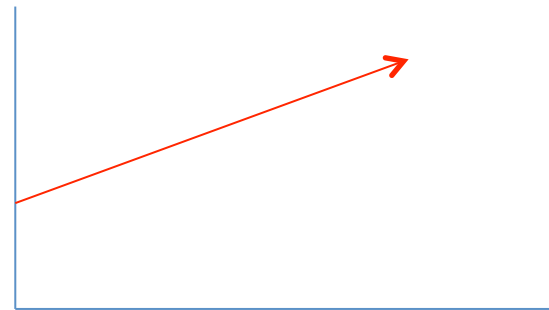
$$\text{fitness}(x) = R_0(x) - R_0$$

Adaptive value of a trait (or suite of traits)

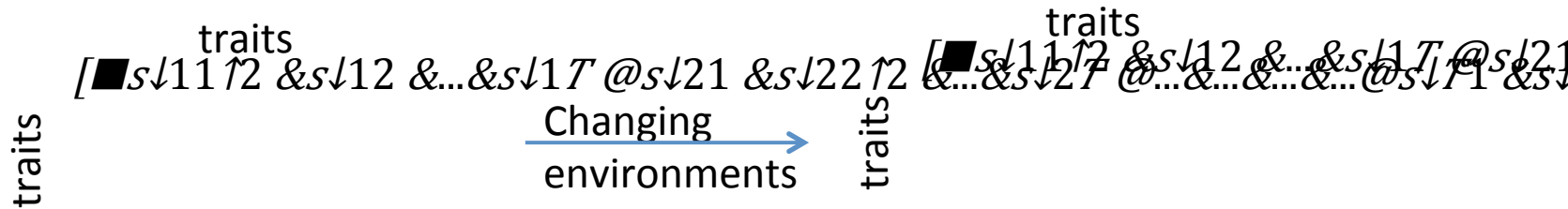




Trait value
with highest
fitness



Traits often show complicated patterns of covariation



These patterns of covariation can reflect:

- Common selection pressures
- Tradeoffs between traits to maximize fitness
- Physical constraints

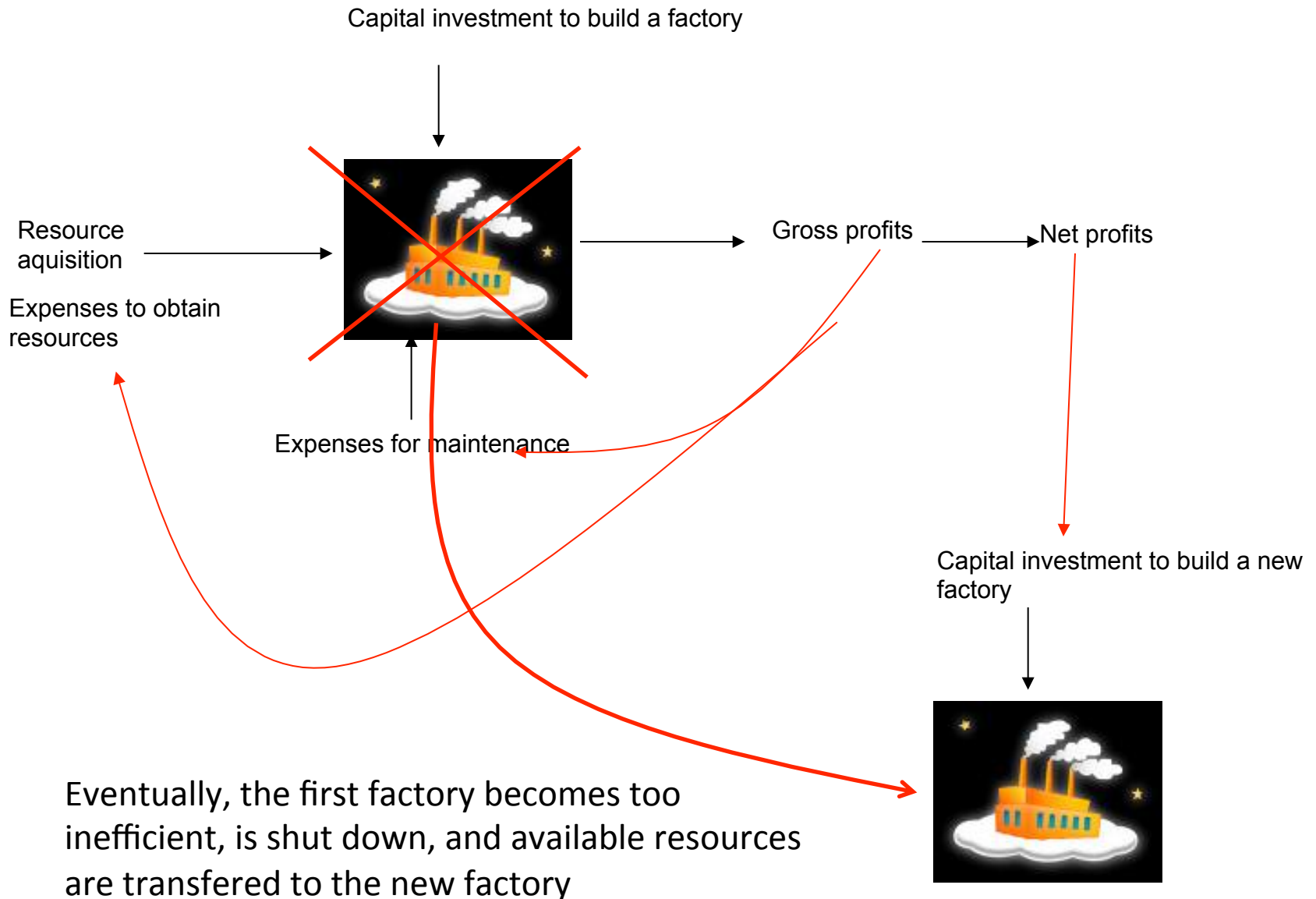
What are the causal process generating these patterns of trait covariation?



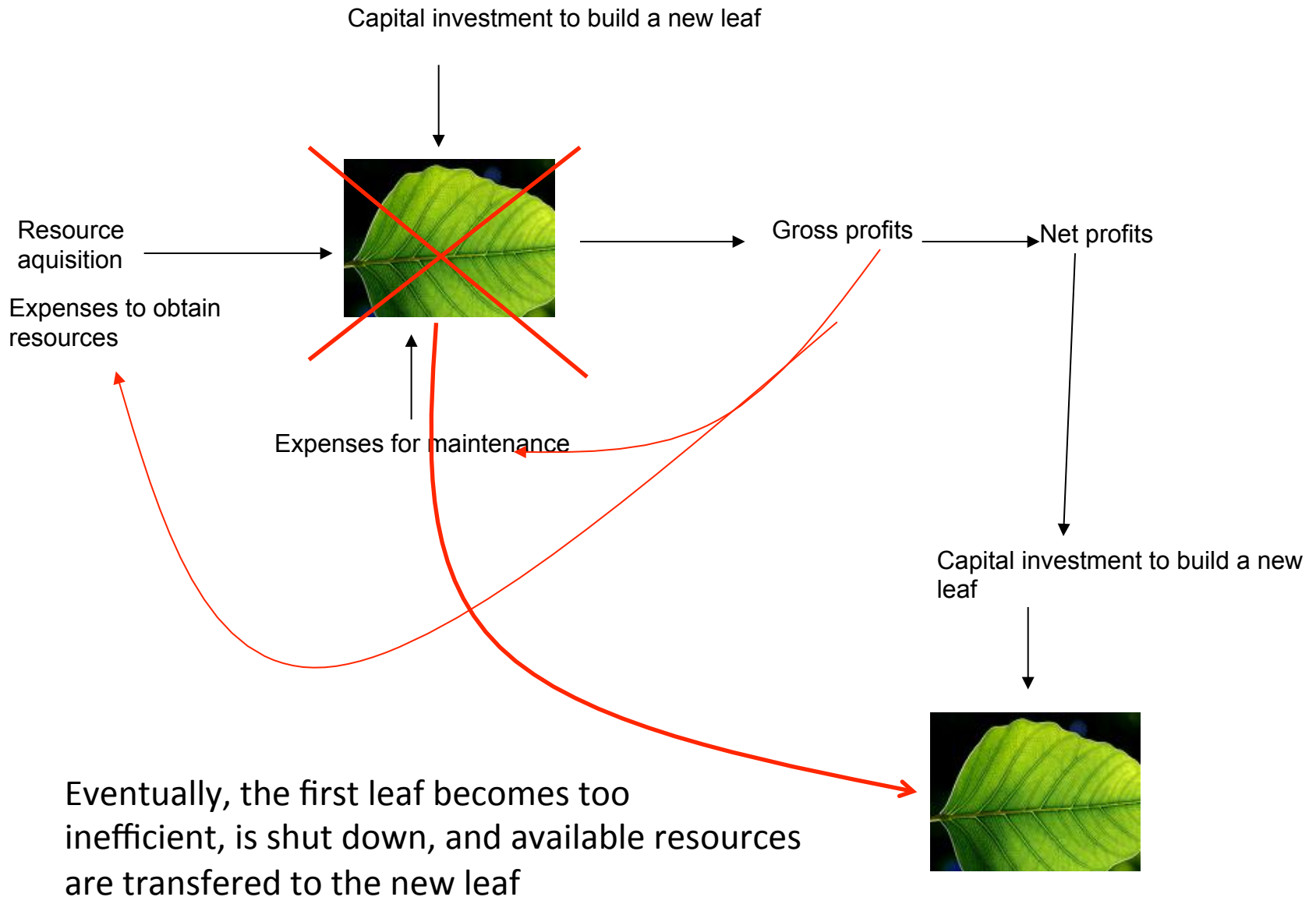
How evolutionary ecologists view co-ordination in leaf traits



An individual plant is a company & an individual leaf is a factory



An individual plant is a company & an individual leaf is a factory



Abstract

Bringing together leaf trait data spanning 2,548 species and 175 sites we describe, for the first time at global scale, a **universal spectrum of leaf economics** consisting of key chemical, structural and physiological properties. The spectrum runs from quick to slow return on investments of nutrients and dry mass in leaves, and **operates largely independently of growth form, plant functional type or biome**. Categories along the spectrum would, in general, describe leaf economic variation at the global scale better than plant functional types, because functional types overlap substantially in their leaf traits. Overall, **modulation of leaf traits and trait relationships by climate is surprisingly modest**, although some striking and significant patterns can be seen. Reliable quantification of the leaf economics spectrum and its interaction with climate will prove valuable for modelling nutrient fluxes and vegetation boundaries under changing land-use and climate.

articles

The worldwide leaf economics spectrum

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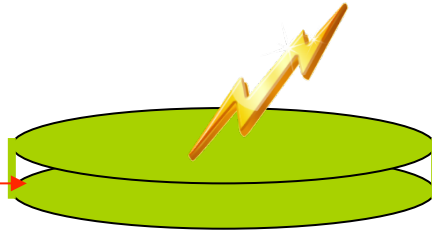
¹Wright, I. et al. (2004). Nature 428: 821-827.

Measured variables

Specific leaf mass (g/cm^2)

dry mass = allocation to convert energy
into sugars

surface area = amount of photons captured

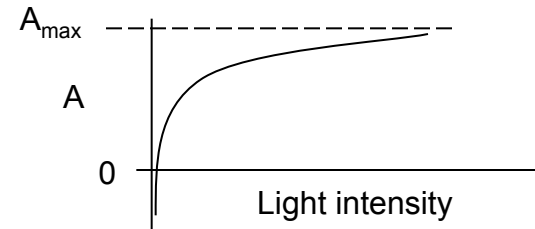


N_m : nitrogen content of leaf (mg/g)

N is the limiting element
for photosynthetic
enzymes



A_{max} : Maximum net photosynthetic rate ($\mu\text{mol}/\text{g}/\text{s}$)



R_m : leaf respiration rate ($\mu\text{mol}/\text{g}/\text{s}$)

Respiration measures the
metabolic activity of the leaf

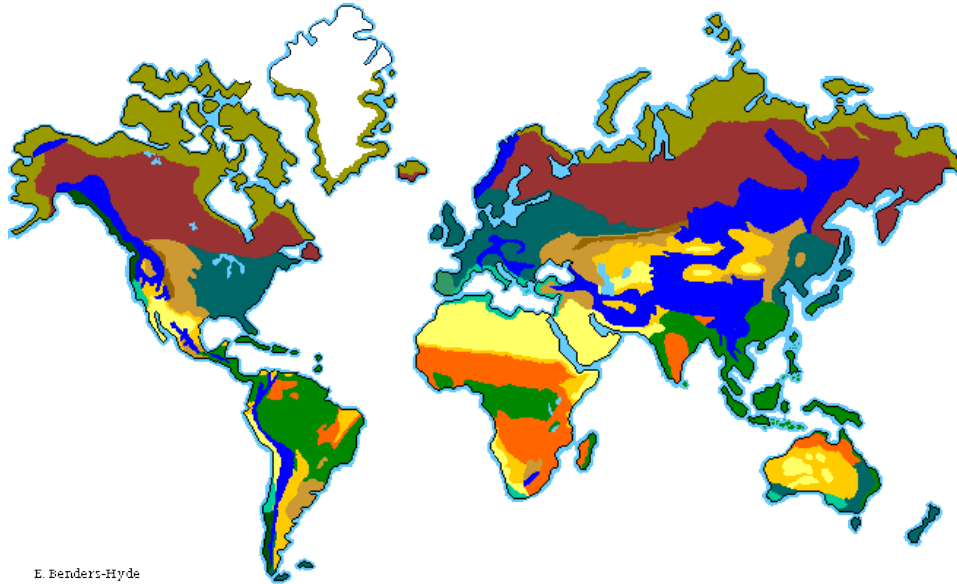


LL: Leaf lifespan (d)

Average # days until plant allows a leaf to
die

The worldwide leaf economic spectrum

2548 species occurring in 175 sites worldwide



Prior expectation: the different environments would select for different patterns of covariation

Found: essentially the same relationships between these « economic » variables irrespective of habit or taxonomy.



$$A_{\max} - LMA - N_m$$

$$LL - LMA - R_m$$

$$P_m - LMA - N_m$$

$$A_m - LMA - N_m$$

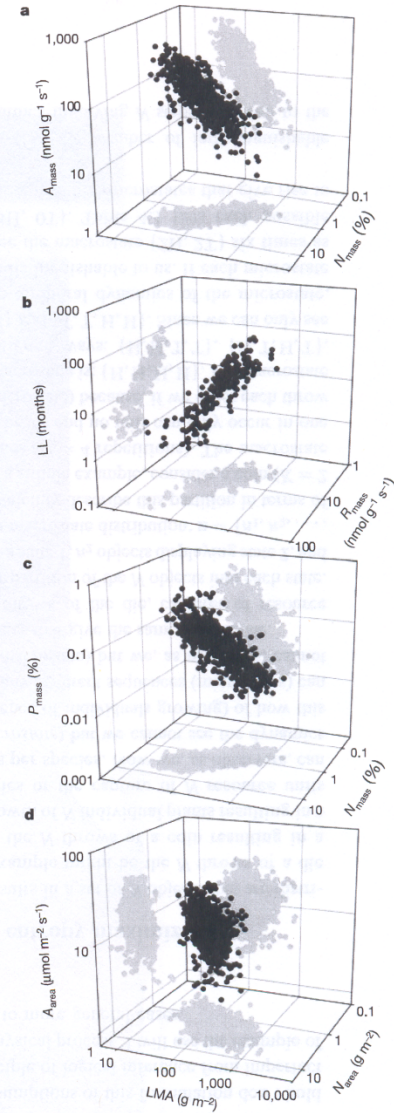
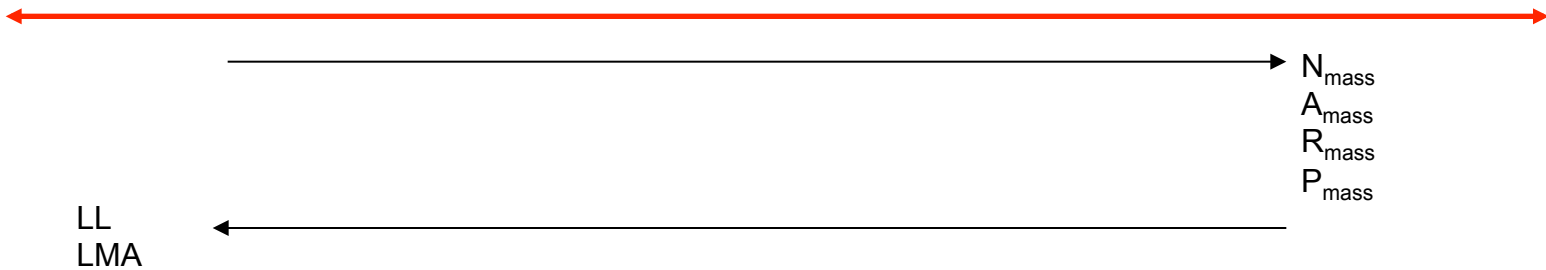


Figure 2 Three-way trait relationships among the six leaf traits with reference to LMA, one of the key traits in the leaf economics spectrum. The direction of the data cloud in three-dimensional space can be ascertained from the shadows projected on the floor and walls of the three-dimensional space. Sample sizes for three-way relationships are necessarily a subset of those for each of the bivariate relationships. **a.** A_{\max} , LMA and N_m ; 706 species. **b.** LL, R_m and LMA; 217 species. **c.** N_m , P_m and LMA; 733 species. **d.** A_{area} , LMA and N_{area} ; 706 species.

1st principal axis of a PCA explains ~ 80% of variation



Resource conservation

- Photosynthetic rate low even under optimal conditions
- Respiration rate low
- Low concentrations of mineral nutrients
- Long lifespan
- Thick, (often small) leaves with cell structure maintained by thick cell walls (dense tissues)



Resource acquisition

- High maximum photosynthetic rate
- High respiration rate
- High concentrations of mineral nutrients
- Short lifespans
- Thin, (often large) leaves with cell structure maintained by water turgour



Generating causes?
What we thought we knew...



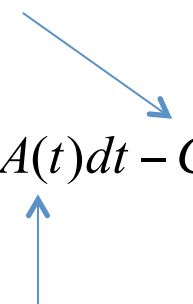
Theoretical causes of variation in leaf lifespan

Assumption

Natural selection acts to maximize the cumulative net amount of carbon fixed by the leaf per unit time (g), and this production is calculated over the lifespan of the leaf.

$$g = \text{total net production of carbon/leaf lifespan} = G/t$$

Construction cost
(carbon invested to construct
the leaf)

$$g = \frac{1}{t} \left(\int_0^t A(t) dt - C \right)$$


Net instantaneous photosynthetic
rate ($\mu\text{mol/g/s}$)

$$g = \frac{1}{t} \left(\int_0^t A(t) dt - C \right)$$

$$A(t) = a \left(1 - \frac{t}{b} \right) = a \left(\frac{b-t}{b} \right)$$

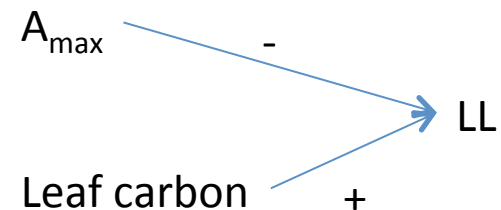
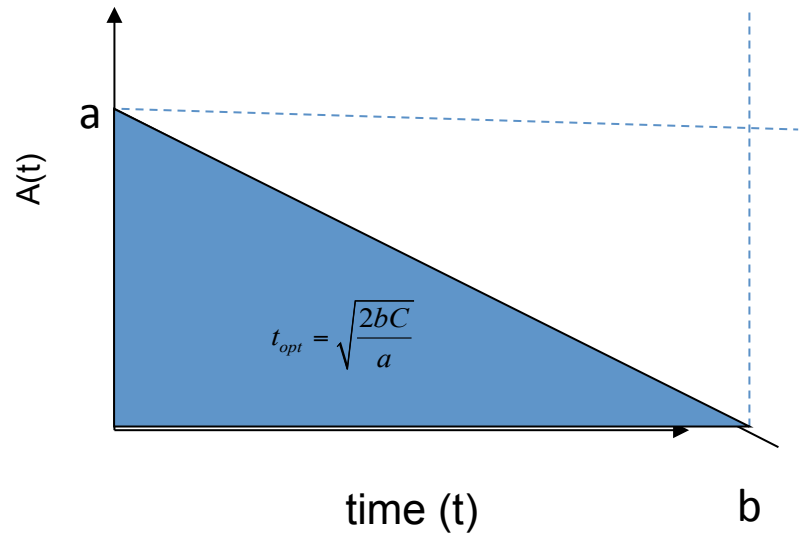
$$\int_0^t A(t) dt = \left[at - \frac{at^2}{2b} \right]$$

$$g = \frac{1}{t} \left(at - \frac{a}{2b} t^2 - C \right)$$

$$g = \frac{-2bC + 2abt - at^2}{2bt}$$

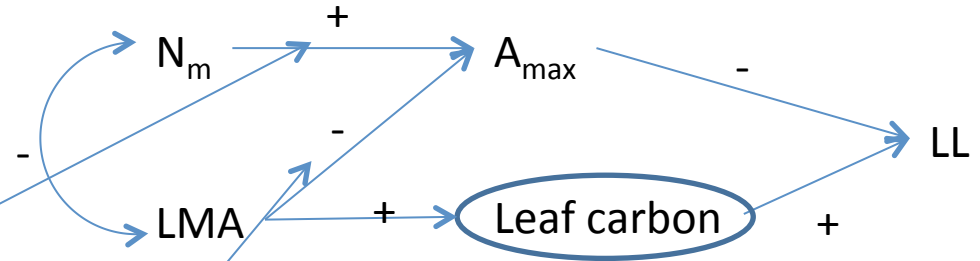
Solving for t when $dg/dt = 0$

$$t_{opt} = \sqrt{\frac{2bC}{a}}$$



Initial causal models

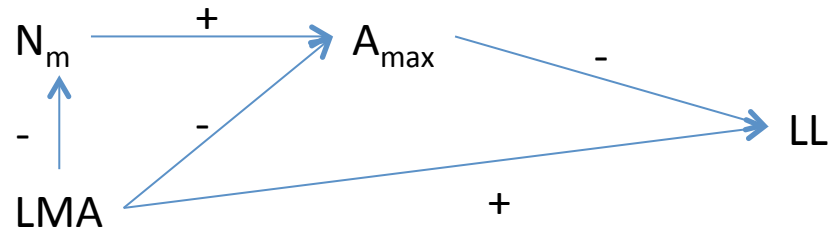
Wright, I. et al. (2004). Nature 428: 821-827.



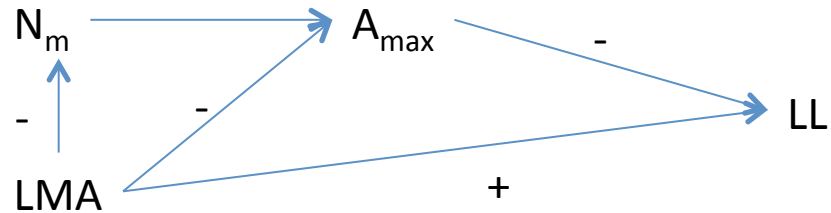
Most leaf nitrogen is in photosynthetic enzymes: more enzymes \rightarrow more photosynthesis

Cells with thicker cell walls, and structural cells (that have no cytoplasm or enzymes), will increase mass while decreasing total carbon fixation and decreasing total nitrogen

My translation of their explanation



$\chi^2 = 12.825, df = 1, p = 0.0003$



Is there any ordering of these four variables that fits the observed patterns of covariation, without requiring common latent causes?

How to answer this:

PC algorithm, testing each equivalent model using a d-sep test of significance¹.

Answer: No.

¹Shiple, B. 2000. A new inferential test for path models based on directed acyclic graphs. Structural Equation Modeling 7206-218.

Where is the latent variable hiding and what might it be?

Vanishing tetrads (assuming linear relationships & MVN distribution)

$$\blacksquare \rho_{12} \rho_{34} - \rho_{14} \rho_{23} = 0 @ \rho_{13} \rho_{24} - \rho_{14} \rho_{23} = 0 @ \rho_{13} \rho_{24} - \rho_{12} \rho_{34} =$$

Vanishing tetrad algorithm

Given a set of 4 observed variables in which no pair of variables are independent conditional on any subset of other variables (including the empty set):

- If the tetrad equation does not equal zero, choose another tetrad equation
- If the tetrad equation does equal zero then there is a latent variable that forms an chokepoint at either (or both) of the pairs of variables not included in the tetrad equation.

Where is the latent variable hiding and what might it be?

Of the three possible tetrad equations involving these four variables, only one is significantly different from zero (i.e. does not vanish):

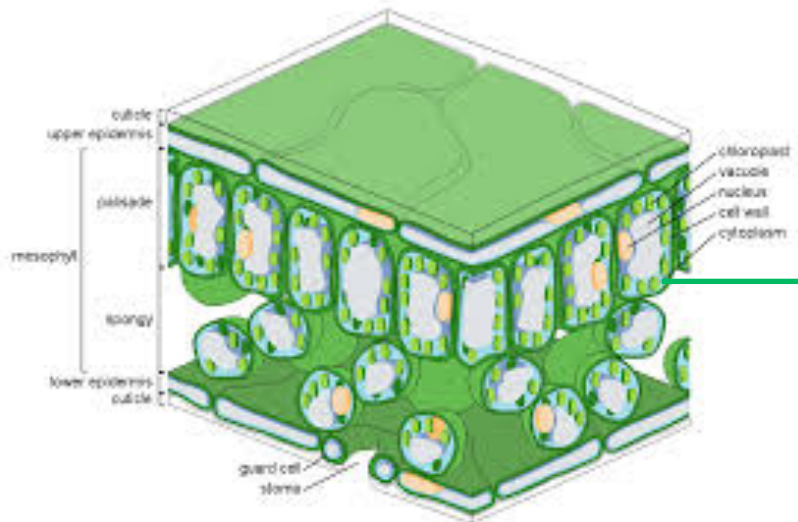
$$\rho \downarrow \ln(LL), \ln(N \downarrow M) \quad \rho \downarrow \ln(LMA), \ln(A \downarrow M) - \rho \downarrow \ln(LL), \ln(LMA) \\ \rho \downarrow \ln(A \downarrow M), \ln(N \downarrow M) \neq 0$$

This means that all causal paths linking every pair of variables except for LL and A_M pass through the same latent variable.

Where is the latent variable hiding and what might it be?

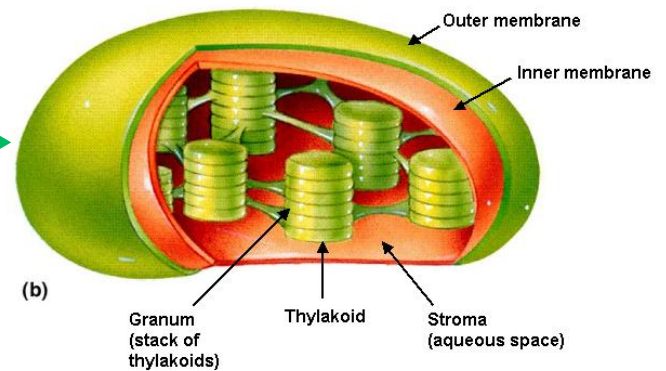
Variable 1	Variable 2	All paths linking pair pass through a latent?
SLM	A_{mass}	✓
SLM	LL	✓
SLM	N_{mass}	✓
A_{mass}	N_{mass}	✓
A_{mass}	LL	✗
LL	N_{mass}	✓

Where is the latent variable hiding and what might it be?

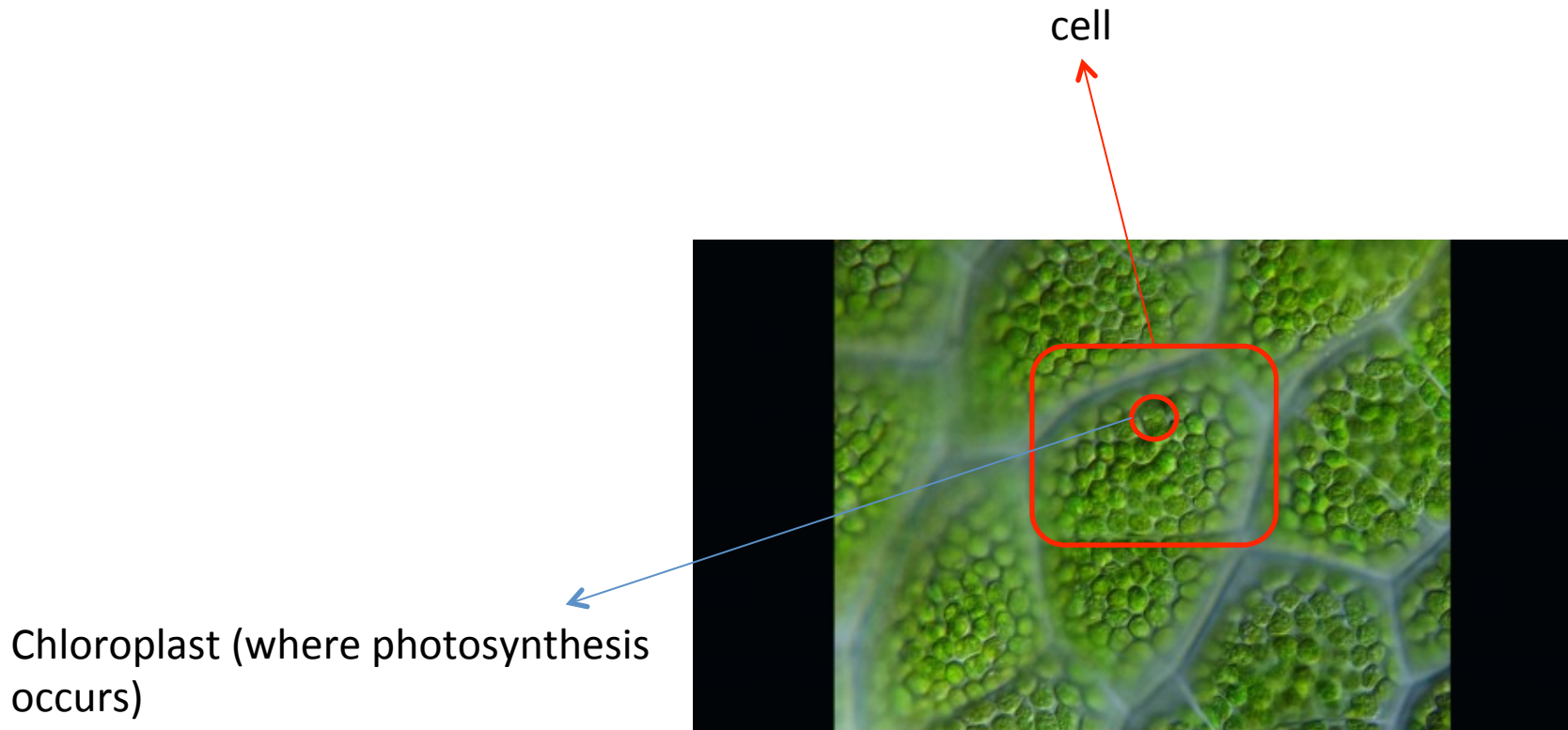


Randy Moore, Dennis Clark, and Darrell Vodopich, Botany Visual Resource Library © 1999 The McGraw-Hill Companies, Inc. All rights reserved.

Three-dimensional Model of Chloroplast Membranes



Where is the latent variable hiding and what might it be?



Where is the latent variable hiding and what might it be?

chloroplasts \propto volume of cytoplasm

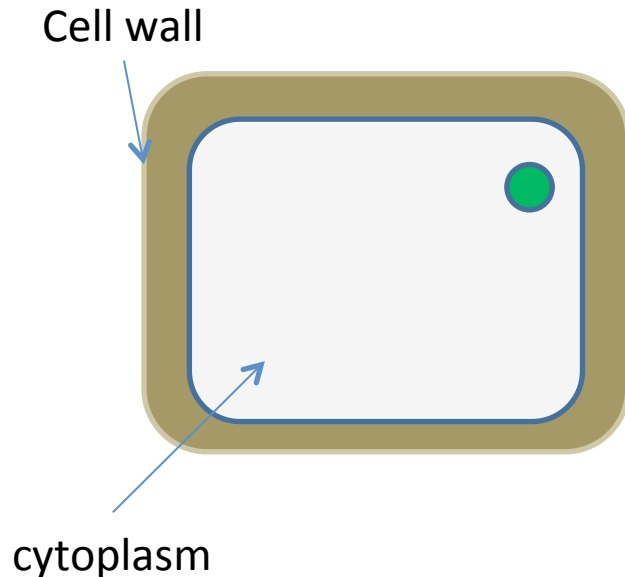
photosynthetic rate per chloroplast is very much less variable than the number of chloroplasts per leaf

Photosynthetic rate per leaf \propto volume of cytoplasm

Nitrogen content per leaf \propto volume of cytoplasm

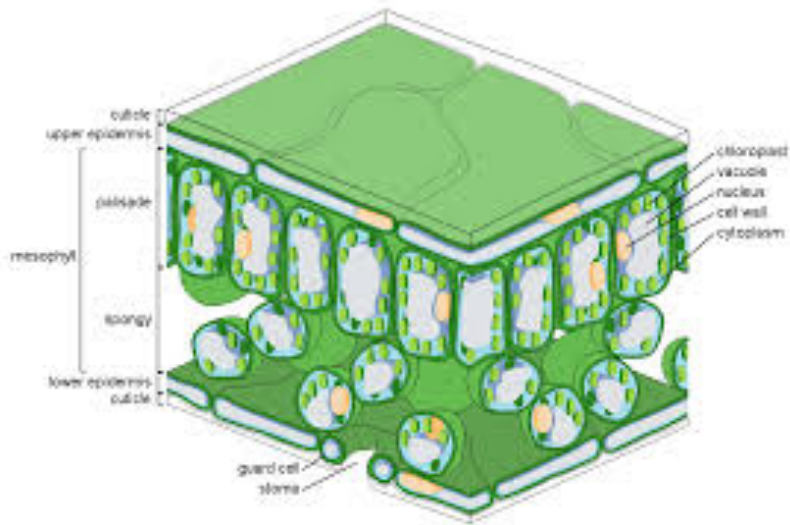
Leaf dry mass is overwhelmingly in the cell walls

Leaf dry mass \propto volume of cell walls



$$\frac{\text{total cytoplasmic volume}}{\text{total cell wall volume}} \quad V_{\downarrow c} / V_{\downarrow w}$$

Where is the latent variable hiding and what might it be?



$$V_{lc} / V_{total} / dry\ mass \propto A_{mass}$$

$$V_{lc} / V_{total} / dry\ mass \propto N_{mass}$$

$$V_{lc} / V_{total} / dry\ mass \propto 1/C$$

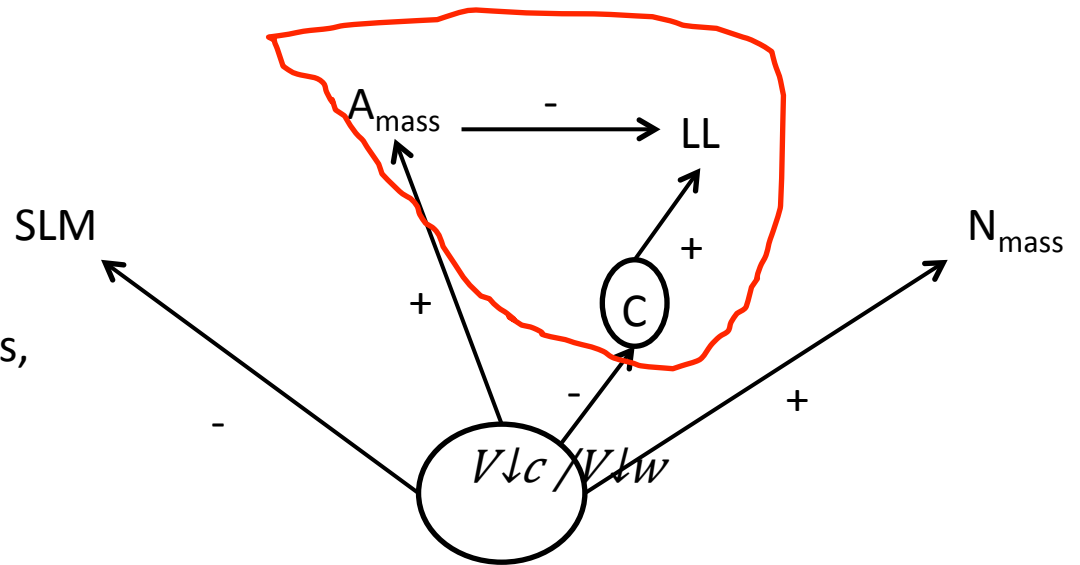
SLM = (tissue density) * thickness

$$V_{lc} / V_{total} / SLM$$

Where is the latent variable hiding and what might it be?



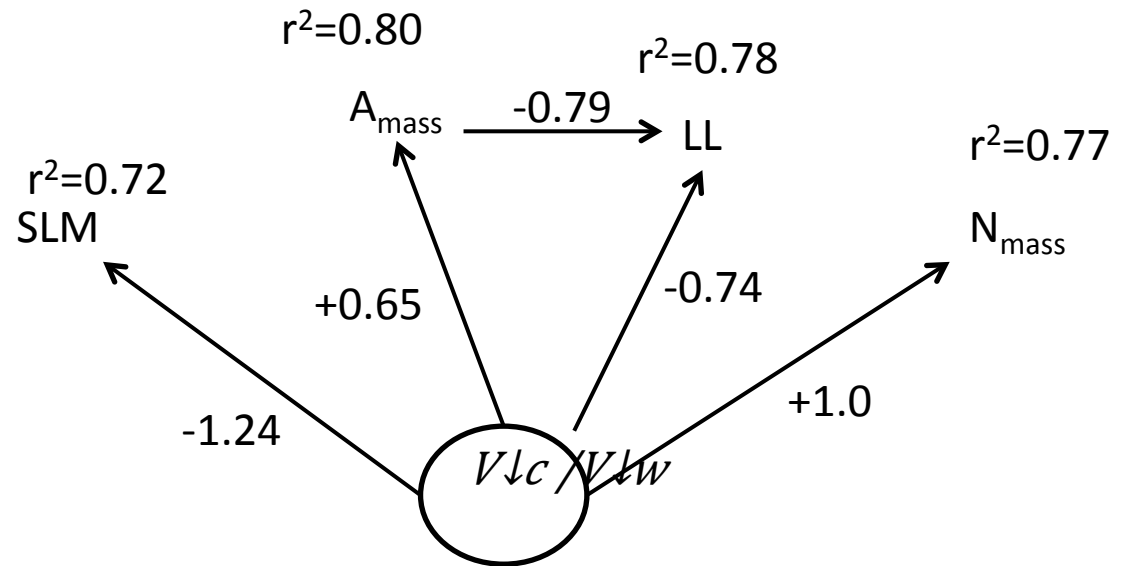
Kikuzawa's model from natural selection
+ detected by non-zero tetrad equation



Agrees with all tetrad equations,
Two vanish, one doesn't

All observed variables ln-transformed

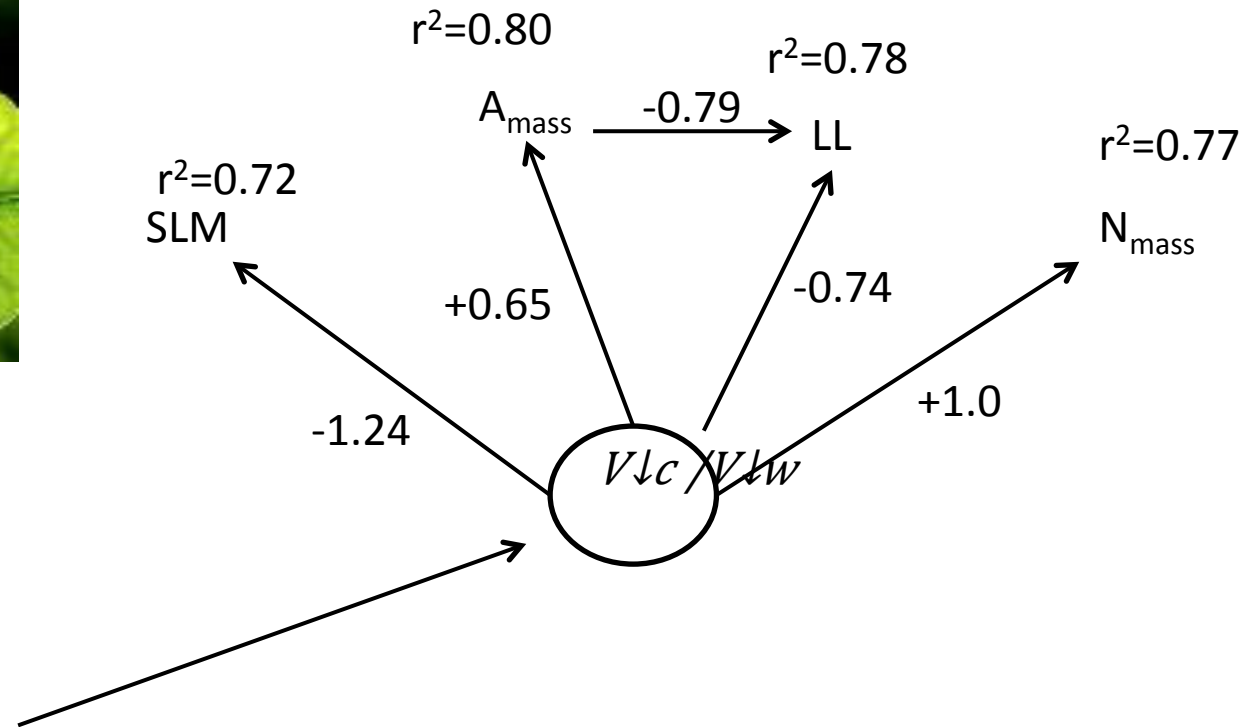
Where is the latent variable hiding and what might it be?



$\chi^2 = 4.080, df = 3, P = 0.39$

All observed variables ln-transformed

What's next?



Next step: this ratio can be estimated (after a lot of work) to provide an independent test of this causal hypothesis